

GALAXY CLUSTER ENVIRONMENTS OF RADIO SOURCES

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ABSTRACT

Using the Sloan Digital Sky Survey (SDSS) and the FIRST (Faint Images of the Radio Sky at Twenty Centimeters) catalogs, we examined the optical environments around double-lobed radio sources. Previous studies have shown that multi-component radio sources exhibiting some degree of bending between components are likely to be found in galaxy clusters. Often this radio emission is associated with a cD-type galaxy at the center of a cluster. We cross-correlated the SDSS and FIRST catalogs and measured the richness of the cluster environments surrounding both bent and straight multi-component radio sources. This led to the discovery and classification of a large number of galaxy clusters out to a redshift of $z \sim 0.5$. We divided our sample into smaller subgroups based on their optical and radio properties. We find that FR I radio sources are more likely to be found in galaxy clusters than FR II sources. Further, we find that bent radio sources are more often found in galaxy clusters than non-bent radio sources. We also examined the environments around single-component radio sources and find that single-component radio sources are less likely to be associated with galaxy clusters than extended, multi-component radio sources. Bent, visually-selected sources are found in clusters or rich groups $\sim 78\%$ of the time. Those without optical hosts in SDSS are likely associated with clusters at even higher redshifts, most with redshifts of $z > 0.7$.

Subject headings: galaxies: clusters: general — galaxies: groups: general — radio continuum: galaxies

1. INTRODUCTION

Galaxy clusters are the largest gravitationally bound objects in the universe. They are typically composed of $\sim 30 - 1000$'s of galaxies, diffuse, hot gas, and dark matter. As such, they can be used as tracers for studying large-scale structure (Bahcall 1988; Postman et al. 1992; Carlberg et al. 1996; Ikebe et al. 1996; Jee et al. 2007; Bradač et al. 2008; Kartaltepe et al. 2008). Clusters also provide an excellent laboratory for the study of galaxy formation and evolution in dense environments (Butcher & Oemler 1978, 1984; Garilli et al. 1999; Thomas et al. 2010). Currently there are thousands of known, spectroscopically confirmed, clusters with redshifts $z < 0.3$, but few spectroscopically confirmed with redshifts above $z \sim 1.0$.

A common method for detecting galaxy clusters is through optical surveys (Abell 1958; Zwicky et al. 1968; Abell et al. 1989; Lumsden et al. 1992; Dalton et al. 1994; Gal et al. 2003; Miller et al. 2005; Gladders et al. 2007; Koester et al. 2007a). Earlier methods of detecting galaxy clusters involved visual selection from photographic plates, but more recent techniques involve automated methods such as identifying a red sequence and determining cluster members based on their colors and their proximity to other galaxies that lie on the red sequence (Bower et al. 1992; Ostrander et al. 1998; Gladders & Yee 2000; Bahcall et al. 2003; Gladders & Yee 2005; Koester et al. 2007a). This method can work without having to know the spectroscopic redshift of the cluster members.

Identifying galaxy clusters through optical selection can become increasingly difficult with increasing redshift. At high redshifts, the galaxies composing the cluster be-

come too faint to detect with an exposure time typical of that of a large area survey. In addition, the peak of the rest-frame optical emission of these high-redshift galaxies will be redshifted into the near-IR. It is possible to search for, and identify, clusters out to much higher ($z \sim 2$) redshifts using near-IR imaging (Daddi et al. 2004; Blanc et al. 2008), but the trade-off is in the small area coverage. New IR detectors with larger collecting areas (such as the NOAO¹ Extremely Wide Field Infrared Imager, NEWFIRM) should greatly help the effort of detecting high-redshift galaxy clusters using this technique. In addition, recent cluster searches in the mid-IR conducted using *Spitzer* have been successful in finding clusters, including some with $z > 1$ (Brodwin et al. 2006; Krick et al. 2009).

Galaxy clusters are also identified by detecting the X-ray emission of the hot gas of the intracluster medium (ICM). Due to the long exposure times needed to detect galaxy clusters in the X-ray, as well as the small field-of-view of most X-ray detectors, it is difficult to conduct a large-scale, systematic survey of X-ray detected galaxy clusters at high redshifts. X-ray detected clusters are also biased towards the most luminous, and therefore the most massive, galaxy clusters at high redshift, although samples at low redshift are complete (Reiprich & Böhringer 2002).

Other methods of detecting galaxy clusters such as the Sunyaev-Zel'dovich (SZ) effect (Sunyaev & Zel'dovich 1970) (see Carlstrom et al. (2002) for a review) also have inherent biases. Clusters detected through the SZ signal should have no redshift bias out to a redshift of $z \sim 2$. However, clusters with bright radio point sources (from

¹ The National Optical Astronomy Observatory is managed by the Association of Universities for Research in Astronomy under a Cooperative Agreement with the National Science Foundation.

galaxies with an active nucleus, AGN) make it difficult to detect an SZ signature (Lin & Mohr 2007; Martini et al. 2009; Lin et al. 2009). As such, surveys searching for galaxy clusters using the SZ effect may possibly exclude clusters with radio sources that are bright at high frequencies. Further, Martini et al. (2009) and Krick et al. (2009) find that the fraction of AGN in clusters is higher for clusters at high redshift suggesting AGN evolution in clusters similar to that of star-forming galaxies. Therefore, a higher fraction of high-redshift clusters, as compared to low-redshift, may be excluded from SZ surveys because they contain radio sources. Another limitation of cluster detection using the SZ effect is the size of the signal from the SZ effect of a galaxy cluster is small and directly related to the mass of the cluster. This implies that clusters detected through their SZ signal are biased towards finding the most massive clusters (Menanteau et al. 2010; Vanderlinde et al. 2010), similar to X-ray detected clusters.

A method of detecting clusters that involves a more targeted approach would be useful, especially if that method allows for the possible identification of high-redshift clusters. If we are able to efficiently select the most promising high redshift cluster candidates and examine these sources more closely, we can find a large number of high redshift galaxy clusters with cluster masses possibly more varied than clusters detected using optical/IR, X-ray, or SZ techniques. Having a wide range of redshifts can help to measure cosmological parameters such as Ω_X , ω_X and Ω_Λ (Allen et al. 2004).

Previous studies (Zhao et al. 1989; Hill & Lilly 1991; Allington-Smith et al. 1993; Dickinson 1997; Deltorn et al. 1997; Zirbel 1997; Blanton et al. 2000, 2001, 2003a; Belsole et al. 2007; Venturi et al. 2007) have show that radio sources are often found in galaxy clusters. In particular, bent, double-lobed sources are frequently associated with clusters. A likely explanation for the bending of the radio lobes is the relative motion between the host galaxy and the intracluster medium (ICM). There are several explanations for this relative motion. One scenario involves a galaxy with a high peculiar velocity relative to the cluster moving through the ICM. If the density of the ICM is high enough, and the velocity of the radio galaxy fast enough, it is possible to create enough ram pressure to bend the lobes of the radio source (Owen & Rudnick 1976; Eilek et al. 1984; Burns 1990; Ball et al. 1993; Bliton et al. 1998). In another scenario, the ICM is set in motion due to a recent cluster-cluster merger. The radio galaxy, with a small peculiar velocity relative to the surrounding cluster, and the moving ICM experience enough relative motion that the resulting ram pressure can produce the observed bending in the lobes (Burns 1990; Roettiger et al. 1996; Burns et al. 1996). Evidence supporting the second scenario is observed with the alignment of the bending of the lobes and the X-ray emission (Gómez et al. 1997). Bent radio sources may also be found in clusters that are relaxed on large scales, e.g. Abell 2029 (Clarke et al. 2004). In these cases, the bending of the lobes may be related to gas motions induced by “sloshing” (Ascasibar & Markevitch 2006) of the central cD. Using bent-lobed radio sources as tracers of clusters may lead to the discovery of a large number of previously undetected high redshift clusters,

without having to perform an extremely deep all-sky survey. This technique may preferentially select clusters undergoing mergers, and/or those that exhibit sloshing.

Double-lobed radio sources are generally divided into two different morphological classes. Fanaroff & Riley (1974) discovered a connection between the radio power and morphology of a given extended radio source. They found that weaker radio sources, those with powers less than $5 \times 10^{25} \text{ W Hz}^{-1}$ at 1440 MHz (assuming a power-law spectrum with $\alpha = 0.8$), typically have bright radio cores and lobes fading toward the edges. These have since become known as FR I sources. The more powerful radio sources ($P_{1440 \text{ MHz}} > 5 \times 10^{25} \text{ W Hz}^{-1}$) have dim or absent cores and edge-brightened lobes and are now referred to as FR II sources. More recently, Owen & White (1991) and Ledlow & Owen (1996) showed that the dividing line between FR I and FR II sources is related to both the radio power and the optical luminosity of the host galaxy.

Differences between FR I and II sources may be related to the power output from the central engine as well as the environment of the source. Zirbel (1997) found that the cluster environments surrounding FR I and FR II sources are different. They found that on average, FR I galaxies are located in richer groups than FR II galaxies. As redshift increased, the likelihood of an FR II galaxy existing in a rich group increased. They also found that high-redshift FR I and II galaxies belong to different subsets of galaxy groups than low-redshift FR I and II galaxies. These galaxy groups, selected based on the presence of a radio source and including both low- and high-redshift FR I and II sources, differ from optically selected galaxy groups.

Croft et al. (2007) looked for radio sources associated with sources detected using the maxBCG algorithm from Koester et al. (2007a). The maxBCG algorithm (as described in Koester et al. (2007b)) detects galaxy clusters by taking advantage of the spatial clustering, the tight sequence that most cluster galaxies are located on in a color-magnitude diagram (the “E/S0 ridgeline” or red sequence as described above), and the fact that there is often a brightest cluster galaxy (BCG) that is often coincident with the center of the cluster. Croft et al. (2007) found that $\sim 20\%$ of the time, the BCG is associated with a radio source at the same location. This percentage was dependent on the stellar mass of the host galaxy, rising as the mass of the host rises. Further, they detected that within a radius of 1.4 Mpc around the BCG, there is an over-abundance of radio sources compared to the field. This implies that galaxy clusters are likely to be hosts to radio sources. Also, there is an association between the presence of a cooling flow in a cluster and the central giant elliptical being radio loud. At least 70% of cooling flows host radio sources in their centers (Burns 1990; Mittal et al. 2009; Dunn et al. 2010), while fewer than $\sim 30\%$ of non-cooling flows have central radio sources.

We present our investigation into the cluster environments surrounding radio galaxies of different morphologies. Specifically, we examine the optical environments surrounding multi-component bent and straight radio sources of type FR I and FR II. We also compare these environments to the cluster environments around single-component radio sources. Throughout this paper we assume $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_\Lambda = 0.7$, and $\Omega_M = 0.3$.

In §2, we discuss how we select our radio sources from the VLA Faint Images of the Radio Sky at Twenty-cm (FIRST) survey for further examination, in §3, we discuss how we identify optical sources in the Sloan Digital Sky Survey (SDSS) catalog associated with our radio sources, and in §4, we measure the richness of the optical environments around the radio-selected sources. In §5, we examine the optical and radio properties of these sources, in §6, we discuss possible X-ray emission associated with our samples, and in §7, we present our conclusions and discuss our findings.

2. SELECTING RADIO SOURCES

Previous studies indicated that bent-double radio sources are associated with galaxy clusters (Blanton et al. 2000, 2001, 2003a; Smolčić et al. 2007; Kantharia et al. 2009; Giacintucci & Venturi 2009; Oklopčić et al. 2010). Identifying these sources in radio catalogs and then searching for optical counterparts can define a sample of radio-selected galaxy clusters. We made use of the FIRST catalog (Becker et al. 1995) to identify possible galaxy clusters based on radio emission. The FIRST survey covers $\sim 25\%$ of the sky and is mostly contained in the northern Galactic cap. The FIRST survey has a flux density threshold of 1 mJy, systematic astrometric errors $< 0.05''$ and total positional errors on the order of $\sim 1''$.

Possible galaxy clusters identified through this characteristic radio emission can then be used for studies of cosmology as well as galaxy and cluster formation and evolution. In this paper, we examine the optical environments around both FR I and FR II extended radio sources (bent and straight). We also study a sample of single-component radio sources for comparison.

2.1. The Visually-Selected Bent Sample

Visual inspection of a radio source is one way to determine if it is a true bent-double source. Blanton (2000) visually examined a sample of $\sim 32,000$ multiple-component sources from the April 1997 release of the FIRST catalog (covering $\sim 3000 \text{ deg}^2$ of the sky). The maximum separation between components was $60''$. A total of 384 sources were identified as bent, double-lobed sources. Many of these sources were studied previously in the optical in an effort to measure the richness of their environments (Blanton et al. 2000, 2001, 2003a). These sources each contain two or more components listed in the FIRST catalog.

2.2. The Automatically-Selected Bent Sample

In order to utilize the entire FIRST catalog (as of April 2003, covering $\sim 9000 \text{ deg}^2$ of the sky), we employed an automated program to identify the bent-double sources within the > 800000 sources in the catalog. Proctor (2006) created a pattern recognition program that used a random training set of 2823 sources from the ~ 16000 FIRST three-component sources to assign a score to each three-component source as to its bent-ness or straight-ness. The maximum separation between any two components was $57''.6$, similar, although not identical, to that for the visually-selected sources. Proctor (2006) visually inspected each of the training set sources and classified them as either bent, non-bent, or ambiguous. Of the

2823 training set sources, Proctor (2006) classified 147 as bent-double sources, 1395 as non-bent-double sources, and 1281 as ambiguous sources. Using these classifications, the program was able to search the entire FIRST catalog for three-component sources and identify bent and straight double-lobed radio sources.

Proctor (2006) gave each of the ~ 16000 three-component sources in the entire FIRST catalog a score that related to the probability that the source was a true bent-double source. For example, eight out of ten sources with a score of 0.80 are expected to be true bent-double sources. In order to limit the sample to only sources most likely to be true bent-double sources, we limited the auto-bent sample to only those sources with a score of 0.50 or higher. Sources with lower scores might also be true bent-double sources, but the number of such sources is overwhelmed by serendipitous sources that are not related. This limits the sample to 1546 sources. Using only the sources with the highest scores eliminates many of the "three-component" sources that only appear related due to projection effects. Proctor (2006) defined the central source for these automatically-selected bent sources as the source opposite the longest side when making a triangle of the three sources.

Since both the visual- and auto-bent samples are selecting for similar sources from different versions of the same catalog, we expect overlap between the two samples. Visual inspection of bent-lobed sources allows for the selection of sources that the automatic selection technique may classify as ambiguous. There are 167 sources (of 384) in the visual-bent sample that are three-component, double-lobed sources (the others have only two, or greater than three, components). Searching the entire ~ 16000 source auto-bent sample for these 167 double-lobed sources, we find that there are 24 sources located within $1''$ of the central location of sources in the visual-bent sample. An additional 126 sources from the entire ~ 16000 source auto-bent sample have central locations within $10''$ of the location of the corresponding visual-bent source. The other 17 double-lobed sources in the visual-bent sample are located within an area with a maximum separation of $24''$ from the corresponding source in the entire ~ 16000 source auto-bent sample. Thus, we recovered all 167 visually-selected three-component double-lobed sources in the entire ~ 16000 source auto-bent sample. The separation between the visual-bent and the automatically selected sample positions is likely due to the automatic selection of the center of the bent-lobed radio source being different than the center of the source as determined visually. When there was a known optical counterpart for a visually-selected bent-lobed radio source, the position of the optical source was used as the position of the center of the bent-lobed radio source. Not all of the visual-bent three-component double-lobed sources have scores high enough to be included in our auto-bent sample. Only 94 of the 167 sources identified in the visual-bent sample as three-component, double-lobed sources have bent probability scores higher than the 0.50 score that we set as a baseline. Figure 1 shows the probability scores of the visual-bent, three-component bent-lobed sources. The sources with scores below 0.50 were not included in the auto-bent sample. Therefore, the total overlap between the visual-bent and auto-bent samples is 94 sources.

2.3. The Straight Sample

We also examined a sample of 3232 sources from the FIRST catalog which represent all of the aligned (straight) three-component sources (with the distance between components limited to $57''.6$) in the entire FIRST survey region. We selected these sources using the same code from Proctor (2006). The straight-lobed sources are those sources identified by the code of Proctor (2006) as having $(d_{min} + d_{mid})/d_{max} < 1.01$ and $d_{min}/d_{mid} \geq 0.7$ where d_{min} is the minimum pair-wise distance between the three radio sources, d_{mid} is intermediate pair-wise distance, and d_{max} is maximum pair-wise distance. In practice, the dividing line between the auto-bent and straight samples is an opening angle of $\sim 160^\circ$. It is possible that the angle at which the observer views a source (classified as straight-lobed) is such that the lobes appear to be aligned even though the source is bent. In this case, sources that appear to be aligned and are included in the straight sample are actually bent-lobed sources. If bent-lobed radio sources are more often associated with galaxy clusters, then the inclusion of these apparently straight bent-lobed sources in the straight sample serves to increase the number of straight-lobed sources located in rich clusters.

2.4. The Single-Component Sample

If galaxy clusters are more likely to be associated with extended, multi-component radio sources, there should be a corresponding lack of galaxy clusters when looking at single-component radio sources. In order to compare extended sources to single-component sources, we randomly picked out 3356 sources in the FIRST catalog that had no other source within $60''$. The number of single-component sources in the FIRST catalog totaled 576,267, but we chose to work with a smaller sample size to better correspond with the sizes of the other samples.

One of the questions we wish to address with the single-component sample is how often are radio sources in general associated with cluster environments? If we find single-component radio sources are located in cluster environments with the same incidence as bent-double radio sources, there is no evidence to suggest that bent-double radio sources are any more likely to be tracers for galaxy clusters than any other radio source. This makes our sample of single-component radio sources a good baseline to compare typical radio sources to our samples of multi-component, extended radio sources.

2.5. Determining Accurate Radio Flux Densities

The FIRST B-array observations sometimes resolve out extended source emission. This can result in an underestimate of the total flux of the object. The NRAO VLA Sky Survey (NVSS; Condon et al. (1998)) surveyed the sky north of $\delta = -40^\circ$ at a lower resolution (the D- and DnC-array) than FIRST (the B-array) at the VLA. If a source is in both catalogs we can use the NVSS flux and compare it to the FIRST flux to determine if the source has extended emission that has been resolved out. Going by the convention set forth by Ivezić et al. (2002), we searched the NVSS within $15''$ of the location of each component of the FIRST source. If the location of the FIRST source is within $15''$ of the location of a source in the NVSS catalog, the probability is less

than 1% that the two sources are random associations (Ivezić et al. 2002).

The extended sources in our sample are often comprised of sources located more than $15''$ from each other, thus we searched for an NVSS counterpart around not only the central radio source but also the two lobes. There were cases where a single NVSS source corresponded to two or more FIRST components. In these instances, we assumed that the single NVSS source was an under-resolved version of the multiple-component FIRST source and thus singularly represented the multiple FIRST components. For these sources we used the higher of the NVSS flux or the sum of the flux of the FIRST components with which the NVSS source was associated.

3. FINDING OPTICAL COUNTERPARTS IN THE SDSS

The Sloan Digital Sky Survey (SDSS) (York et al. 2000) is a drift-scan survey of the northern Galactic cap. The SDSS cataloged photometry in five bands (*ugriz*) for over 350 million unique sources and spectra of over a million sources as of data release 7 (DR7, Abazajian et al. (2009)). DR7 contains photometric redshifts calculated for every extragalactic source in the SDSS catalog with a new hybrid technique that gives much more accurate results than previous data releases. DR7 also includes updated and more accurate magnitudes for all of the sources in the *photo* catalog that better accounts for sky background subtraction issues for crowded fields. The astrometry of the sources in DR7 was updated as well, yielding more accurate source positions.

The FIRST survey was designed to cover the same area of the sky as the SDSS. This makes it convenient to search the SDSS for optical counterparts for all of the FIRST sources from the samples we have described above. The positional accuracy of both SDSS and FIRST are less than $1''$ so we were able to search in a very small area around each radio source for an associated optical source. Because of the large number of sources in the SDSS catalog, it is necessary to identify sources which are likely to be chance-coincidences, instances when a physically unrelated optical source appears close in projection to a radio source. To achieve this, we searched the SDSS for all optical sources within $10''$ of the core of the multi-component radio sources as discussed below. We found that a radius of $10''$ allowed us to maximize the possibility of finding an optical counterpart while keeping the number of chance-coincidences to a minimum.

3.1. Correlating FIRST Sources With SDSS Sources

Following the procedure set forth by Moran et al. (1996), we matched the original central radio source positions with the SDSS catalog. We then shifted both the RA and Dec of every radio source in each of our samples by $30'$ and matched the two catalogs again. The optical sources matched with these random positions are not real radio/optical counterparts but instead give an idea as to the number of chance-coincidences to expect as a function of separation between the radio and optical positions. We compared the number of SDSS matches as a function of increasing distance from the center of the radio source to the number of SDSS matches that the shifted positions give as a function of increasing distance from the location of these positions. Looking at the

number of matched sources as a function of separation between the radio source and the optical source (keeping only the closest optical source to each radio source) should show a peak at small separations for real radio/optical counterparts. For the random sample, there is no peak at small separations but instead a steadily rising number of matches as the separation between the radio and optical source is increased. This rising number of matches is a result of the increased area that is being searched as separation is increased. We see in Figure 2 that the number of random matches closely follows the real matches starting at a separation of around $2''$. This is for the straight sample, but it is similar for all of the samples.

Figure 3 shows how increasing the allowed separation between the radio source and the optical source increases the number of chance-coincidences. We see that the total number of SDSS matches continues to increase upwards, but the number of good matches that are expected, those that are not chance-coincidences, does not increase as quickly. There are true, non-chance-coincidence, matches at larger separations. However, if we allow matches to come from larger separations, while recovering a higher fraction of the true radio/optical counterparts expected, we increase the number of chance-coincidences in our sample much more quickly than the number of true radio/optical counterparts.

We aimed to make our samples 95% reliable, meaning that we expect 5% of the sources to be serendipitous chance-coincidences. The dash-dotted line in Figure 3 shows how the percentage of reliable sources in our sample decreases as the separation is increased. We settled on 95% for a number of reasons. First, we want our sample to be as free as possible of chance-coincidences and we have achieved this by requiring a 95% reliability cut-off. We would also like our sample to be as complete as possible. That is, recovering a large percentage of the true radio/optical counterparts. We define the completeness of the sample as the fraction of radio/optical counterparts identified when limiting matches to only those contained within the radius set by our 95% reliability criteria compared to the total number of radio/optical matches within $10''$. Constraining our samples to 95% reliability maximizes the completeness of the samples while simultaneously limiting the number of chance-coincidences.

It is difficult to determine the center of a bent-lobed radio source automatically. We find that as a result of the possible ambiguity as to which of the three components of the doubled-lobed radio source is the central component, the maximum allowable separation between the optical source and the presumed center of the radio source for the visual-bent and auto-bent samples is larger than for the other samples. This is similar to results in McMahon et al. (2002), that for multiple component radio sources the separation between the center of an extended radio source and its optical counterpart is larger than for radio point sources. Limiting the auto-bent sample to a 95% reliability cut-off limits the sample completeness to below 60%. As a compromise, to increase the completeness of the auto-bent sample we have lowered the reliability cut-off to 90%. This brings the completeness of the auto-bent sample more in line with the other samples. We find that the samples were 95% reliable (or 90% for the auto-bent sample) out to radii

between $1''.9$ and $6''.8$ from the radio source, depending on the sample.

The results of these selection criteria are shown in Table 1. Column 1 of Table 1 identifies the name of each sample, column 2 lists the number of radio sources that each sample contains, column 3 lists the number of FIRST radio sources in each sample that are contained within the SDSS footprint, column 4 gives the total number of radio sources in each sample with a unique match within the SDSS database located $10''$ or less from the center of the radio source, column 5 gives the radius, in arcseconds, out to which an optical match in the SDSS database located within that distance from the center of the radio source is 95% likely to be coincident with the radio source and column 6 gives the number of sources remaining in each sample that have an optical counterpart in the SDSS within a radius corresponding to that 95% confidence. Column 7 gives the completeness of each sample (see §3.3), column 8 lists the number of radio/optical sources that meet our color criteria (see §3.3), column 9 gives the total number of sources in each sample with redshift $z \geq 0.01$ and a Schechter correction factor (see §4.3) less than 3, and columns 10 and 11 list the number of FR I and FR II sources in column 9 (see §3.4) in each sample, respectively.

3.2. Determining Redshift

A source in the SDSS can have up to four different redshift values associated with it, one measured spectroscopically and the others based on the color and shape of the spectrum of the source. In DR7, over 1.2 million sources have associated spectra and thus a spectroscopically measured redshift. If one of the radio/optical sources has a spectroscopically measured redshift in SDSS, we use that value as the redshift of the source for the rest of our calculations. Unfortunately, that still leaves a vast majority of the ~ 357 million sources in the SDSS without spectroscopically measured redshifts. For these sources, redshifts were inferred photometrically.

The SDSS **photoz2** table was generated by a neural network program which used a training set of known galaxy colors and redshifts to determine a more accurate photometric redshift (Oyaizu et al. 2008). The **photoz2** table provides photometric redshift estimates for ~ 77 million sources in DR7 which have been classified as galaxies and have a magnitude of $m_r < 22$. There are two different estimations of the photometric redshift contained within the **photoz2** table. The **photozcc2** photometric redshift is to be used for faint sources which have $m_r > 20$. The **photozd1** photometric redshift has a smaller error and is to be used for brighter sources with $m_r < 20$. Unfortunately, not all of the sources in the SDSS catalog have **photoz2** redshifts.

Nearly every extragalactic source in DR7 has a redshift in the **photoz** table. The photometric redshifts in the **photoz** table were obtained with use of the template fitting method (Budavári et al. 2000; Csabai et al. 2003). This method compares the expected colors of a given galaxy type with those observed for an individual galaxy. Template fitting involves taking a small number of spectral templates for discrete galaxy types and then choosing the best fit redshift by comparing the galaxy morphology, colors, and apparent magnitude and determining the redshift value that gives an

appropriate luminosity. This basic photometric redshift measurement is much improved in DR7 and gives results consistent with spectroscopically measured redshifts (Abazajian et al. 2009). Figure 4 shows the correlation between the spectroscopic and photometric redshifts for the different samples in the instances where there exists a spectroscopic redshift. Examination of Figure 4 shows that the photometric redshifts are very similar in most cases to the spectroscopic redshifts.

The spectroscopic redshifts are the most reliable, so if a matching optical source has an associated spectroscopic redshift, we use that value as the redshift of the source. If the source does not have a spectroscopic redshift, but does have an associated `photoz2` redshift, we used the specific `photoz2` redshift depending on the apparent magnitude of the source, as described above. The errors for the `photoz2` photometric redshifts are much smaller than the errors associated with the more simply calculated `photoz` photometric redshifts. In other cases, we used the redshift given by the `photoz` table as the redshift of the source. Figure 5 shows the distribution of redshifts for each of the different methods of calculating redshift for the straight sample. The **Best Redshift** line on the histogram refers to the single redshift given to each radio/optical source with the priority as described above. The other samples have similar distributions. Overall there are a small number of sources with spectroscopic redshifts, but all sources with redshifts above $z = 1.0$ have been obtained spectroscopically. The distribution of redshifts from the `photoz2` table are similar for both (`photozcc2` and `photozd1`) estimations. Redshifts obtained from the `photoz` table have a peak at lower redshifts, similar to the `spectroscopic` table and lower than that of the `photoz2` table.

Figure 6 shows the redshift distribution of each radio source sample using the best redshift available as described above. The visual-bent sample peaks at a lower redshift than the other samples, most likely a result of the visual selection of each source. Low redshift sources are easier to identify by eye as bent-double sources. The straight sample has a higher fraction of high redshift sources than the other samples.

3.3. Identifying Possible Clusters

We expect that optical hosts associated with radio galaxies in clusters detected to the limit of the SDSS will mostly be red elliptical galaxies. If we assume that the galaxies hosting the radio sources are ellipticals with similar colors, they will form a recognizable distribution on a plot of color versus redshift. Figure 7 shows the results of comparing a source's redshift with its $r - i$ color. Plotting redshift versus $r - i$ color allows us to differentiate between red elliptical galaxies and higher redshift blue quasars. We drew a line in Figure 7 to set a boundary between ellipticals and quasars. The sources below the line are likely associated with quasars and we excluded them from our samples to avoid attempting to search for galaxy clusters around quasars in the SDSS. Any galaxies potentially associated with a cluster around these high-redshift quasars would be too faint to be detected with the SDSS. These objects will be explored in more detail in a future paper. In this paper we are more interested in the cluster environments surrounding elliptical galaxies. We removed these blue sources from our

samples as our "color-cut", along with any sources that are without a detection in any of the five SDSS color bands. The removal of these sources accounts for less than 10% of the sample for all of the samples except the straight sample, where the removal of these high-redshift blue sources accounts for more than 20% of the sample. We see this as the difference between columns 6 and 8 in Table 1.

3.4. Determining Radio Power and FR Morphology

With the redshift of the optical source giving us the distance to the source, we were able to calculate an absolute magnitude and a radio power. Sources were dereddened using the maps of Schlegel et al. (1998) and k-corrected using code written specifically for use with SDSS sources (Blanton & Roweis 2007). With apparent magnitudes adjusted for reddening and k-corrected to a reference frame of $z = 0$, we calculated rest-frame absolute magnitudes and radio powers for each source.

Ledlow & Owen (1996) made a distinction between FR I and FR II sources using the radio power of the source as well as its absolute V-band magnitude, M_V . They found that while FR II sources generally are found to have powers greater than $P_{1440 \text{ MHz}} = 10^{25} \text{ W Hz}^{-1}$, there was a correlation between the power of the radio source, the V-band absolute magnitude of the optical source associated with the radio source, and the morphology of the radio source. The line drawn in Figure 8 replicates the distinction that they found between FR I and FR II sources and we classified our sources based on these criteria. We converted magnitudes from the SDSS g and r bands to the Johnson V band using the conversions in Smith et al. (2002), namely that $V = g - 0.55(g - r) - 0.03$.

Using this distinction between FR I and FR II sources, we compared the optical environments surrounding both types of sources. Thus, we were able to not only compare bent-double sources and straight sources to single-component sources, we also examined the differences between FR I and FR II sources within these samples. This allowed us to identify the type of radio sources most likely to be found in rich galaxy clusters. While the FR I/II criteria are usually only applied to extended sources, we applied them here to our single-component sample as well which contained a mix of extended and non-extended sources using the Ledlow & Owen (1996) division.

We also visually determined the FR I and FR II classifications of all radio sources in the bent and straight samples with an associated optical source that met our reliability criteria. We visually inspected the FIRST radio image and contour maps of each of these sources. For the sources that are clear FR I or FR II sources, we identified them as such. For the sources where the visual classification was less certain, we marked them as possible FR I or FR II sources. There were also several sources that fit neither the FR I or FR II criteria and we marked those sources as "other". The plots in Figure 9 are similar to Figure 8, except we use the FR I or FR II classification we determined visually for the visual-bent, auto-bent, and straight samples.

Similar to the results of Best (2009) and Lin et al. (2010), we found that while there may be a general trend for FR I sources to reside below the line proposed by Ledlow & Owen (1996), it is by no means an absolute separation. Specifically, we found that for the visual-

bent sample, 81% of the sources we visually identified as FR I sources are also FR I sources according to the criteria of Ledlow & Owen (1996). For the same visual-bent sample, only 40% of the sources we visually classified as FR II would also be FR II sources in the Ledlow & Owen (1996) scheme. For the auto-bent sample, 79% of FR I sources and 21% of the FR II sources that we visually-identified follow the Ledlow & Owen (1996) demarcation. Likewise, for the straight sample, 76% of the visually-identified FR I and 44% of the visually-identified FR II sources follow the Ledlow & Owen (1996) criteria. This is possibly the result of extended emission being resolved out leading to the mis-classification of some FR I sources as FR II sources. We are more likely to mis-classify an FR I source as an FR II source than the other way around.

Table 2 gives the numerical breakdown of visually classified FR I and FR II sources in the two samples. Columns 3 and 4 are the number of clearly identified FR I and FR II sources in each sample, respectively. Columns 5 and 6 list the number of ambiguous FR I and FR II sources, and column 7 gives the number of sources in each sample with a radio morphology that cannot be classified, even tentatively, as an FR I or FR II source. Columns 8 and 9 list the total number of FR I and II visually-classified sources, respectively, that remain after redshift and apparent magnitude selection (see §4.3 and §4.5). There were several sources in the automatically selected samples that appeared to be either two or three unrelated sources. This visual inspection allowed us to classify those sources as either questionable FR I/II (in the case where it appeared that there was an unrelated radio source near a double-lobed source) or as other (in the case where all three radio sources appeared to be unrelated to each other). This allows us to state with more certainty that the sources that are securely classified as FR I/II are in fact true three component radio sources, and not spurious chance-coincidences.

The radio sources located at high redshifts present problems for a definitive visual FR I/II classification. For these sources, the three components are typically located in very close proximity on the sky and thus difficult to determine if the lobes are edge-bright, etc. The resolution of the FIRST survey also limits accurate FR I/II determination, especially for the low surface-brightness sources. For the sources where this becomes an issue, it is up to the discretion of the examiner whether the source is classified as I or II and it can vary even after repeated viewings of the same source. Thus, visual classification is not necessarily a better solution than classifying using the Ledlow & Owen (1996) criteria. We show some typical FR I and FR II sources from the visual-bent and straight samples in Figure 10.

3.5. Source Extent

We determined the physical extent of the extended sources. We measured the angular distance from the center of each lobe to the central source and added these together. In addition, we included the semi-major axis of each lobe in the total extent of the source, so that our extents are effectively the distance from the edge of one lobe to the other, as if the source was straight. We converted these angular sizes to physical extents using the redshift of the source as determined by the optical

counterpart. These physical extents are affected by projection effects caused by the inclination of the source as a result of our viewing angle. Figure 11 compares the extent of the radio source with the redshift of the source. We plotted upper and lower limits for the angular extent of the sources. The center of each component of a source had to be within $60''$ of another component to be in the visual-bent sample and $57''.6$ for the auto-bent and straight samples, but the lobes can have extended emission, giving some sources total extents greater than the presumed $120''$ (for the visual-bent sample) or $115''.2$ (for the auto-bent and straight samples) maximum angular extent. An extent of $120''$ is shown as the solid line in Figure 11. The angular resolution of the FIRST survey is $5''$. In order for a source to be identified as a multi-component source, all of the sources (at least the central source and two lobes) need to be resolved independently. This implies that there is a minimum angular extent of $10''$ for all of the three-component sources in our sample. This is shown as the dashed line in Figure 11.

Previous authors argue that the physical extent of a radio source is analogous to the age of that source: the older a source is, the more time it has had to expand from the central engine. Thus the more extended sources are also the oldest sources. Best (2009) finds that for their sample, FR I sources are more extended, and thus older. We find, for all three of our samples, that the FR I sources are in fact the smaller sources. This can be seen in Figure 12 where we plotted the cumulative fraction of sources as a function of source extent. We see that, with the exception of the largest straight-lobed radio sources, FR II sources (short dashed line) are larger than FR I sources (solid line), both when determining FR I/II morphology based on the Ledlow & Owen (1996) criteria (the left-hand plot in Figure 12), and determining the morphology visually (right-hand plot). We determined the K-S test probability that the FR I and FR II populations from each sample were drawn from the same parent population. We found that when FR morphology was determined by the method of Ledlow & Owen (1996) the size distributions of the visual-bent sample had a K-S test probability of 0.0730%, the auto-bent sample had a probability of 60.0%, and the straight sample had a probability of 0.0631% that the FR I and II sources came from the same parent population. When the FR morphology was determined visually, we found that the K-S test probability was 16.5% for the visual-bent sample, 16.0% for the auto-bent sample, and $5.67 \times 10^{-10}\%$ for the straight sample that the FR I and II sources came from the same parent population. These low probability scores (with the exception of the Ledlow & Owen (1996) classified auto-bent sample) imply that FR I and FR II sources are drawn from different parent populations in terms of size distribution. This may be a result of FR II sources being generally more powerful than FR I sources. The more powerful FR II sources will be able to expand to larger extents before the expansion is halted by any intervening ICM.

Further examination of Figure 6 shows that while they are generally similar, our samples do not have identical redshift distributions. Most notably, the visual-bent sample peaks at a redshift of $z \sim 0.2 - 0.3$, lower than that of the other samples. We limited our samples to those sources with components separated by a

maximum of $\sim 60''$ from each other. Of course, this is an angular size and not a physical size, so nearby, physically extended sources are likely to have components separated by more than this maximum angular separation. Since the visual-bent sample is composed of lower-redshift sources in general, this sample may include a lower fraction of sources with large physical extents than the other samples. In order to examine a subset of sources that are free of this bias, we created two groups of subsamples based on Figure 11. We defined two boxes on this plot, one box that is smaller and is composed of lower-redshift, less physically extended radio sources, and one box of higher-redshift sources containing more extended radio sources. The sources in these boxes (which we refer to as the small box and the large box later in this paper) are free of bias regarding their angular extent as a function of redshift. Both boxes limit the physical size of the sources such that at a given redshift they would be included in our samples, regardless of their angular extent. Examining only the sources in these boxes should remove any effect of angular size of the radio source in the results when examining the physical sizes of these sources. We plotted the size distributions of the FR I and FR II sources within these two boxes in Figure 13 for our different samples. Table 3 lists the number of FR I and II sources (determined both by the Ledlow & Owen (1996) criteria and visually) in each sample contained within the boxes. Specifically, columns 2 and 3 list the number of FR I and II sources, respectively, determined using the criteria of Ledlow & Owen (1996), contained within the small box. Columns 4 and 5 list the number of FR I and II sources, respectively, determined visually, contained within the small box. Columns 6 and 7 list the number of FR I and II sources, respectively, (using Ledlow & Owen (1996) criteria), contained within the large box. Columns 8 and 9 list the number of FR I and II sources, respectively, determined visually, contained within the large box.

In general, we find the same result as previously when we limit the sample to sources within the boxes. As seen in Figure 13, the FR II sources are still mostly larger than the FR I sources. The most obvious exception is for sources in the visual-bent sample that have been classified as FR I or II visually (upper right panel of Figure 13). In this case, the FR I sources are found to be larger. Specifically, the K-S test probabilities are as follows. When determining FR morphology using the method of Ledlow & Owen (1996) for the sources contained within the small box (upper-left plot), we found that the visual-bent FR I and II sources had a 99.9% probability of coming from the same parent population, the auto-bent FR I and II sources had a probability of 56.5%, and the straight FR I and II sources had a probability of 2.61% of coming from the same parent population. When we examined these same sources located within the large box (lower-left plot), we found that the visual-bent sample had a K-S probability of 0.601%, the auto-bent sample had a probability of 85.5%, and the straight sample had a probability of 0.985%. When we determined the FR morphology visually for sources within the small box (upper-right plot), we found that the visual-bent sample had a K-S test probability of 0.223%, the auto-bent sample had a probability of 11.2%, and the straight sample had a probability of 49.7%. The same sources located

in the large box (lower-left plot) had K-S test probabilities of 37.7% for the visual-bent sample, 0.994% for the auto-bent sample, and 0.617% for the straight sample. Given the results for the other samples and classification methods, as well as the difficulty in classifying sources as FR I or II visually, we draw the general conclusion that FR I sources appear to be smaller in our samples.

4. DETERMINING CLUSTER RICHNESS

We examine the cluster properties of the radio sources in our samples. This includes measuring the number of galaxies around each radio source. This richness measurement will identify clusters as well as groups and even areas with less-than-average galaxy counts. Characterizing the richness in the optical environment around each radio source will allow us to infer the basic cluster properties of the different samples of radio sources.

4.1. Choosing A Richness Measurement System

We determine the richness of the environments using a method similar to Allington-Smith et al. (1993) and Zirbel (1997). In those papers, as well as Blanton et al. (2000, 2001), the richness measurement $N_{0.5}^{-19}$ corresponds to counting all galaxies within a 0.5 Mpc radius of the radio source with absolute magnitudes brighter than $M_V = -19$. This is an improved metric over that of Hill & Lilly (1991) which involved counting all galaxies within 0.5 Mpc of the radio source with apparent magnitudes in the range of m_{rg} to $m_{rg} + 3$, with m_{rg} being the magnitude of the radio source. The appealing aspect of using the $N_{0.5}^{-19}$ method is that it measures the same absolute magnitude range for all of the clusters, down to the magnitude limit of the observations. This allows for a more accurate measure of the cluster richness than through the use of apparent magnitudes alone. In the case where the radio galaxy is not the brightest galaxy in the cluster, using the apparent magnitude of the optical source associated with the radio source does not account for galaxies in the cluster that might be brighter than this. Counting all of the galaxies down to an absolute magnitude limit avoids this problem.

When Allington-Smith et al. (1993) chose 0.5 Mpc as a radius within which to search for cluster members, they were balancing search area with their smaller detector size. They acknowledged that they expected to find poor groups instead of rich clusters, so the 0.5 Mpc radius would be adequate for these means. However, for richer clusters this radius is too small, i.e. Abell (1958) used a radius of $1.5h^{-1}$ Mpc. We chose a radius of 1.0 Mpc as a compromise between the two. This is also a reasonable area in which to search for cluster members in the much deeper SDSS catalog. Our richness metric is thus $N_{1.0}^{-19}$, a count of all galaxies brighter than $M_r = -19$ within 1.0 Mpc of the radio source.

We have used the r-band in the SDSS. If we assume that a typical elliptical galaxy has a color of $V - R \approx 0.9$ and using the conversion between the standard Johnson bands and the SDSS bands provided in Smith et al. (2002), we find that $V \approx r + 0.8$. Thus by using the SDSS r-band, we searched, on average, 0.8 magnitudes fainter than Allington-Smith et al. (1993). By including galaxies nearly a full absolute magnitude fainter as well as searching out to a larger radius around the radio

source allows us a better measurement of the richness of the richer clusters.

4.2. Accounting for Background Counts

Because we are using the SDSS, we have the advantage of being able to estimate the background galaxy count locally around each cluster candidate. We are not limited by the size of the CCD as we would be if we were observing each of these fields individually. For the local background galaxy estimation we searched within an annulus with inner and outer radii of 2.7 and 3 Mpc, respectively, around the radio source for all optical sources brighter than $M_r = -19$. Most sources located this far from the radio source will be unassociated with the potential cluster. Of course, the area of this annulus is larger than the area in which we are searching for potential cluster galaxies. To account for this we normalized the number of galaxies found within the background annulus to match that of the inner 1.0 Mpc by multiplying by the ratio of the areas.

Then we subtracted the normalized background galaxy counts from the galaxy counts within the inner 1.0 Mpc to obtain a measurement for the overdensity of galaxies within 1.0 Mpc of the radio source. This overdensity allows us to approximate the richness of the potential cluster. Figures 14 and 15 show examples of bent-lobed and straight-lobed radio sources in both rich and poor environments. Other sources look similar to these typical sources. The sources included in Figures 14 and 15 are located at typical redshifts ($0.2 < z < 0.3$) for our different samples.

4.3. Schechter Correction

The limiting magnitude of SDSS in the r band is $m_r \sim 22$. For sources at high enough redshifts, the absolute magnitude chosen ($M_r = -19$) will be fainter than the limiting magnitude of the SDSS. These fields then need to be corrected to account for these unobserved sources. To do this, we employed a Schechter (1976) luminosity function with $M_r^* = -21.21$ and $\alpha = -1.05$ based on the findings of Blanton et al. (2003b) specific to SDSS galaxy observations. The luminosity function predicts the number of expected galaxies over a given magnitude range. We calculated a k-correction for each of the sources, as in Blanton & Roweis (2007). The k-correction, related to the color of the source, allows for a more accurate determination of the absolute magnitude over a given wavelength band in the source's rest-frame. Typically, the redshift at which the apparent magnitude of an $M_r = -19$ galaxy becomes fainter than the limiting magnitude of the SDSS is $z \sim 0.26$. The correction was defined as $f_c = \phi(M_r)/\phi(M_{r,lim})$ with M_r representing the faint end ($M_r = -19$) of the absolute magnitude range we wish to search in and $M_{r,lim}$ representing the absolute magnitude corresponding to the limiting magnitude of the SDSS at the redshift of the source. We multiply the correction factor, f_c , by the background-adjusted galaxy counts to give a limiting-magnitude corrected richness measurement.

We limited our sample to those sources whose redshifts and colors are such that the value of the applied Schechter correction is less than 3, to increase the reliability of our richness measurements. For example, a

hypothetical source with a Schechter correction factor of $f_c \approx 10$ and a measured over-density (richness) of 3 sources has a Schechter corrected richness of 30, placing it solidly into the rich group/poor cluster category. This may not necessarily correspond to a cluster but simply a source with a high Schechter correction factor. Limiting our sample to those with small correction factors ($f_c \leq 3$) allows us to more confidently determine if there truly is a galaxy cluster present. The redshift this correction factor corresponds to is typically $z \sim 0.50$.

4.4. Abell Cluster Comparison

As a comparison, we used Abell clusters located within the footprint of the SDSS and measured the richness of those clusters using our $N_{1.0}^{-19}$ metric. There are 819 Abell clusters located within the SDSS footprint with associated redshifts in the NASA/IPAC Extragalactic Database (NED) small enough as to not warrant a Schechter correction. Based on the redshift of each Abell cluster, we calculated the apparent magnitude of an $M_r = -19$ source at the redshift of each of the 819 clusters that matched our criteria, and searched within 1.0 Mpc of the center of the cluster for all sources brighter than this magnitude limit. The apparent magnitude was found using a k-correction from Sarazin et al. (1982) and Sandage (1973), assuming that $k(z) = 2.5 \log(1+z)$ and that $k(z) \approx z$ for sources where $z \leq 0.2$. We utilized this calculation for the k-correction because there is not necessarily a source located at the center of the cluster as defined by Abell et al. (1989). Without a source on which to base our k-correction we have applied this estimation. Almost all of the galaxy clusters are located at redshifts of $z < 0.2$ and thus have very small k-corrections. Figure 16 shows the relationship between the number of cluster members that Abell et al. (1989) identified and the cluster richness we have calculated using $N_{1.0}^{-19}$. The relationship between these two numbers is not very clear, similar to the findings of Wen et al. (2009) (their Figure 17), although a general trend is apparent (with a Spearman correlation coefficient of 0.423), albeit with significant scatter. Wen et al. (2009) argue that projection effects (especially for sources with $z \geq 0.1$) and an inconsistent magnitude range for each potential cluster (due to the use of apparent magnitudes by Abell et al. (1989) instead of absolute magnitudes) cause these inconsistencies between their cluster member counts and the cluster member counts from Abell et al. (1989).

4.5. Nearby Clusters

A problem presents itself for the lowest redshift sources. We have set a radius of 2.7-3.0 Mpc for determining the unrelated background sources for each potential cluster. For sources where the redshift is very low, the area of sky searched corresponding to the annulus from 2.7-3.0 Mpc away from the radio source becomes immense. Searching this area becomes infeasible at low enough redshifts as the number of sources in the SDSS in an area that large easily exceeds a few million. Thus we limit our sample to only sources with a redshift of $z \geq 0.01$. Sources below this limit are nearby and most likely well known, removing them from the samples means that we can not make generalizations about the most nearby galaxy clusters containing radio sources

but does not bias the results for sources whose redshift is greater than this lower limit. Between the four samples, there are a total of only 10 sources with redshifts lower than this value. Removing these sources, as well as sources with $f_c > 3$, is seen as the difference between columns 8 and 9 in Table 1.

4.6. Cluster Richness Results

Table 4 lists the results of the cluster richness measurements. Column 1 lists the sample name, and column 2 gives the fraction of each sample found in an environment with an over-density of 20 or more sources calculated as described above. An over-density of 20 sources likely corresponds to a poor cluster or a group of galaxies. For all of the columns, the number in parentheses corresponds to the total number of sources in that sample. Columns 3 and 4 give the fraction of FR I and FR II sources (with the FR classification determined by the power-magnitude method as in Ledlow & Owen (1996)) in each sample, respectively, located in environments with an over-density of 20 or more sources. Columns 5, 6, and 7 give the fraction of each sample, in the same order as before, located in an environment with an over-density of 40 or more sources. This corresponds to a richer cluster. The first line for each sample contains only those sources which have magnitudes and redshifts such that they do not need to be Schechter corrected. The second line for each sample also includes all sources whose Schechter correction is less than 3.

Table 5 gives the percentages of those sources *visually* classified as FR I/II located in environments of 20 or 40 or more galaxies, in the same manner as Table 4. It should be noted that although there is overlap between the visual-bent and auto-bent samples, after the cuts on the samples have been made (as described in §3.3, §4.3, and §4.5), there is an overlap of only 44 sources between the two samples (including objects with Schechter correction less than 3). This represents $\sim 16\%$ of the auto-bent sample and $\sim 27\%$ of the visual-bent sample, so differences in the richness distributions of these two samples are not surprising.

We see that, in general, multi-component sources are more often located in rich cluster environments than single-component sources. We also see that bent sources are more often located in galaxy clusters than straight sources. We see a general trend towards FR I sources being more often associated with rich clusters than FR II sources. This is true for FR class determined visually (Table 5) as well as by using the classification scheme proposed by Ledlow & Owen (1996) (Table 4). An exception is for visually classified sources in the auto-bent sample. Here, we find that FR II sources are in richer environments.

Figures 17 and 18 show the fraction of sources with varying richness for the different samples. Figure 17 shows the distribution for the FR I sources. The left panel shows the distribution of richness for the sources that have been classified as FR I through the classification scheme of Ledlow & Owen (1996). The right panel shows that same distribution, except for sources that have been visually classified as FR I sources. Figure 18 shows the distributions for the FR II sources. The left panel shows the distribution of cluster richnesses for sources that have been classified as FR II through

the Ledlow & Owen (1996) method, and the right panel shows those sources classified as FR II visually. These distributions are only for the subset of sources needing no Schechter correction (see §4.3). We examined the likelihood that the distribution of cluster richness for the different samples could come from the same parent population using the K-S test. We found that the probability for the visual-bent sample (with an average richness of 57 ± 7 sources) to come from the same parent population as the straight sample (with an average richness of 27 ± 6 sources) is $3.14 \times 10^{-10}\%$ and for the visual-bent sample compared to the single-component sample (with an average richness of 11 ± 6 sources) that probability is $1.50 \times 10^{-24}\%$. The probability between the auto-bent sample (with an average richness of 45 ± 7 sources) and the straight sample is $1.54 \times 10^{-3}\%$ and for the auto-bent sample compared to the single-component sample that probability is $2.46 \times 10^{-16}\%$. If we group both the visual- and auto-bent samples together and compare them to the straight sample, the likelihood that the distribution in cluster richness comes from the same parent population is $1.55 \times 10^{-9}\%$ and for the single-component sample compared to the bent samples, the likelihood is $1.22 \times 10^{-28}\%$. The likelihood of the distribution of cluster richness of FR I sources coming from the same parent population as FR II sources (using all four samples and the Ledlow & Owen (1996) criteria for determining FR type) is $1.22 \times 10^{-3}\%$. That likelihood rises to 1.47% when the FR type is determined visually. Therefore, the bent-double sources are more often located in cluster environments than the straight sources and the single-component sources. Further, FR I sources are more likely to be located in cluster environments than FR II sources, although when FR type is determined visually the distribution in cluster richness is more similar.

Table 6 lists sources from the visual-bent, auto-bent, and straight samples with $N_{1.0}^{-19}$ values of 40 or higher. This table is available in its entirety in machine-readable and Virtual Observatory (VO) forms in the online journal. A portion is shown here for guidance regarding its form and content. Column 1 lists the source name and column 2 lists the sample (V for visual-bent, A for auto-bent, and S for straight) that the source belongs to. Columns 3 and 4 are the RA and Dec of the source in J2000 coordinates. Column 5 is the SDSS de-reddened r -band magnitude of the associated optical source and column 6 is the r -band absolute magnitude. Column 7 lists the total 1440 MHz flux of the radio source in mJy. Column 8 gives the opening angle of the radio source. The total power of the radio source, in W Hz^{-1} , is given in column 9. The FR types, determined using the criteria from Ledlow & Owen (1996) and visually, are in columns 10 and 11, respectively. Column 12 lists the redshift of the source. The $N_{1.0}^{-19}$ value is given in column 13 along with the Schechter correction factor, f_c , in column 14. Finally, column 15 lists the Abell cluster (if there is one) located within 3 Mpc (projected) of the radio source. Note that some radio sources appear twice, if they appear in both the visual-bent and auto-bent samples. In these fifteen overlap cases we see that the opening angle is often different between the two samples. This is due to the different methods for determining the center of the radio source. For the visual-bent sample, the source

center was defined as the location of the corresponding optical source if there was one, and the location of the radio core if an optical counterpart was lacking (Blanton 2000). This is different than the auto-bent sample where the source center was always defined as the location of the radio component opposite the longest side when making a triangle of the three radio sources (Proctor 2006). These differences in the central position account for the differences in opening angle measurement between the visual-bent and auto-bent samples.

An intriguing question remains for the sources with low $N_{1.0}^{-19}$ measurements (i.e. $N_{1.0}^{-19} < 5$). Sources falling into this category in the visual- and auto-bent samples require some type of explanation as to how the radio lobes were bent. If they are not in a cluster (at least as optically identified) what could be responsible for the observed bending of the lobes? One possible explanation is that these radio sources reside in fossil groups (Ponman et al. 1994; Jones et al. 2000). Fossil groups are thought to be compact galaxy groups within which the member galaxies have merged into one, or few, galaxies near the center-of-mass of the cluster. These fossil groups can be detected, via their ICM, in the X-ray. D’Onghia et al. (2005) found that in their simulations $\sim 33\%$ of groups actually exist as fossil groups. Observationally, Vikhlinin et al. (1999) and Jones et al. (2003) have found that percentage to be between 10%-20%. Further X-ray observations of the sources in our samples with low $N_{1.0}^{-19}$, specifically in the visual- and auto-bent samples, could help to shed light on whether these sources are in fossil groups.

5. PHYSICAL PROPERTIES OF RADIO SELECTED GALAXY CLUSTERS

We have assembled a large collection of radio-selected potential galaxy clusters with known properties such as optical colors, redshift, richness, radio source extent, radio power, bending angle of the radio source and radio morphology. In Figure 19, we plot the radio source size distribution for the different samples, separating the sources located in rich clusters ($N_{1.0}^{-19} \geq 40$, short dashed line) from those in poor clusters ($N_{1.0}^{-19} < 40$, solid line). Only sources contained within the small box in Figure 11 and that have colors and redshifts such that they need no Schechter correction (see §4.3) are included in the plot. This includes 13, 23 and 53 sources with $N_{1.0}^{-19} < 40$ and 25, 21 and 22 sources with $N_{1.0}^{-19} \geq 40$ in the visual-bent, auto-bent and straight samples, respectively.

We see no obvious difference in radio source extent for sources located in clusters versus those not in clusters. We performed a K-S test on the size distributions of sources in clusters versus those not in clusters and found that the FR I and II sources (determined using the Ledlow & Owen (1996) criteria) in the visual-bent sample had a 96.2% probability of coming from the same parent population, those in the auto-bent sample had a 85.1% probability of coming from the same parent population, and those in the straight sample had a 72.0% probability of coming from the same parent population. This confirms what a visual inspection of Figure 19 implies, there is no difference in physical extent for sources in clusters versus those not in clusters. Plotting radio source extent against $N_{1.0}^{-19}$ (Figure 20) further helps to

illustrate this. We see no obvious trend of radio source extent as a function of the $N_{1.0}^{-19}$ value.

Previous authors (i.e. Allington-Smith et al. (1993); Zirbel (1997)) found that in general, nearby FR II sources are more often located in poor environments, while at higher redshifts, they tend to be found in richer environments. Figure 21 shows the relationship between the redshift and the cluster richness for the FR I (left-panel) and FR II (right-panel) sources in our samples. Our samples seem to show a similar trend between the richness of the cluster and the redshift of the cluster for both FR I and FR II sources. Examining the Spearman correlation between the redshift and $N_{1.0}^{-19}$ for FR I sources (from Ledlow & Owen (1996)) there is a slight positive correlation of 0.21, implying that there is a trend between the richness and redshift of a cluster containing an FR I source. This correlation drops to 0.049 for FR II sources (again classified as in Ledlow & Owen (1996)), implying very little to no correlation between the richness and redshift of a cluster containing an FR II source. If we ignore the FR type we find a positive correlation of 0.15. Therefore, searching around radio sources, we find richer environments at higher redshifts (see Figure 22). The fractions are highest for bent-lobed sources, as seen in Tables 4 and 5. This could follow from the results of Martini et al. (2009). If clusters contain a higher number of AGN at higher redshifts ($z \sim 1$) then we might expect to find richer environments around AGN when searching at high-redshift as compared to low-redshift.

It has been observed previously (Burns 1990; Blanton et al. 2000, 2001; Mao et al. 2009, 2010) that wide-angle-tail (WAT) sources tend to be located in rich cluster environments. Burns (1990) found evidence that the bent-lobed nature of WATs is a result of a recent cluster-cluster or cluster-subcluster merger. WATs typically have powers near the classic FR I/II break ($P_{1440 \text{ MHz}} \sim 10^{25} \text{ W Hz}^{-1}$). Figure 23 shows that the richest clusters have radio sources that fall near this break. The left-hand panel of Figure 23 shows only the sources contained within the small box in Figure 11 that need no Schechter correction (see §4.3) and the right-hand panel shows all sources, including ones not contained within the small box, that need no Schechter correction. Table 7 gives the breakdown of the number of sources with richnesses above and below $N_{1.0}^{-19} = 100$ and the percentage of those sources that have radio powers between $24.75 < \log P_{1440 \text{ MHz}} < 25.75$, a typical radio power range where WATs are found. We see that a higher fraction of clusters with $N_{1.0}^{-19} > 100$ have radio sources with powers typical of WATs than less rich clusters.

We also examined the relationship between the opening angle of the radio source and the richness of the cluster environment. There was no obvious correlation between the two as might be expected since the angles are affected by viewing angle, ICM density, and galaxy velocity. Blanton (2000) found similar results, seeing no correlation between the opening angle and the cluster richness.

6. CORRELATION WITH X-RAY CATALOGS

X-ray observations can confirm a source’s association with a galaxy cluster. In addition, X-ray observations can provide information about the temperature and the

mass of the galaxy cluster. We searched the *ROSAT* All-Sky Survey (RASS) for possible X-ray counterparts for the sources in our samples. We used the RASS Faint Source Catalog (RASS-FSC), whose selection criteria included any source in the 0.1-2.4 keV energy band that had a detection likelihood of at least 7 and contained at least 6 source photons. In the *ROSAT* All-Sky Survey catalogs, the detection likelihood is defined as $-\ln(P)$, where P is the probability that the observed distribution of photons originates from a spurious background fluctuation (Voges et al. 1999).

We examined the rate at which each sample had sources with X-ray counterparts, and whether this was related to the radio source being found in an optical cluster. We searched within a radius of 1.0 Mpc for any possible X-ray sources in the RASS-FSC associated with all radio sources with an optical counterpart and also more specifically for those radio sources found in a cluster environment with a richness measurement of $N_{1.0}^{-19} \geq 40$. Given the flux limits, sources at high redshift are unlikely to be detected in the RASS-FSC. To eliminate some of the effects of the flux limit of the RASS-FSC, we have limited our samples to only sources with redshifts less than $z = 0.25$ or $z = 0.15$ as sources at these redshifts are more likely to be detected by the RASS-FSC. The results of this search are listed in Table 8. Column 2 gives the fraction of radio sources in each sample with optical counterparts and not in rich optical clusters in the SDSS and a corresponding X-ray source in the RASS-FSC. Columns 3 and 4 give the same fraction, but for sources with redshifts less than $z = 0.25$ and $z = 0.15$, respectively. Column 5 gives the fraction of radio sources in each sample located in optical clusters with $N_{1.0}^{-19} \geq 40$ with a corresponding X-ray source in the RASS-FSC. Columns 6 and 7 give the same fraction, but for sources with redshifts less than $z = 0.25$ and $z = 0.15$, respectively.

Examination of Table 8 shows that for all of the radio samples, objects associated with optically-detected clusters are more likely to have an X-ray counterpart within a projected distance of 1.0 Mpc than all sources located in less-dense optical environments. When we limit these to only sources with redshifts $z \leq 0.25$ we find that there is a higher percentage of sources with X-ray counterparts (both those not located in optically-detected clusters as well as those within optical clusters), and this fraction is even higher when we limit the sample to sources with $z \leq 0.15$ (with the exception of the single-component sample). This is expected given the flux limits of the RASS-FSC. Lower redshift clusters will be more frequently detected. In addition, we will detect a larger number of spurious sources at lower redshifts, since our 1.0 Mpc search region will correspond to a larger angular size on the sky. Visual-bent sources are more often associated with RASS-FSC X-ray sources than the other samples. Additionally, multiple-component sources in general are more likely to have an associated RASS-FSC X-ray source than single-component sources. Figure 24 shows the distribution of redshifts for the optically identified radio sources in our samples that have associated X-ray emission.

For the sources at the lowest redshifts, using a radius of 1.0 Mpc within which to search for X-ray counterparts in-

creases the number of chance-coincidences. We repeated the process of matching X-ray sources to the positions of our radio sources using a fixed maximum angular separation of $5'$. The results of this correlation are found in Table 9. The columns are identical to Table 8. In general, there are fewer radio sources with RASS-FSC X-ray counterparts located within $5'$ than within 1.0 Mpc. Still, we find that low redshift sources in optical clusters are most likely to have X-ray counterparts.

7. SUMMARY AND CONCLUSIONS

We created four samples of radio sources from the FIRST source catalog based on visual and automatic selection of multi-component, double-lobed, radio sources as well as single-component radio sources. We find that more than 50% of these radio sources have unique optical counterparts in the SDSS. We limited the maximum angular separation between radio and optical source positions such that 95% of the radio/optical sources in each sample (with the exception of the auto-bent sample at 90%) are true radio/optical sources and not chance-coincidences as compared to a random distribution of points on the sky. We created these samples to examine the cluster environments surrounding radio sources, specifically to examine if bent-lobed radio sources are more likely to be associated with galaxy clusters than other types of radio sources.

Using the SDSS DR7, we searched for optical counterparts around each radio source. Based on the optical properties in the SDSS for each of the radio/optical sources, we were able to calculate a redshift, absolute magnitudes in all of the SDSS wavelength bands, radio power at 1440 MHz, and the physical extents of the radio sources. We limited our samples of radio sources with optical counterparts to only those sources that were not too faint, too blue, or too nearby in order to remove sources that we could not properly examine using the SDSS. We measured the richness of the source environments using $N_{1.0}^{-19}$, the number of galaxies within 1 Mpc of the radio source with an absolute r-magnitude brighter than $M_r = -19$, corrected for background counts.

We find that, in general, multi-component radio sources are more often associated with galaxy clusters than single-component sources, and bent sources are more often in clusters than straight sources. The visually-selected, bent sources are most often found to be associated with clusters, followed by (in order) the auto-selected bent sources, the straight sources, and the single-component sources. In general, we find that FR I sources are found in richer environments than FR II sources, and this is true whether the FR I/II classification is done by visual inspection or by using radio power and optical magnitude criteria. The difference in environments between FR I and II sources, however, is less clear for some of the samples when this classification is done visually. Limiting to only those sources not requiring a Schechter correction (our most secure richness measurements) visually-selected, bent-lobed sources are found in clusters or groups 78% of the time, and in rich clusters 62% of the time. These values are 59% and 41% for the auto-bent sample, 43% and 24% for the straight sample, and 29% and 10% for the single-component sample.

We examined the radio source extents for all of the

samples. In general, we find that the FR II sources are larger than the FR I sources, whether this distinction is made visually or using radio power and optical magnitude criteria. We do not find an obvious correlation between the richness of the radio source environment and the extent of the radio source. This implies that there is no preference for radio sources in clusters to have a different characteristic size than radio sources not located in clusters in our samples.

We find that we are selecting richer environments with increasing redshift for all of our samples, for both FR I and II sources up to $z \approx 0.5$. This may be related to clusters having a higher fraction of radio-loud AGN at high redshift as compared to nearby. When examining the richest clusters in our samples, we find that a large fraction of them host radio sources near the FR I/II break, consistent with them being WAT sources.

We searched for X-ray counterparts around sources in our samples, examining separately objects with optical hosts only and those within clusters. A number of those sources located in rich cluster environments also have X-ray emission associated with them. As we restrict the sources to only those at low redshift, we find an even higher fraction with associated X-ray detections, as expected due to the flux limits of the RASS. We will further examine the X-ray properties of these sources in a future paper.

Since bent, double-lobed radio sources are frequently associated with rich clusters, we can use them as tracers for clusters at high redshifts. Given the sensitivity of the FIRST survey, we can detect bent, double-lobed radio galaxies out to $z \approx 2$. The visual-bent sample has 83 sources that are undetected in the SDSS to its magnitude limit ($m_r \sim 22$). Given the cluster association rate at low redshifts, we expect 51 of these sources to be associated with rich clusters at high ($z > 0.7$) redshifts. Using the larger, auto-bent sample, we expect to find 322 rich clusters at $z > 0.7$ (with small overlap between the two samples). We are currently in the process of following up on these sources using deep optical and near-infrared imaging. This cluster-finding technique is complementary to other high-redshift cluster surveys and may select clusters with a wider range of masses than other searches. It may preferentially select clusters that are merging or still in the process of forming. In addition, it gives us the opportunity to examine AGN feedback at high redshift.

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Table 1
Samples

Sample Name (1)	Total (2)	Footprint (3)	Unique (4)	Radius (5)	95% (6)	Complete (7)	First Cut (8)	Second Cut (9)	FR I (10)	FR II (11)
Visual-Bent	384	355	291	6''8	272	97.7%	236	166	143	23
Auto-Bent	1546	1384	910	4''2	599 ^a	83.6%	519	272	219	53
Straight	3232	2929	1806	3''2	1288	95.0%	840	449	322	127
Single-Component	3348	3003	1374	1''9	782	87.3%	680	358	335	23

Note. — Col. (1): name of the sample; col. (2): total number of radio sources; col. (3): number of radio sources within the SDSS footprint; col. (4): number of radio sources with a unique optical counterpart in the SDSS catalog within 10''; col. (5): the maximum angular separation between a radio source and an optical source corresponding to our 95% confidence criteria, as described in §3.1; col. (6): number of radio/optical counterparts with separations less than the maximum angular separation; col. (7): percentage of radio/optical counterparts with a separation less than the maximum angular separation; col. (8): the number of sources remaining after color selection, as described in §3.3; col. (9): the number of sources remaining after redshift and apparent magnitude selection, as described in §4.3 and §4.5; col. (10): number of sources classified as FR I based on the criteria of Ledlow & Owen (1996) after making the first and second cuts; col. (11): number of sources classified as FR II based on the criteria of Ledlow & Owen (1996) after making the first and second cuts.

^a The Auto-bent sample has a confidence rate of 90%.

Table 2
Results of Visual FR I/II Classification

Sample (1)	Total (2)	FR I (3)	FR II (4)	FR I? (5)	FR II? (6)	Other (7)	FR I ¹ (8)	FR II ² (9)
Visual-Bent	272	200	48	15	8	1	134	22
Auto-Bent	599	369	137	49	22	22	178	56
Straight	1288	659	498	63	36	32	272	138

¹ The number of visually-classified FR I sources remaining after redshift and apparent magnitude selection, as described in §4.3 and §4.5.

² The number of visually-classified FR II sources remaining after redshift and apparent magnitude selection, as described in §4.3 and §4.5.

Table 3
Sources Contained in Boxes (Figure 11)

Sample (1)	Small Box				Large Box			
	FR I ¹ (2)	FR II ¹ (3)	FR I ² (4)	FR II ² (5)	FR I ¹ (6)	FR II ¹ (7)	FR I ² (8)	FR II ² (9)
Visual-Bent	96	24	88	21	19	19	25	9
Auto-Bent	200	51	164	56	112	42	106	26
Straight	261	107	224	110	115	101	125	77

¹ FR type determined using the Ledlow & Owen (1996) criteria.

² FR type determined visually.

Table 4
Cluster Richness, $N_{1.0}^{-19}$

Sample (1)	$N_{1.0}^{-19} \geq 20$			$N_{1.0}^{-19} \geq 40$		
	FR I&II (2)	FR I (3)	FR II (4)	FR I&II (5)	FR I (6)	FR II (7)
Visual-Bent ^a	78%(98)	76%(85)	85%(13)	62%(98)	65%(85)	46%(13)
Visual-Bent ^b	78%(166)	80%(143)	70%(23)	63%(166)	65%(143)	48%(23)
Auto-Bent ^a	59%(120)	67%(97)	26%(23)	41%(120)	47%(97)	13%(23)
Auto-Bent ^b	66%(272)	73%(219)	38%(53)	50%(272)	56%(219)	25%(53)
Straight ^a	43%(217)	49%(164)	23%(53)	24%(217)	28%(164)	9%(53)
Straight ^b	52%(449)	58%(322)	39%(127)	32%(449)	37%(322)	21%(127)
Single-Component ^a	29%(209)	29%(202)	14%(7)	10%(209)	10%(202)	0%(7)
Single-Component ^b	35%(358)	36%(335)	22%(23)	15%(358)	15%(335)	13%(23)

Note. — The numbers in parentheses correspond to the number of sources in each sample and sub-sample from which the percentages are calculated.

^a Only sources needing no Schechter correction

^b Schechter corrected sources included

Table 5
Cluster Richness, $N_{1.0}^{-19}$ with visual FR classifications

Sample (1)	$N_{1.0}^{-19} \geq 20$		$N_{1.0}^{-19} \geq 40$	
	(FR I) (2)	(FR II) (3)	(FR I) (4)	(FR II) (5)
Visual-Bent ^a	80%(83)	64%(11)	63%(83)	55%(11)
Visual-Bent ^b	79%(134)	73%(22)	63%(134)	59%(22)
Auto-Bent ^a	59%(82)	77%(22)	39%(82)	59%(22)
Auto-Bent ^b	66%(178)	70%(56)	48%(178)	59%(56)
Straight ^a	45%(141)	38%(61)	26%(141)	20%(61)
Straight ^b	53%(272)	50%(138)	32%(272)	31%(138)

Note. — The numbers in parentheses correspond to the number of sources in each sample and sub-sample from which the percentages are calculated.

^a Only sources needing no Schechter correction

^b Schechter corrected sources included

Table 6
All Extended sources with $N_{1.0}^{-19} \geq 40$

Source Name	Smpl ¹	α	δ	m_r	M_r	S	Angle	$P_{1440 \text{ MHz}}$	FR ²	FR ³	z	$N_{1.0}^{-19}$	f_c	Abel
(1)	(2)	(3)	(4)	(mag) (5)	(mag) (6)	(mJy) (7)	(deg) (8)	(W Hz ⁻¹) (9)	(10)	(11)	(12)	(13)	(14)	(15)
J002859.3+002000	S	00:28:59.38	+00:20:00.6	17.12	-23.40	19.8	169.5	2.77e+24	I	I	0.222 ^a	61	1.00	...
J005625.7-011543	V	00:56:25.70	-01:15:43.0	13.36	-24.48	515.3	85.0	7.60e+24	I	I	0.078 ^b	52	1.00	A011
J005702.0-005230	A	00:57:02.07	-00:52:30.7	13.41	-23.11	72.5	147.2	3.29e+23	I	I	0.044 ^a	53	1.00	A011
J005702.1-005231	V	00:57:02.10	-00:52:31.0	13.41	-23.11	72.5	147.0	3.29e+23	I	I	0.044 ^a	53	1.00	A011
J010242.5-005032	V	01:02:42.50	-00:50:32.0	17.46	-23.54	66.5	87.0	1.33e+25	I	I	0.261 ^b	64	1.00	...
J010456.5+000423	V	01:04:56.50	+00:04:23.0	18.26	-23.26	83.4	8.0	2.50e+25	I	I	0.312 ^b	206	1.37	...
J011403.1-011058	V	01:14:03.10	-01:10:58.0	16.90	-23.15	16.5	139.0	1.59e+24	I	I	0.187 ^a	55	1.00	...
J011403.1-011057	A	01:14:03.15	-01:10:58.0	16.90	-23.15	16.5	138.9	1.59e+24	I	I	0.187 ^a	55	1.00	...
J011633.3-092753	S	01:16:33.38	-09:27:53.3	18.17	-22.74	22.1	179.2	4.13e+24	I	I	0.253 ^b	47	1.00	...
J013503.8+011325	S	01:35:03.81	+01:13:25.3	18.90	-23.08	20.7	175.9	8.56e+24	I	I	0.359 ^b	122	1.91	...
J022736.7-005253	V	02:27:36.70	-00:52:53.0	20.26	-19.24	69.7	85.0	4.84e+24	II	II?	0.161 ^b	49	1.00	...
J023027.9+010847	A	02:30:27.96	+01:08:47.2	17.45	-23.65	130.9	87.8	2.77e+25	I	I	0.267 ^a	103	1.05	...
J023028.1+010850	V	02:30:28.10	+01:08:50.0	17.45	-23.65	130.9	88.0	2.77e+25	I	I	0.267 ^a	108	1.05	...
J030259.5-001136	V	03:02:59.50	-00:11:36.0	17.29	-22.38	63.8	97.0	4.23e+24	I	I	0.158 ^a	49	1.00	...
J072244.7+302842	S	07:22:44.71	+30:28:42.4	19.38	-22.90	15.8	176.5	7.44e+24	I	I	0.380 ^b	106	2.47	...
J072248.4+412921	A	07:22:48.43	+41:29:21.2	15.60	-22.78	31.7	146.2	7.37e+23	I	I	0.097 ^b	42	1.00	...
J072830.4+264240	V	07:28:30.40	+26:42:40.0	16.05	-23.59	93.2	153.0	6.38e+24	I	I	0.160 ^b	75	1.00	A058
J072955.9+414227	A	07:29:55.92	+41:42:27.5	16.79	-23.16	116.7	96.5	1.07e+25	I	I	0.183 ^b	82	1.00	...
J073420.2+434304	S	07:34:20.28	+43:43:04.4	20.62	-21.77	37.4	170.8	2.00e+25	II	II?	0.402 ^b	105	2.76	...
J074546.0+323530	A	07:45:46.09	+32:35:30.3	17.34	-23.29	42.6	74.5	6.34e+24	I	I	0.228 ^b	61	1.00	...
J075107.8+184724	A	07:51:07.85	+18:47:24.3	16.93	-23.73	12.0	144.9	1.87e+24	I	I?	0.233 ^a	46	1.00	...
J075128.4+245205	A	07:51:28.44	+24:52:05.0	18.21	-24.05	22.0	140.0	1.07e+25	I	II	0.386 ^a	121	2.43	...
J075128.5+245201	V	07:51:28.50	+24:52:01.0	18.21	-24.05	22.0	140.0	1.07e+25	I	II	0.386 ^a	127	2.43	...
J075145.1+310811	S	07:51:45.17	+31:08:11.3	18.36	-23.96	23.4	170.2	1.22e+25	I	I	0.398 ^a	50	2.58	...
J075457.8+210129	S	07:54:57.89	+21:01:29.1	17.84	-23.41	21.7	172.9	5.33e+24	I	I	0.286 ^b	52	1.15	...
J075718.7+345905	S	07:57:18.71	+34:59:05.8	17.66	-23.30	8.2	175.6	1.61e+24	I	I	0.259 ^a	62	1.00	...
J075814.0+111657	A	07:58:14.02	+11:16:57.8	18.33	-23.03	45.8	147.8	1.19e+25	I	I	0.293 ^a	117	1.23	...
J075850.3+471409	S	07:58:50.33	+47:14:10.0	18.36	-23.73	25.6	178.8	9.56e+24	I	I	0.344 ^b	46	2.08	...
J075917.1+270916	V	07:59:17.10	+27:09:16.0	15.14	-23.58	484.7	163.0	1.53e+25	I	I	0.112 ^b	98	1.00	A061
J080104.7+395637	V	08:01:04.70	+39:56:37.0	18.90	-23.04	7.0	145.0	2.68e+24	I	I?	0.348 ^b	73	1.84	...
J080641.5+451316	A	08:06:41.55	+45:13:16.7	17.75	-23.04	21.4	136.8	3.69e+24	I	I	0.244 ^a	77	1.00	...
J080822.4+390059	V	08:08:22.40	+39:00:59.0	17.54	-22.63	84.5	136.0	8.94e+24	I	I	0.196 ^a	47	1.00	...
J081243.7+250246	S	08:12:43.75	+25:02:46.6	17.39	-23.37	55.7	178.5	9.35e+24	I	I	0.241 ^a	44	1.00	...
J081245.9+574750	A	08:12:45.98	+57:47:50.7	17.51	-23.60	49.6	153.6	1.09e+25	I	II?	0.272 ^a	43	1.06	...
J081343.7+525736	S	08:13:43.76	+52:57:36.1	16.03	-23.26	212.6	176.8	1.05e+25	I	II	0.138 ^a	47	1.00	...
J081445.9+261551	A	08:14:45.98	+26:15:51.6	17.84	-23.36	27.3	135.9	6.51e+24	I	I	0.282 ^b	92	1.12	...
J081446.0+261548	V	08:14:46.00	+26:15:48.0	17.82	-23.39	27.3	136.0	6.40e+24	I	I	0.280 ^a	93	1.12	...
J081457.6+383310	V	08:14:57.60	+38:33:10.0	17.14	-23.22	20.4	163.0	2.55e+24	I	I	0.211 ^b	114	1.00	...
J081544.1+371016	V	08:15:44.10	+37:10:16.0	16.74	-23.16	124.7	81.0	1.04e+25	I	I	0.175 ^a	89	1.00	...
J081601.8+380415	S	08:16:01.87	+38:04:15.1	16.27	-23.56	427.5	167.7	3.44e+25	I	I	0.173 ^a	44	1.00	...
J081652.7+413333	V	08:16:52.70	+41:33:33.0	19.41	-22.70	13.9	90.0	6.37e+24	I	I	0.375 ^a	88	2.14	...
J081810.6+233211	V	08:18:10.60	+23:32:11.0	17.74	-23.08	51.8	24.0	8.97e+24	I	I	0.244 ^a	49	1.00	...
J082459.9+042549	A	08:24:59.92	+04:25:49.9	16.73	-23.68	54.5	98.0	6.71e+24	I	I	0.210 ^b	265	1.00	A066
J082712.7+382001	V	08:27:12.70	+38:20:01.0	17.58	-23.73	133.9	119.0	3.37e+25	I	I	0.289 ^b	137	1.19	A066
J082712.7+382000	A	08:27:12.75	+38:20:00.4	17.58	-23.73	133.9	119.4	3.37e+25	I	I	0.289 ^b	138	1.19	A066
J082759.9+514926	S	08:28:00.00	+51:49:26.9	18.10	-23.88	21.9	166.0	9.01e+24	I	II	0.359 ^a	62	1.90	...
J082835.2+322824	V	08:28:35.20	+32:28:24.0	17.47	-23.71	47.0	148.0	1.10e+25	I	I	0.280 ^a	102	1.11	A067
J083231.2+351713	S	08:32:31.24	+35:17:13.3	17.11	-23.95	86.2	165.8	1.85e+25	I	I	0.269 ^a	107	1.03	...
J083341.1+382614	V	08:33:41.10	+38:26:14.0	19.05	-23.17	15.1	106.0	7.06e+24	I	I?	0.379 ^b	180	2.34	...
J083413.1+452807	A	08:34:13.10	+45:28:07.1	19.11	-23.21	14.1	134.9	6.56e+24	I	I	0.378 ^b	134	2.57	...
J083715.1+092529	S	08:37:15.13	+09:25:29.9	18.07	-23.72	25.2	168.1	8.99e+24	I	I	0.337 ^b	78	1.65	...
J083842.1+444821	A	08:38:42.14	+44:48:21.5	18.96	-22.45	16.3	76.2	4.63e+24	I	I	0.304 ^b	62	1.27	...
J083913.9+060944	A	08:39:13.91	+06:09:44.9	18.24	-24.14	23.1	115.9	1.23e+25	I	I	0.401 ^b	113	2.73	...
J084153.8+472448	S	08:41:53.81	+47:24:48.1	18.45	-23.63	33.9	169.9	1.55e+25	I	I	0.375 ^a	112	2.09	...
J084228.1+112400	S	08:42:28.17	+11:24:01.0	18.53	-23.09	20.4	179.5	6.36e+24	I	II	0.317 ^a	59	1.46	...
J084455.6+482655	S	08:44:55.65	+48:26:55.2	19.36	-22.78	16.3	166.8	7.74e+24	I	I	0.382 ^b	51	2.20	...
J084525.5+522915	S	08:45:25.53	+52:29:15.8	18.85	-23.55	20.1	177.1	1.08e+25	I	II?	0.403 ^a	70	2.78	...
J084559.4+223109	V	08:45:59.40	+22:31:09.0	18.58	-23.54	25.8	102.0	1.16e+25	I	I	0.373 ^a	65	2.15	...
J084729.4+361025	S	08:47:29.48	+36:10:25.5	18.40	-23.68	32.2	172.1	1.55e+25	I	I	0.384 ^a	95	2.09	...
J084803.3+580947	S	08:48:03.39	+58:09:47.8	16.05	-24.51	58.7	165.1	8.18e+24	I	II	0.222 ^a	67	1.00	...
J085415.1+062919	S	08:54:15.20	+06:29:19.3	17.41	-24.36	37.4	175.2	1.27e+25	I	I	0.329 ^a	95	1.62	...
J085543.2+260200	A	08:55:43.27	+26:02:00.8	18.03	-22.65	24.6	157.2	3.89e+24	I	II	0.235 ^b	61	1.00	...
J085720.8+163103	S	08:57:20.84	+16:31:03.7	18.77	-22.97	22.6	179.0	8.05e+24	I	I	0.337 ^b	65	1.59	...
J085912.5+031405	A	08:59:12.58	+03:14:05.8	17.15	-22.94	24.7	75.5	2.43e+24	I	I	0.189 ^a	49	1.00	...
J090003.6+073056	S	09:00:03.66	+07:30:56.5	18.21	-24.00	41.2	171.9	1.99e+25	I	I	0.384 ^a	70	2.33	...
J090141.7+012105	S	09:01:41.73	+01:21:05.5	21.27	-19.77	37.7	167.0	9.78e+24	II	I	0.293 ^b	69	1.02	...
J090230.2+350510	V	09:02:30.20	+35:05:10.0	20.23	-22.00	13.5	56.0	5.95e+24	II	I	0.370 ^a	114	2.37	...
J090414.0-002144	S	09:04:14.09	-00:21:44.7	18.72	-22.51	42.3	172.3	1.39e+25	II	II	0.325 ^b	93	1.14	...
J090859.7+343104	V	09:08:59.70	+34:31:04.0	17.78	-23.14	15.8	105.0	2.99e+24	I	I	0.254 ^a	55	1.00	...

Table 6 — *Continued*

Source Name	Smp1 ¹	α	δ	m_r	M_r	S	Angle	$P_{1440 \text{ MHz}}$	FR ²	FR ³	z	$N_{1.0}^{-19}$	f_c	Abel
(1)	(2)	(3)	(4)	(mag) (5)	(mag) (6)	(mJy) (7)	(deg) (8)	(W Hz ⁻¹) (9)	(10)	(11)	(12)	(13)	(14)	(15)
J090859.7+343104	A	09:08:59.75	+34:31:04.0	17.78	-23.14	15.8	105.4	2.99e+24	I	I	0.254 ^a	55	1.00	...
J091007.4+183504	A	09:10:07.46	+18:35:04.9	17.71	-22.88	55.6	104.6	8.21e+24	I	I	0.228 ^b	80	1.00	...
J091023.7+352415	A	09:10:23.77	+35:24:15.1	18.20	-23.88	15.6	147.0	6.95e+24	I	II?	0.371 ^b	114	2.08	A075 ^a
J091344.5+474216	A	09:13:44.54	+47:42:16.4	14.81	-22.06	16.4	158.2	1.02e+23	I	I?	0.051 ^a	44	1.00	A075 ^a
J091419.9+120015	A	09:14:19.99	+12:00:15.5	18.77	-23.59	33.8	156.5	1.81e+25	I	II	0.402 ^a	120	2.69	...
J091745.7+275101	S	09:17:45.78	+27:51:01.8	18.35	-23.55	32.4	173.8	1.26e+25	I	I	0.350 ^b	157	1.78	...
J091823.0+333939	A	09:18:23.08	+33:39:39.9	18.66	-23.43	12.9	105.4	5.75e+24	I	???	0.371 ^b	100	2.09	...
J091950.6+355045	V	09:19:50.60	+35:50:45.0	16.59	-23.98	203.2	44.0	2.83e+25	I	I	0.222 ^a	103	1.00	...
J092041.6+065958	A	09:20:41.67	+06:59:58.2	18.40	-24.02	13.7	87.7	7.50e+24	I	I?	0.406 ^a	85	2.83	...
J092137.8-005857	A	09:21:37.82	-00:58:57.2	18.03	-23.45	35.1	137.7	1.03e+25	I	II	0.309 ^b	62	1.33	...
J092802.7+010926	S	09:28:02.79	+01:09:26.4	19.99	-22.43	14.1	172.4	7.49e+24	I	II	0.401 ^b	82	2.84	...
J093406.1+242041	A	09:34:06.18	+24:20:41.8	18.79	-22.69	27.3	79.3	8.00e+24	I	I	0.309 ^b	135	1.33	...
J093506.2+415631	S	09:35:06.27	+41:56:31.3	17.00	-23.22	12.3	172.9	1.50e+24	I	I?	0.198 ^a	50	1.00	...
J093524.9+235503	V	09:35:24.90	+23:55:03.0	18.04	-23.16	163.1	36.0	3.74e+25	II	I	0.277 ^b	77	1.11	A082 ^a
J093540.6+510203	S	09:35:40.66	+51:02:03.8	17.55	-23.27	26.8	170.3	4.78e+24	I	I	0.248 ^a	72	1.00	...
J093723.7-021514	S	09:37:23.76	-02:15:14.5	18.55	-23.30	52.2	179.6	1.99e+25	I	II?	0.347 ^b	49	1.72	...
J093926.6+404402	V	09:39:26.60	+40:44:02.0	18.11	-22.57	17.1	125.0	2.70e+24	I	I	0.234 ^b	97	1.00	...
J094307.3+250130	A	09:43:07.33	+25:01:30.4	18.41	-23.12	15.1	153.0	4.40e+24	I	II	0.308 ^a	70	1.37	...
J094601.0+292550	S	09:46:01.01	+29:25:50.1	17.66	-22.70	17.2	174.3	2.14e+24	I	II	0.211 ^a	60	1.00	...
J094649.9+093025	S	09:46:49.94	+09:30:25.4	16.41	-23.22	62.4	176.0	4.33e+24	I	I	0.161 ^a	64	1.00	A087 ^a
J094655.4+302323	V	09:46:55.40	+30:23:23.0	18.72	-22.88	36.2	156.0	1.06e+25	I	II	0.309 ^b	63	1.44	...
J094709.8+094504	S	09:47:09.85	+09:45:04.0	17.41	-22.62	20.5	175.1	1.89e+24	I	I	0.184 ^a	59	1.00	A087 ^a
J095004.6+291727	V	09:50:04.60	+29:17:27.0	17.86	-23.02	44.1	119.0	8.07e+24	I	II	0.251 ^a	86	1.00	A087 ^a
J095004.7+291723	A	09:50:04.75	+29:17:23.8	17.86	-23.02	44.1	118.8	8.07e+24	I	II	0.251 ^a	87	1.00	A087 ^a
J095534.7+162845	S	09:55:34.73	+16:28:45.6	18.11	-22.79	34.2	165.3	6.00e+24	I	I	0.246 ^b	64	1.00	...
J095755.9+155721	A	09:57:55.93	+15:57:21.9	18.51	-22.42	28.5	103.4	5.55e+24	I	I	0.258 ^b	68	1.00	...
J095810.8+155010	S	09:58:10.84	+15:50:10.9	17.74	-22.92	15.4	177.5	2.43e+24	I	I	0.235 ^b	41	1.00	...
J095927.5+300547	A	09:59:27.53	+30:05:47.7	18.42	-23.24	20.2	148.1	6.78e+24	I	I	0.328 ^a	55	1.50	...
J095937.0+082921	A	09:59:37.07	+08:29:21.4	19.48	-22.95	90.2	114.1	5.22e+25	II	I?	0.416 ^b	101	2.86	...
J100052.0+063948	S	10:00:52.06	+06:39:48.1	18.29	-22.79	14.5	164.4	3.11e+24	I	I	0.269 ^b	62	1.05	...
J100141.3+043528	S	10:01:41.36	+04:35:28.8	17.41	-22.95	23.9	167.3	2.88e+24	I	I	0.208 ^a	50	1.00	...
J100446.8+140508	S	10:04:46.82	+14:05:08.8	17.51	-24.46	76.8	170.8	2.55e+25	I	???	0.326 ^a	141	1.89	...
J100736.1+060207	S	10:07:36.17	+06:02:07.8	18.34	-23.30	8.0	169.9	2.61e+24	I	I	0.324 ^a	67	1.47	...
J100837.1+534707	S	10:08:37.18	+53:47:07.6	18.78	-23.15	30.9	178.6	1.15e+25	I	I	0.343 ^b	54	1.84	...
J100900.1+132254	S	10:09:00.10	+13:22:54.4	17.41	-23.06	24.6	163.9	3.47e+24	I	I	0.223 ^a	45	1.00	...
J100948.1+002903	S	10:09:48.18	+00:29:03.3	17.70	-22.34	35.8	163.8	3.38e+24	I	II	0.186 ^a	46	1.00	...
J101108.7+150231	S	10:11:08.77	+15:02:31.2	19.31	-23.03	26.9	171.3	1.39e+25	I	II	0.396 ^b	77	2.61	...
J101122.0+213853	S	10:11:22.08	+21:38:53.4	19.31	-22.77	28.1	164.4	1.27e+25	I	II?	0.374 ^b	88	2.07	...
J101344.1+493119	S	10:13:44.19	+49:31:19.1	18.85	-23.24	2.2	178.0	9.75e+23	I	???	0.370 ^b	63	2.10	...
J101602.4+240007	V	10:16:02.40	+24:00:07.0	17.72	-23.80	31.3	105.0	9.19e+24	I	I	0.309 ^a	46	1.36	...
J101740.9+080415	S	10:17:40.95	+08:04:15.2	16.30	-23.69	49.1	175.5	4.44e+24	I	I	0.182 ^a	74	1.00	...
J101924.9+121832	A	10:19:24.94	+12:18:32.6	18.36	-22.63	11.5	116.9	2.30e+24	I	I	0.261 ^b	58	1.00	...
J102032.0+310730	V	10:20:32.00	+31:07:30.0	17.68	-23.92	31.1	117.0	9.60e+24	I	II	0.316 ^a	44	1.44	...
J102032.1+310731	A	10:20:32.15	+31:07:31.1	17.68	-23.92	31.1	116.8	9.60e+24	I	II	0.316 ^a	44	1.44	...
J102308.2+070628	A	10:23:08.20	+07:06:28.9	17.84	-23.45	17.8	146.7	4.53e+24	I	II?	0.290 ^a	118	1.18	...
J102336.1+371516	S	10:23:36.16	+37:15:16.9	15.93	-23.03	49.0	179.9	1.92e+24	I	II	0.124 ^b	74	1.00	A099 ^a
J102337.2+324625	A	10:23:37.23	+32:46:25.6	17.81	-23.64	22.5	155.7	6.40e+24	I	I	0.305 ^a	49	1.31	...
J102524.5+424850	A	10:25:24.55	+42:48:50.8	18.63	-22.84	18.2	150.1	5.33e+24	I	I	0.309 ^b	65	1.32	...
J102731.7+072246	A	10:27:31.75	+07:22:46.3	18.54	-23.18	49.1	139.3	1.71e+25	I	I	0.333 ^b	48	1.56	...
J102757.8+103345	S	10:27:57.86	+10:33:45.9	16.05	-22.48	123.8	171.5	3.25e+24	I	II	0.102 ^b	103	1.00	A102 ^a
J102819.4-022652	S	10:28:19.41	-02:26:52.5	18.22	-23.57	16.6	164.3	6.02e+24	I	I	0.339 ^b	49	1.64	...
J102909.2+152553	A	10:29:09.23	+15:25:53.5	17.99	-23.49	80.9	145.3	2.37e+25	I	II	0.309 ^a	72	1.33	...
J102944.9+252311	V	10:29:44.90	+25:23:11.0	17.21	-23.48	236.0	50.0	3.81e+25	I	I	0.237 ^a	86	1.00	...
J103129.9+184235	S	10:31:29.98	+18:42:35.9	18.16	-22.33	12.1	178.5	1.67e+24	I	I	0.221 ^b	75	1.00	A103 ^a
J103201.6+350253	V	10:32:01.60	+35:02:53.0	17.29	-21.66	45.1	84.0	1.68e+24	I	I	0.121 ^a	110	1.00	A103 ^a
J103215.8+315236	V	10:32:15.80	+31:52:36.0	18.18	-23.54	71.0	85.0	2.48e+25	I	II	0.334 ^a	122	1.57	A103 ^a
J103258.8+304538	V	10:32:58.80	+30:45:38.0	18.77	-23.40	24.8	122.0	1.13e+25	I	I	0.375 ^b	130	2.24	...
J103449.4+182318	A	10:34:49.41	+18:23:18.9	17.26	-22.73	32.7	73.0	3.04e+24	I	II	0.184 ^a	44	1.00	...
J103452.6+042445	A	10:34:52.68	+04:24:45.4	18.35	-21.56	10.7	67.6	9.26e+23	I	I	0.179 ^b	75	1.00	A104 ^a
J103527.6+304240	A	10:35:27.69	+30:42:40.5	18.97	-23.32	16.7	116.4	8.28e+24	I	I?	0.389 ^b	115	2.50	A104 ^a
J103846.4+041450	A	10:38:46.48	+04:14:50.8	18.20	-23.23	21.0	137.2	5.78e+24	I	II	0.301 ^b	47	1.29	...
J104308.2+211425	A	10:43:08.23	+21:14:25.3	19.32	-22.85	28.9	123.7	1.37e+25	I	I	0.381 ^b	57	2.24	...
J104416.2+524055	A	10:44:16.25	+52:40:55.5	17.25	-22.81	58.6	143.2	5.60e+24	I	II	0.187 ^a	44	1.00	...
J104516.2+235140	V	10:45:16.20	+23:51:40.0	17.24	-23.39	33.0	103.0	5.01e+24	I	I	0.230 ^b	70	1.00	...
J105010.9+303955	V	10:50:10.90	+30:39:55.0	17.98	-22.98	145.4	127.0	2.91e+25	II	II	0.261 ^b	136	1.00	...
J105100.1+062615	A	10:51:00.17	+06:26:15.6	20.21	-21.62	24.1	132.8	1.08e+25	II	I	0.372 ^b	92	1.69	...
J105147.4+552309	S	10:51:47.46	+55:23:09.4	14.59	-23.13	187.5	178.7	2.47e+24	I	I	0.074 ^a	62	1.00	A111 ^a
J105550.8+543450	A	10:55:50.88	+54:34:50.5	19.65	-22.74	29.6	81.0	1.72e+25	II	I	0.416 ^b	250	2.76	...
J105720.3+301229	A	10:57:20.40	+30:12:29.4	17.07	-23.77	85.0	157.0	1.48e+25	I	I	0.245 ^a	55	1.00	...

Table 6 — *Continued*

Source Name	Smp1 ¹	α	δ	m_r (mag)	M_r (mag)	S (mJy)	Angle (deg)	$P_{1440\text{ MHz}}$ (W Hz ⁻¹)	FR ²	FR ³	z	N _{1.0} ⁻¹⁹	f_c	Abel
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)	(15)
J105754.3+422920	A	10:57:54.34	+42:29:20.3	18.35	-23.28	13.5	144.0	4.43e+24	I	II	0.325 ^a	49	1.46	...
J105759.6+083646	A	10:57:59.64	+08:36:46.3	21.39	-19.73	44.4	128.1	1.49e+25	II	I	0.328 ^b	49	1.07	A1130
J105937.7+395452	V	10:59:37.70	+39:54:52.0	17.63	-23.95	132.1	43.0	4.02e+25	I	I	0.314 ^b	52	1.41	...
J110249.7+404337	V	11:02:49.70	+40:43:37.0	18.50	-23.28	15.1	112.0	5.43e+24	I	II	0.338 ^a	54	1.63	...
J110456.9+002959	A	11:04:56.95	+00:30:00.0	18.37	-23.37	21.3	134.2	7.51e+24	I	I?	0.335 ^b	66	1.58	...
J110519.5+582350	A	11:05:19.55	+58:23:50.1	19.37	-22.98	23.9	68.7	1.29e+25	I	???	0.404 ^b	151	2.64	...
J110649.6+135510	S	11:06:49.69	+13:55:10.2	16.75	-23.10	558.5	179.5	4.67e+25	II	I	0.176 ^b	68	1.00	...
J110708.9+281211	S	11:07:08.92	+28:12:11.4	18.68	-22.97	17.4	165.9	5.63e+24	I	I	0.323 ^b	91	1.49	...
J110812.3+261035	V	11:08:12.30	+26:10:35.0	16.57	-23.47	115.0	128.0	1.09e+25	I	I	0.186 ^b	76	1.00	...
J110822.9+291427	S	11:08:22.98	+29:14:27.1	16.02	-24.38	117.1	167.1	1.49e+25	I	I	0.213 ^a	61	1.00	...
J110901.9+380841	A	11:09:01.99	+38:08:41.4	18.96	-23.33	19.1	144.0	8.52e+24	I	II	0.371 ^b	93	2.51	...
J110907.7+001231	S	11:09:07.72	+00:12:31.5	17.19	-23.79	18.4	167.5	3.65e+24	I	I	0.260 ^b	76	1.00	...
J110956.6+325207	V	11:09:56.60	+32:52:07.0	17.56	-22.61	42.0	33.0	4.23e+24	I	I	0.191 ^b	76	1.00	...
J111613.5+444653	A	11:16:13.53	+44:46:53.8	17.78	-22.86	35.1	137.2	5.50e+24	I	I	0.234 ^b	48	1.00	...
J111653.9+353655	A	11:16:53.90	+35:36:55.4	18.98	-22.92	10.7	107.6	4.19e+24	I	I	0.351 ^b	73	1.80	...
J111746.0-010944	S	11:17:46.09	-01:09:44.4	18.47	-22.98	10.0	169.5	2.86e+24	I	I	0.306 ^b	56	1.31	...
J111833.6+311511	V	11:18:33.60	+31:15:11.0	17.42	-23.09	320.7	95.0	4.38e+25	II	I	0.220 ^a	123	1.00	...
J112038.5+291234	V	11:20:38.50	+29:12:34.0	17.03	-23.75	83.0	126.0	1.38e+25	I	I	0.240 ^a	63	1.00	...
J112206.9+380927	S	11:22:06.92	+38:09:27.3	18.42	-23.50	21.9	164.8	8.61e+24	I	I	0.352 ^a	51	1.81	...
J112523.7+361824	V	11:25:23.70	+36:18:24.0	17.42	-23.83	42.2	120.0	1.03e+25	I	I	0.285 ^a	53	1.15	...
J112523.8+361821	A	11:25:23.82	+36:18:21.7	17.42	-23.83	42.2	120.2	1.03e+25	I	I	0.285 ^a	56	1.15	...
J112559.8+252837	V	11:25:59.80	+25:28:37.0	16.01	-22.81	46.0	85.0	1.57e+24	I	I	0.116 ^a	53	1.00	A125
J112649.4+162445	A	11:26:49.44	+16:24:45.3	17.92	-23.42	32.2	132.6	8.81e+24	I	I	0.300 ^a	60	1.22	...
J112723.9+000759	A	11:27:23.95	+00:07:59.3	16.93	-22.40	12.4	105.7	6.53e+23	I	I	0.142 ^b	64	1.00	...
J112802.2+240249	S	11:28:02.22	+24:02:49.8	18.58	-23.60	21.6	178.1	1.04e+25	I	II	0.384 ^a	68	2.26	...
J112839.9+433837	S	11:28:39.94	+43:38:37.4	16.27	-23.28	39.4	176.5	2.50e+24	I	I?	0.155 ^a	42	1.00	...
J113026.7+124648	S	11:30:26.75	+12:46:48.7	17.74	-23.16	14.4	175.8	2.71e+24	I	I	0.254 ^a	49	1.00	A127
J113048.8+252435	V	11:30:48.80	+25:24:35.0	16.23	-23.15	90.3	74.0	4.95e+24	I	II	0.145 ^a	60	1.00	...
J113157.0+390801	V	11:31:57.00	+39:08:01.0	17.71	-22.93	21.5	65.0	3.34e+24	I	II	0.233 ^a	96	1.00	A129
J113157.0+390800	A	11:31:57.01	+39:08:00.6	17.71	-22.93	21.5	83.9	3.34e+24	I	II	0.233 ^a	96	1.00	A129
J113225.9+234514	S	11:32:25.98	+23:45:14.0	19.26	-20.86	89.0	169.9	7.99e+24	II	I	0.182 ^b	63	1.00	...
J113523.0-011521	A	11:35:23.08	-01:15:21.8	18.11	-23.73	24.6	82.1	9.06e+24	I	I	0.342 ^b	47	1.71	...
J113546.8+234135	A	11:35:46.89	+23:41:35.5	16.88	-22.16	6.0	147.0	2.61e+23	I	I	0.130 ^a	51	1.00	...
J113735.0+065629	S	11:37:35.04	+06:56:29.4	17.55	-23.99	35.8	174.5	1.07e+25	I	II	0.312 ^a	52	1.39	...
J113902.6+322821	S	11:39:02.60	+32:28:21.6	16.39	-22.95	29.1	173.9	1.51e+24	I	I	0.141 ^a	70	1.00	A133
J113911.3+173434	S	11:39:11.31	+17:34:34.8	17.87	-23.72	22.6	169.5	7.06e+24	I	I	0.318 ^a	57	1.43	...
J113954.9+131128	S	11:39:54.92	+13:11:28.4	19.53	-22.63	36.9	177.7	1.60e+25	II	II	0.367 ^b	46	2.22	...
J114044.4+274931	S	11:40:44.44	+27:49:31.3	20.35	-21.72	89.6	178.3	6.36e+25	II	II	0.455 ^b	46	2.06	...
J114403.8+440021	S	11:44:03.89	+44:00:21.5	17.23	-24.15	49.9	167.2	1.36e+25	I	II	0.299 ^a	98	1.24	...
J114558.7+592309	A	11:45:58.78	+59:23:09.7	19.17	-22.16	13.2	130.5	3.47e+24	I	I	0.295 ^b	44	1.21	...
J114612.5+331133	S	11:46:12.59	+33:11:33.2	18.73	-23.35	14.4	167.8	6.17e+24	I	???	0.365 ^a	85	2.07	...
J114639.9+224135	V	11:46:39.90	+22:41:35.0	17.45	-22.46	40.7	69.0	3.46e+24	I	I	0.177 ^a	74	1.00	...
J114833.1+233226	V	11:48:33.10	+23:32:26.0	16.97	-22.92	34.0	124.0	2.86e+24	I	I	0.176 ^a	64	1.00	...
J114953.1+550101	S	11:49:53.14	+55:01:01.2	18.04	-23.50	27.2	177.9	8.17e+24	I	I	0.312 ^a	47	1.38	...
J115058.3+553747	A	11:50:58.34	+55:37:47.4	17.83	-22.60	43.0	120.3	5.63e+24	I	I	0.215 ^b	74	1.00	...
J115416.3+100939	A	11:54:16.36	+10:09:39.9	17.80	-22.57	47.5	150.9	5.92e+24	I	II	0.211 ^b	96	1.00	...
J115638.5+204849	A	11:56:38.59	+20:48:49.8	16.21	-23.23	17.5	124.2	9.84e+23	I	I	0.146 ^a	54	1.00	...
J115911.7+450341	S	11:59:11.74	+45:03:41.7	18.46	-23.02	19.3	176.8	5.77e+24	I	I	0.312 ^b	50	1.33	...
J120013.9+561502	A	12:00:13.91	+56:15:02.0	14.92	-22.36	20.6	137.0	1.85e+23	I	II	0.061 ^b	85	1.00	A143
J120210.3+274109	S	12:02:10.38	+27:41:09.0	15.91	-23.27	32.7	175.5	1.51e+24	I	I	0.134 ^a	52	1.00	...
J120359.8+012610	S	12:03:59.90	+01:26:10.8	19.30	-23.11	27.4	169.5	1.51e+25	I	I	0.408 ^b	257	2.81	...
J120535.1+113849	S	12:05:35.18	+11:38:49.4	17.42	-23.15	14.7	173.4	2.12e+24	I	I	0.225 ^a	65	1.00	...
J120845.4+174635	S	12:08:45.47	+17:46:35.8	18.68	-22.90	15.6	175.9	4.96e+24	I	I	0.320 ^b	41	1.42	...
J120905.0+562310	S	12:09:05.02	+56:23:10.1	18.65	-22.92	46.3	173.6	1.52e+25	I	I	0.325 ^b	126	1.41	...
J120938.4+242038	V	12:09:38.40	+24:20:38.0	17.91	-22.97	34.4	83.0	6.37e+24	I	I	0.252 ^b	76	1.00	...
J121038.3+000110	S	12:10:38.34	+00:01:10.7	19.05	-23.10	24.5	179.9	1.03e+25	I	I	0.362 ^b	47	2.22	...
J121045.0+214824	A	12:10:45.07	+21:48:24.7	19.89	-22.42	54.5	155.9	2.92e+25	II	II	0.402 ^b	61	2.55	...
J121111.0+060743	A	12:11:11.02	+06:07:43.5	16.11	-23.16	56.2	120.2	2.81e+24	I	I	0.139 ^a	41	1.00	...
J121730.5+002357	A	12:17:30.54	+00:23:57.7	19.01	-22.82	32.8	155.6	1.28e+25	I	II	0.350 ^b	182	1.70	...
J122135.5+473249	S	12:21:35.51	+47:32:49.6	17.85	-23.52	35.4	179.1	9.57e+24	I	I	0.298 ^a	73	1.24	...
J122208.0+341056	S	12:22:08.04	+34:10:56.8	17.45	-23.34	43.3	164.7	7.13e+24	I	I	0.239 ^a	44	1.00	...
J122436.6+351824	A	12:24:36.66	+35:18:24.5	18.50	-23.77	16.6	79.8	7.35e+24	I	I	0.370 ^a	157	2.45	...
J123549.4+214630	S	12:35:49.49	+21:46:30.6	18.11	-22.75	14.8	169.3	2.66e+24	I	I	0.249 ^b	56	1.00	...
J123704.9+525502	S	12:37:04.91	+52:55:02.5	18.33	-22.76	408.5	176.5	9.72e+25	II	II	0.282 ^b	69	1.05	...
J123847.4+520301	S	12:38:47.47	+52:03:01.0	17.26	-23.08	59.6	179.9	8.22e+24	I	II	0.221 ^a	42	1.00	A158
J124022.9+365333	V	12:40:22.90	+36:53:33.0	18.17	-23.96	34.3	73.0	1.54e+25	I	I	0.373 ^a	57	2.16	...
J124046.7-022433	S	12:40:46.75	-02:24:33.6	20.38	-21.81	51.9	178.9	2.43e+25	II	II	0.379 ^b	99	2.30	...
J124106.3+382348	V	12:41:06.30	+38:23:48.0	16.98	-23.15	96.9	114.0	9.62e+24	I	I	0.190 ^a	53	1.00	...
J124108.7+273447	V	12:41:08.70	+27:34:47.0	16.23	-23.99	172.6	126.0	1.89e+25	I	I	0.199 ^a	76	1.00	A158

Table 6 — *Continued*

Source Name	Smp1 ¹	α	δ	m_r	M_r	S	Angle	$P_{1440 \text{ MHz}}$	FR ²	FR ³	z	$N_{1.0}^{-19}$	f_c	Abel
(1)	(2)	(3)	(4)	(mag) (5)	(mag) (6)	(mJy) (7)	(deg) (8)	(W Hz ⁻¹) (9)	(10)	(11)	(12)	(13)	(14)	(15)
J124311.6+074049	A	12:43:11.65	+07:40:49.4	19.47	-22.60	13.6	147.6	5.80e+24	I	II	0.364 ^b	105	2.06	...
J124319.8-013405	S	12:43:19.81	-01:34:05.3	18.66	-23.60	6.2	169.8	3.09e+24	I	I	0.390 ^a	47	2.42	...
J124447.9+313923	V	12:44:47.90	+31:39:23.0	18.53	-22.24	24.9	78.0	4.26e+24	I	II	0.243 ^b	74	1.00	...
J124455.0+313824	A	12:44:55.06	+31:38:24.8	19.00	-22.00	16.9	96.0	3.46e+24	I	II	0.263 ^b	70	1.00	...
J124651.9+300521	V	12:46:51.90	+30:05:21.0	16.26	-22.94	124.1	53.0	5.83e+24	I	I	0.135 ^b	66	1.00	A161
J124942.2+303838	V	12:49:42.20	+30:38:38.0	16.89	-23.28	93.1	104.0	9.63e+24	I	I	0.194 ^a	46	1.00	...
J124950.4+071319	A	12:49:50.47	+07:13:19.6	16.74	-23.78	27.5	122.4	2.95e+24	II	I	0.197 ^b	73	1.00	...
J125115.7+224841	A	12:51:15.78	+22:48:41.5	18.28	-23.42	37.2	163.8	1.26e+25	I	I	0.329 ^a	62	1.54	...
J125441.1+444218	S	12:54:41.16	+44:42:18.9	19.25	-22.91	12.6	170.8	5.79e+24	I	I	0.376 ^b	81	2.22	...
J125923.3+275444	V	12:59:23.30	+27:54:44.0	13.59	-23.12	248.2	135.0	1.34e+24	I	I	0.048 ^b	172	1.00	A165
J125930.1+490559	A	12:59:30.15	+49:05:59.5	19.56	-22.47	11.0	69.7	4.43e+24	I	I	0.356 ^b	70	1.98	...
J125935.6+275735	V	12:59:35.60	+27:57:35.0	12.08	-23.04	205.9	93.0	2.68e+23	I	I	0.024 ^a	166	1.00	A165
J130053.5-031127	S	13:00:53.51	-03:11:27.5	17.81	-22.81	19.9	168.0	3.06e+24	I	II	0.232 ^b	46	1.00	...
J130153.2+254414	S	13:01:53.22	+25:44:14.7	18.11	-23.39	81.3	163.9	2.41e+25	I	II	0.310 ^a	94	1.34	...
J130317.0+315004	V	13:03:17.00	+31:50:04.0	16.93	-22.67	225.6	157.0	1.45e+25	II	I	0.156 ^b	119	1.00	A166
J130400.3+012302	S	13:04:00.38	+01:23:02.0	16.88	-23.49	28.1	174.7	3.53e+24	I	I	0.211 ^a	44	1.00	...
J130549.3+242755	V	13:05:49.30	+24:27:55.0	19.02	-23.41	27.6	64.0	1.52e+25	I	I	0.408 ^b	76	2.88	...
J130657.5+312244	A	13:06:57.58	+31:22:45.0	16.37	-23.70	25.0	126.6	2.41e+24	I	I	0.188 ^b	54	1.00	...
J130719.6+545435	S	13:07:19.66	+54:54:35.4	18.46	-23.30	21.0	169.8	7.57e+24	I	I?	0.338 ^a	43	1.61	...
J131015.3+545833	S	13:10:15.31	+54:58:33.5	19.13	-22.78	225.8	174.4	8.70e+25	II	II	0.349 ^b	49	1.80	...
J131451.6+383417	A	13:14:51.68	+38:34:17.8	17.22	-23.49	8.7	127.2	1.39e+24	I	I	0.236 ^a	54	1.00	...
J131753.8+523300	S	13:17:53.84	+52:33:00.5	18.40	-22.88	24.1	172.3	5.97e+24	I	II	0.287 ^b	55	1.18	...
J131756.7+314447	V	13:17:56.70	+31:44:47.0	17.44	-23.05	26.3	31.0	3.54e+24	I	I	0.218 ^b	55	1.00	...
J131827.2+342136	A	13:18:27.26	+34:21:36.4	18.87	-23.47	29.7	129.8	1.52e+25	I	II	0.395 ^a	277	2.63	A171
J131938.9+354800	A	13:19:38.98	+35:48:00.6	18.44	-22.62	13.6	130.9	2.87e+24	I	I	0.267 ^b	53	1.03	...
J132503.6+233131	S	13:25:03.69	+23:31:31.4	20.42	-21.67	7.8	177.9	3.58e+24	II	I	0.375 ^b	92	2.10	...
J132523.6+341954	V	13:25:23.60	+34:19:54.0	16.70	-22.51	99.1	91.0	4.73e+24	I	I	0.136 ^b	45	1.00	...
J132610.9+093253	A	13:26:11.00	+09:32:53.7	18.82	-21.60	112.0	83.0	1.37e+25	II	II	0.209 ^b	72	1.00	...
J132624.5+242222	S	13:26:24.54	+24:22:22.8	18.60	-23.74	36.6	170.5	1.95e+25	I	I?	0.402 ^a	49	2.62	...
J133006.0-014304	A	13:30:06.10	-01:43:04.8	17.09	-18.69	28.3	74.5	6.70e+22	II	II?	0.032 ^b	47	1.00	A175
J133006.4+405458	A	13:30:06.46	+40:54:58.8	18.58	-23.59	16.6	92.6	7.66e+24	I	I	0.377 ^b	98	2.24	...
J133307.0+153145	A	13:33:07.01	+15:31:45.4	18.53	-23.61	28.9	111.3	1.31e+25	I	I	0.374 ^b	172	2.20	...
J133415.8+332340	V	13:34:15.80	+33:23:40.0	18.47	-22.35	30.5	139.0	5.44e+24	I	I	0.248 ^b	46	1.00	...
J133421.6+332305	V	13:34:21.60	+33:23:05.0	18.18	-22.72	32.1	128.0	6.02e+24	I	I	0.253 ^b	49	1.00	...
J133520.1+410004	V	13:35:20.10	+41:00:04.0	16.31	-24.07	857.2	76.0	1.04e+26	II	I	0.208 ^b	206	1.00	A176
J133535.8+065250	S	13:35:35.89	+06:52:50.6	19.27	-23.04	12.3	178.0	6.12e+24	I	I?	0.390 ^b	64	2.56	...
J133623.9+342221	S	13:36:23.95	+34:22:21.4	17.78	-23.43	74.6	171.2	1.77e+25	I	II	0.281 ^a	96	1.13	...
J133724.8+332003	A	13:37:24.89	+33:20:03.6	17.45	-23.47	28.3	137.0	5.40e+24	I	II	0.255 ^a	49	1.00	...
J133830.8+152737	S	13:38:30.83	+15:27:37.4	18.61	-22.53	18.6	167.9	4.35e+24	I	I	0.279 ^b	53	1.09	...
J134251.6+311052	S	13:42:51.66	+31:10:52.6	18.10	-23.18	140.3	176.2	3.42e+25	II	II	0.285 ^a	94	1.17	...
J134354.5+324151	A	13:43:54.57	+32:41:51.7	19.31	-22.19	19.2	76.5	5.91e+24	I	I	0.315 ^b	123	1.35	...
J134643.7+570000	S	13:46:43.72	+57:00:00.3	17.83	-23.70	6.5	176.6	1.89e+24	I	I	0.308 ^a	43	1.37	...
J135103.4+305405	V	13:51:03.40	+30:54:05.0	17.04	-23.71	119.2	176.0	1.69e+25	I	I?	0.239 ^b	83	1.00	...
J135121.6+102256	A	13:51:21.67	+10:22:56.7	19.10	-23.28	41.4	63.5	2.27e+25	I	I	0.407 ^b	197	2.74	...
J135144.5+030419	A	13:51:44.59	+03:04:19.9	18.58	-23.42	38.7	111.6	1.61e+25	I	I	0.361 ^a	72	1.93	...
J135341.7+331339	A	13:53:41.71	+33:13:39.6	14.48	-22.22	34.5	158.9	1.84e+23	I	I	0.048 ^b	56	1.00	...
J135645.8-011146	S	13:56:45.87	-01:11:46.8	18.15	-24.16	80.0	170.8	4.14e+25	I	II	0.396 ^a	72	2.54	...
J135812.1+511925	A	13:58:12.13	+51:19:25.5	17.79	-22.74	18.0	119.5	2.51e+24	I	I	0.222 ^b	45	1.00	...
J140010.3-023734	S	14:00:10.34	-02:37:34.5	18.95	-23.38	29.5	172.7	1.50e+25	I	I	0.393 ^b	58	2.59	...
J140220.7+013910	S	14:02:20.76	+01:39:10.0	17.53	-23.35	16.4	168.6	3.08e+24	I	I	0.253 ^a	96	1.00	...
J140332.7+292924	V	14:03:32.70	+29:29:24.0	18.02	-23.05	66.5	0.0	1.43e+25	I	I	0.270 ^b	123	1.04	...
J140346.9+590611	S	14:03:46.94	+59:06:11.9	19.29	-23.04	9.8	176.7	5.03e+24	I	II	0.395 ^b	78	2.61	...
J140604.0+404138	V	14:06:04.00	+40:41:38.0	16.44	-23.93	295.3	66.0	3.69e+25	I	I	0.211 ^a	89	1.00	...
J140631.7+093620	S	14:06:31.70	+09:36:20.8	16.36	-23.04	47.3	175.4	2.65e+24	I	I	0.146 ^a	45	1.00	...
J140656.6+443715	A	14:06:56.62	+44:37:15.8	20.48	-21.53	62.8	136.0	2.57e+25	II	I	0.358 ^b	58	1.95	...
J141231.7+140041	A	14:12:31.74	+14:00:41.3	16.05	-23.24	47.8	135.6	2.44e+24	I	II	0.140 ^a	98	1.00	A187
J141236.4+094213	S	14:12:36.43	+09:42:13.3	17.73	-23.84	16.9	174.9	5.34e+24	I	II	0.319 ^a	69	1.41	...
J141744.9+211604	S	14:17:44.93	+21:16:04.1	18.78	-23.53	17.2	176.3	8.71e+24	I	II	0.393 ^b	141	2.57	...
J141811.5+321138	V	14:18:11.50	+32:11:38.0	18.40	-23.63	26.3	115.0	1.10e+25	I	I	0.361 ^a	76	1.99	...
J141833.0+232332	A	14:18:33.01	+23:23:32.4	17.93	-24.05	20.9	130.3	8.97e+24	I	II	0.365 ^a	47	1.91	...
J142041.8+250035	V	14:20:41.80	+25:00:35.0	17.72	-24.29	115.2	92.0	4.86e+25	I	I	0.363 ^a	120	1.95	A189
J142051.9+251300	A	14:20:51.94	+25:13:00.9	21.39	-20.48	20.7	91.4	8.80e+24	II	I?	0.364 ^b	58	1.75	A189
J142137.0+610027	A	14:21:37.08	+61:00:27.5	17.97	-23.57	23.3	111.2	6.84e+24	I	I	0.309 ^a	94	1.38	...
J142443.8+405435	V	14:24:43.80	+40:54:35.0	17.96	-22.83	35.0	116.0	6.07e+24	I	I	0.245 ^b	84	1.00	...
J142443.9+405438	A	14:24:43.90	+40:54:38.0	17.96	-22.83	35.0	116.2	6.07e+24	I	I	0.245 ^b	85	1.00	...
J142446.4+040345	A	14:24:46.48	+04:03:45.3	18.67	-23.16	20.3	131.2	7.54e+24	I	I	0.343 ^b	115	1.69	...
J142543.9+395821	A	14:25:43.93	+39:58:21.0	19.00	-23.38	19.8	102.8	1.07e+25	I	II?	0.405 ^a	96	2.74	...
J142545.8+264553	V	14:25:45.80	+26:45:53.0	17.34	-22.53	14.4	81.0	1.20e+24	I	I	0.176 ^a	92	1.00	A191

Table 6 — *Continued*

Source Name	Smp1 ¹	α	δ	m_r (mag)	M_r (mag)	S (mJy)	Angle (deg)	$P_{1440\text{ MHz}}$ (W Hz ⁻¹)	FR ²	FR ³	z	N _{1.0} ⁻¹⁹	f_c	Abel
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)	(15)
J142715.6+503228	A	14:27:15.67	+50:32:29.0	17.76	-23.65	10.9	126.8	2.94e+24	I	I	0.298 ^a	82	1.27	...
J142755.0+255436	A	14:27:55.03	+25:54:36.8	18.74	-22.71	39.0	92.6	1.13e+25	I	I	0.307 ^b	67	1.30	...
J142821.8+235319	A	14:28:21.87	+23:53:19.8	15.95	-23.26	49.2	125.5	2.34e+24	I	I	0.135 ^a	43	1.00	...
J142821.9+235320	V	14:28:21.90	+23:53:20.0	15.95	-23.26	49.2	126.0	2.34e+24	I	I	0.135 ^a	43	1.00	...
J143320.5+191330	A	14:33:20.52	+19:13:30.4	17.06	-23.34	23.0	120.5	2.88e+24	I	I	0.211 ^a	44	1.00	...
J143346.7+021755	S	14:33:46.79	+02:17:55.2	18.70	-23.17	170.8	177.9	6.66e+25	II	II	0.350 ^b	41	1.76	...
J143357.2+174023	A	14:33:57.22	+17:40:23.0	18.99	-22.56	15.8	108.7	4.99e+24	I	I	0.319 ^b	47	1.39	...
J143424.0+151410	A	14:34:24.03	+15:14:10.9	16.46	-23.14	38.9	74.7	2.58e+24	I	I	0.158 ^a	49	1.00	...
J143631.1+431125	S	14:36:31.15	+43:11:25.6	18.73	-23.48	27.9	178.2	1.29e+25	I	I	0.377 ^a	57	2.33	...
J143716.6+161604	S	14:37:16.64	+16:16:04.4	16.97	-24.06	35.9	175.4	7.48e+24	I	I	0.266 ^a	62	1.02	...
J143716.9+245209	V	14:37:16.90	+24:52:09.0	15.99	-22.19	219.0	154.0	4.33e+24	I	I	0.090 ^a	68	1.00	A193
J143732.4+163802	S	14:37:32.40	+16:38:03.0	17.54	-23.49	7.6	177.6	1.58e+24	I	I	0.265 ^a	106	1.01	...
J143822.6+034016	S	14:38:22.69	+03:40:16.9	20.95	-20.30	743.3	174.0	1.88e+26	II	I	0.290 ^b	213	1.15	A194
J143919.6+480832	S	14:39:19.62	+48:08:32.5	18.97	-23.36	19.0	165.7	9.63e+24	I	II	0.392 ^a	62	2.59	...
J143950.3+415217	A	14:39:50.35	+41:52:17.3	18.49	-23.82	16.9	109.2	8.40e+24	I	I	0.390 ^a	48	2.55	...
J143958.9+284857	V	14:39:58.90	+28:48:57.0	17.77	-23.07	100.9	61.0	1.83e+25	I	I	0.250 ^a	86	1.00	...
J144032.2+240937	S	14:40:32.23	+24:09:37.8	19.51	-22.22	15.8	177.7	5.19e+24	II	I?	0.325 ^b	83	1.57	...
J144408.4+354745	A	14:44:08.40	+35:47:45.4	18.19	-23.70	33.6	135.9	1.31e+25	I	II	0.350 ^a	110	1.77	...
J144422.1+211453	S	14:44:22.19	+21:14:53.4	18.77	-22.39	55.9	167.9	1.27e+25	II	II	0.276 ^b	43	1.10	...
J144603.4+305852	A	14:46:03.43	+30:58:52.9	18.06	-23.10	31.0	145.3	7.20e+24	I	II	0.279 ^b	81	1.09	...
J144603.5+305853	V	14:46:03.50	+30:58:53.0	18.06	-23.10	31.0	145.0	7.20e+24	I	II	0.279 ^b	82	1.09	...
J144815.3+093843	A	14:48:15.39	+09:38:43.8	18.41	-22.72	18.9	150.9	4.24e+24	I	II	0.275 ^b	46	1.07	...
J144859.7+360306	S	14:48:59.75	+36:03:06.2	19.43	-22.99	22.8	174.8	1.19e+25	I	II	0.397 ^b	57	2.85	...
J145004.9+140645	A	14:50:04.92	+14:06:46.0	18.00	-23.48	44.4	126.5	1.31e+25	I	I	0.309 ^a	94	1.32	...
J145046.5+263625	V	14:50:46.50	+26:36:25.0	18.24	-22.97	14.7	122.0	3.48e+24	I	I	0.281 ^b	114	1.12	...
J145114.4+304423	S	14:51:14.48	+30:44:23.5	16.83	-22.29	26.1	164.7	1.16e+24	I	I?	0.131 ^b	65	1.00	A198
J145213.0+375251	V	14:52:13.00	+37:52:51.0	17.58	-23.96	47.5	58.0	1.43e+25	I	I	0.313 ^b	177	1.37	...
J145302.8+330842	S	14:53:02.86	+33:08:42.4	17.69	-23.26	66.8	176.3	1.20e+25	I	II	0.248 ^a	49	1.00	...
J145329.9+142111	S	14:53:29.95	+14:21:11.3	18.16	-24.16	23.1	175.5	1.15e+25	I	I	0.389 ^b	108	2.57	...
J145416.2+152739	S	14:54:16.26	+15:27:39.1	18.41	-23.26	20.8	170.5	6.77e+24	I	I	0.324 ^a	62	1.51	...
J145444.4+262223	S	14:54:44.43	+26:22:23.2	16.95	-23.59	50.8	167.7	7.13e+24	I	I	0.222 ^a	50	1.00	...
J145556.2+044149	S	14:55:56.30	+04:41:49.7	19.05	-23.09	85.8	170.7	3.90e+25	II	I	0.375 ^b	85	2.19	...
J145722.6+023255	A	14:57:22.63	+02:32:55.1	16.88	-22.64	79.2	147.4	4.82e+24	I	I	0.152 ^a	47	1.00	...
J145900.2+275401	V	14:59:00.20	+27:54:01.0	17.69	-22.96	14.6	119.0	2.18e+24	I	I	0.229 ^a	53	1.00	A200
J150107.8+521511	A	15:01:07.81	+52:15:11.0	18.20	-23.41	37.7	75.4	1.20e+25	I	I	0.320 ^a	53	1.45	...
J150210.6+171837	S	15:02:10.67	+17:18:38.0	18.54	-23.61	33.8	168.5	1.59e+25	I	I	0.380 ^a	76	2.19	...
J150233.4+425554	A	15:02:33.43	+42:55:55.0	18.17	-23.17	34.0	91.5	8.82e+24	I	I	0.293 ^a	48	1.22	...
J150456.4+143447	S	15:04:56.47	+14:34:47.5	18.37	-22.89	104.8	175.9	2.50e+25	II	I	0.282 ^a	72	1.15	...
J150957.3+332715	V	15:09:57.30	+33:27:15.0	15.91	-22.94	152.4	67.0	5.32e+24	I	I	0.117 ^a	140	1.00	A203
J151130.8+322821	V	15:11:30.80	+32:28:21.0	20.19	-21.77	177.4	143.0	7.30e+25	II	II	0.359 ^b	74	1.87	...
J151443.9+223725	V	15:14:43.90	+22:37:25.0	18.14	-24.11	141.4	80.0	6.82e+25	I	I	0.384 ^a	169	2.42	...
J152055.6+233723	A	15:20:55.70	+23:37:23.5	18.24	-23.32	42.5	100.1	1.29e+25	I	I	0.314 ^a	78	1.40	...
J152055.7+233726	V	15:20:55.70	+23:37:26.0	18.24	-23.32	42.5	100.0	1.29e+25	I	I	0.314 ^a	76	1.40	...
J152127.0+315732	V	15:21:27.00	+31:57:32.0	17.41	-23.98	79.0	104.0	2.07e+25	I	I	0.294 ^b	62	1.25	A206
J152350.6+361106	V	15:23:50.60	+36:11:06.0	17.84	-23.02	43.2	124.0	7.91e+24	I	I	0.251 ^b	102	1.00	...
J152642.0+005330	S	15:26:42.01	+00:53:30.1	15.24	-23.58	236.6	177.1	8.19e+24	I	I	0.117 ^b	46	1.00	...
J152753.9+474930	S	15:27:53.98	+47:49:30.7	18.51	-23.33	9.8	169.6	3.63e+24	I	II	0.343 ^a	114	1.71	...
J152945.7+304236	V	15:29:45.70	+30:42:36.0	15.16	-23.97	93.9	106.0	4.20e+24	I	I	0.132 ^b	55	1.00	A208
J153030.8+321053	V	15:30:30.80	+32:10:53.0	18.09	-22.78	28.4	32.0	5.22e+24	I	I	0.251 ^b	51	1.00	...
J153035.0+422444	A	15:30:35.09	+42:24:44.2	18.38	-23.63	27.2	135.7	1.14e+25	I	I	0.362 ^b	79	1.96	...
J153126.2+103102	A	15:31:26.29	+10:31:02.8	18.13	-22.88	12.7	124.2	2.58e+24	I	I	0.263 ^a	48	1.01	...
J153521.9+342243	V	15:35:21.90	+34:22:43.0	17.52	-23.55	179.8	43.0	3.91e+25	I	I	0.271 ^b	114	1.04	...
J153613.0+423318	S	15:36:13.03	+42:33:18.9	18.08	-23.74	35.6	175.6	1.37e+25	I	I	0.349 ^a	51	1.69	...
J153717.6+101328	A	15:37:17.69	+10:13:28.2	19.86	-21.32	21.9	139.6	6.00e+24	II	I	0.300 ^b	62	1.10	...
J154104.9+432702	V	15:41:04.90	+43:27:02.0	17.66	-23.45	114.9	134.0	2.43e+25	I	I	0.267 ^a	63	1.06	...
J154109.3+345620	S	15:41:09.37	+34:56:20.7	19.54	-22.88	46.4	166.0	2.59e+25	II	I	0.410 ^b	57	2.85	...
J154115.9+113843	A	15:41:15.95	+11:38:43.2	19.44	-21.85	21.6	139.4	5.14e+24	II	II?	0.282 ^b	83	1.18	...
J154118.9+514044	S	15:41:18.97	+51:40:44.3	15.78	-23.65	45.5	168.5	2.62e+24	I	II	0.148 ^a	41	1.00	...
J154451.4+344221	A	15:44:51.45	+34:42:21.0	18.18	-22.58	13.2	79.8	2.23e+24	I	I	0.242 ^b	75	1.00	...
J154455.1+102619	A	15:44:55.15	+10:26:19.0	18.06	-22.63	15.3	150.9	2.36e+24	I	II	0.232 ^b	62	1.00	...
J154952.5+190951	A	15:49:52.51	+19:09:51.3	16.90	-22.32	13.8	145.0	6.48e+23	I	I	0.135 ^a	56	1.00	...
J155053.2+501925	A	15:50:53.26	+50:19:25.7	18.79	-23.38	4.9	124.9	2.26e+24	I	I	0.376 ^b	185	2.24	...
J155246.8+092432	A	15:52:46.81	+09:24:32.7	19.35	-22.89	10.6	144.6	5.23e+24	I	I	0.388 ^b	99	2.38	...
J155750.2+534334	S	15:57:50.22	+53:43:34.2	17.81	-24.19	209.6	173.7	6.28e+25	I	I	0.312 ^a	117	1.93	...
J155848.1+303849	A	15:58:48.17	+30:38:49.6	18.57	-22.75	34.9	105.6	9.18e+24	I	I	0.295 ^b	49	1.20	...
J160012.8+181545	A	16:00:12.88	+18:15:45.7	18.29	-23.18	19.1	138.3	5.52e+24	I	II	0.307 ^a	131	1.32	...
J160723.8+344211	V	16:07:23.80	+34:42:11.0	17.18	-24.10	49.4	105.0	1.22e+25	I	I	0.286 ^a	61	1.17	...
J161129.8+050135	S	16:11:29.88	+05:01:35.6	19.39	-22.18	10.1	172.1	3.20e+24	I	I?	0.320 ^b	85	1.41	...
J161215.5+121644	A	16:12:15.54	+12:16:44.8	18.86	-23.19	21.8	124.0	9.32e+24	I	I	0.365 ^a	121	2.02	...
J161402.3+544409	A	16:14:02.34	+54:44:09.7	18.95	-22.99	33.1	83.0	1.36e+25	I	I	0.358 ^b	247	1.86	...

Table 6 — *Continued*

Source Name	Smpl ¹	α	δ	m_r (mag)	M_r (mag)	S (mJy)	Angle (deg)	$P_{1440\text{ MHz}}$ (W Hz ⁻¹)	FR ²	FR ³	z	$N_{1.0}^{-19}$	f_c	Abel
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)	(15)
J161429.6+403710	S	16:14:29.70	+40:37:10.9	16.88	-23.27	9.6	171.0	9.78e+23	I	I	0.193 ^b	42	1.00	...
J161547.8+031850	S	16:15:47.89	+03:18:50.8	19.74	-20.83	49.9	169.3	7.59e+24	II	I	0.231 ^b	68	1.00	...
J161610.9+090653	S	16:16:10.96	+09:06:53.3	18.94	-21.07	167.7	166.3	1.57e+25	II	I	0.185 ^b	135	1.00	...
J161925.3+202549	S	16:19:25.33	+20:25:49.9	17.47	-23.06	80.0	176.6	1.13e+25	I	I	0.223 ^b	54	1.00	...
J162007.1+422846	V	16:20:07.10	+42:28:46.0	16.38	-23.17	163.7	72.0	1.03e+25	I	I	0.154 ^b	62	1.00	A217
J162311.1+522133	A	16:23:11.13	+52:21:33.0	18.53	-22.03	15.4	99.2	2.25e+24	I	II?	0.226 ^b	51	1.00	...
J162758.0+334547	V	16:27:58.00	+33:45:47.0	16.91	-22.77	60.0	126.0	4.28e+24	I	II	0.163 ^a	50	1.00	...
J162806.7+130015	A	16:28:06.74	+13:00:15.8	18.00	-22.28	30.7	71.8	3.59e+24	I	II	0.205 ^b	40	1.00	...
J163002.4+542133	S	16:30:02.46	+54:21:33.4	18.09	-22.95	24.6	169.6	5.00e+24	I	II?	0.263 ^b	62	1.02	...
J163310.9+360735	S	16:33:10.91	+36:07:35.2	17.11	-22.53	21.7	172.9	1.48e+24	I	II	0.160 ^b	68	1.00	...
J163351.2+171055	A	16:33:51.23	+17:10:55.2	17.96	-23.85	30.9	141.6	1.10e+25	I	I	0.337 ^b	76	1.68	...
J163516.7+202053	S	16:35:16.75	+20:20:53.8	19.38	-21.83	81.5	167.0	1.88e+25	II	I	0.278 ^b	151	1.12	...
J163549.0+290229	V	16:35:49.00	+29:02:29.0	19.44	-22.30	38.3	162.0	1.32e+25	II	I	0.331 ^b	53	1.59	...
J164054.0+324730	V	16:40:54.00	+32:47:30.0	16.36	-22.87	58.9	41.0	2.83e+24	I	I	0.136 ^a	66	1.00	...
J164602.3+530048	A	16:46:02.35	+53:00:48.3	18.64	-23.32	36.5	146.9	1.50e+25	I	I	0.358 ^b	76	1.88	...
J164827.0+511819	A	16:48:27.08	+51:18:19.6	18.30	-22.95	25.0	150.5	6.05e+24	I	I?	0.284 ^b	92	1.15	...
J165007.8+320208	V	16:50:07.80	+32:02:08.0	18.23	-23.12	32.1	109.0	8.54e+24	I	I	0.296 ^a	92	1.23	...
J165013.6+320201	V	16:50:13.61	+32:02:01.0	18.74	-22.63	9.5	3.0	2.54e+24	I	I	0.297 ^b	79	1.24	...
J165514.4+221245	V	16:55:14.40	+22:12:45.0	18.04	-22.30	32.8	70.0	3.92e+24	I	I	0.207 ^b	64	1.00	...
J165618.5+435157	V	16:56:18.49	+43:51:57.0	18.00	-23.88	138.9	128.0	5.31e+25	I	I	0.347 ^b	45	1.77	...
J165711.0+333126	S	16:57:11.05	+33:31:26.8	17.40	-23.55	15.7	169.7	3.08e+24	I	I	0.258 ^b	58	1.00	...
J165734.2+165554	S	16:57:34.29	+16:55:54.3	20.06	-21.15	76.3	171.8	1.88e+25	II	II	0.286 ^b	43	1.13	...
J170209.3+332246	V	17:02:09.30	+33:22:46.0	19.89	-22.32	24.4	128.0	1.14e+25	II	I	0.380 ^b	75	2.33	...
J170650.1+613429	S	17:06:50.19	+61:34:29.8	20.20	-21.99	15.0	168.9	1.06e+25	II	I	0.454 ^b	80	2.29	...
J170724.5+234926	A	17:07:24.60	+23:49:26.7	17.78	-23.97	33.3	145.3	1.15e+25	I	II	0.333 ^a	66	1.60	...
J171445.8+433759	S	17:14:45.80	+43:37:59.8	17.99	-22.99	117.2	179.5	2.31e+25	II	II	0.259 ^b	56	1.00	...
J171759.8+533651	S	17:17:59.89	+53:36:51.8	18.11	-23.31	17.9	178.3	4.83e+24	I	II	0.298 ^a	51	1.28	...
J172320.7+355805	V	17:23:20.70	+35:58:05.0	16.29	-22.75	276.4	132.0	1.14e+25	I	I	0.127 ^b	49	1.00	...
J172853.4+342347	S	17:28:53.44	+34:23:47.1	19.64	-21.39	42.5	177.7	9.39e+24	II	II	0.273 ^b	40	1.02	...
J212434.9-003206	S	21:24:34.94	-00:32:06.2	17.50	-23.20	76.5	174.5	1.22e+25	I	I	0.235 ^a	77	1.00	...
J213550.4-075231	S	21:35:50.41	-07:52:32.0	18.98	-22.91	295.0	174.2	1.21e+26	II	II	0.359 ^b	108	1.78	...
J214237.4-080432	A	21:42:37.46	-08:04:32.0	16.24	-23.46	37.9	155.2	2.74e+24	I	II	0.165 ^b	102	1.00	A2367
J215423.6+003710	V	21:54:23.60	+00:37:10.0	18.37	-22.09	41.2	40.0	5.57e+24	II	???	0.219 ^b	156	1.00	A2392
J222051.5+005816	V	22:20:51.50	+00:58:16.0	18.21	-23.43	92.5	57.0	2.89e+25	I	I	0.318 ^a	139	1.48	...
J222421.1-003122	S	22:24:21.11	-00:31:22.7	18.51	-23.94	51.6	178.2	2.84e+25	I	II	0.407 ^a	54	2.92	...
J230909.8-003628	V	23:09:09.80	-00:36:28.0	19.89	-22.53	8.8	90.0	4.81e+24	I	I?	0.406 ^b	54	2.83	...
J233820.1-085129	A	23:38:20.19	-08:51:29.6	20.71	-21.27	60.9	121.3	2.60e+25	II	I	0.364 ^b	54	1.90	...
J234153.1-002302	V	23:41:53.09	-00:23:02.0	18.14	-23.00	15.9	143.0	3.70e+24	I	I	0.279 ^a	61	1.08	...
J234153.1-002301	A	23:41:53.11	-00:23:01.4	18.14	-23.00	15.9	142.7	3.70e+24	I	I	0.279 ^a	60	1.08	...

Note. — A question mark in Col. 11 represents a dubious visual FR I/II classification. Three successive question marks represent an inability to visually classify the radio source as either FR I or II.

¹ The sample each source belongs to: V = visual bent sample, A = auto bent sample, and S = straight sample.

² FR type determined following Ledlow & Owen (1996).

³ FR type determined visually.

^a The redshift comes from a spectroscopic measurement.

^b The redshift comes from a photometric measurement.

^c The difference in redshift between the identified Abell cluster (from NED) and the radio cluster is greater than 1500 km s⁻¹.

^d The Abell cluster does not have a confirmed redshift in NED.

Table 7
Richness distribution of sources with WAT-like radio powers

Sample (1)	$N_{1.0}^{-19} < 100$		$N_{1.0}^{-19} > 100$	
	# (2)	% (3)	# (4)	% (5)
Visual-Bent	138	55.8%	28	67.9%
Auto-Bent	242	44.6%	30	86.7%
Straight	430	46.5%	19	68.4%
Single-Component	351	3.7%	7	42.9%

Note. — Col. (1): name of the sample; col. (2): number of sources with a cluster richness measurement less than 100; col. (3): percentage of sources with $N_{1.0}^{-19} < 100$ and $24.75 < \log P_{1440 \text{ MHz}} < 25.75$; col. (4): number of sources with a cluster richness measurement greater than 100; col. (5): percentage of sources with $N_{1.0}^{-19} > 100$ and $24.75 < \log P_{1440 \text{ MHz}} < 25.75$.

Table 8
RASS-FSC Matches (within 1.0 Mpc)

Sample (1)	$N_{1.0}^{-19} < 40$			$N_{1.0}^{-19} \geq 40$		
	All (2)	$z \leq 0.25$ (3)	$z \leq 0.15$ (4)	All (5)	$z \leq 0.25$ (6)	$z \leq 0.15$ (7)
Visual-Bent	11.3%(62)	14.7%(34)	25.0%(12)	19.2%(104)	28.3%(53)	43.8%(16)
Auto-Bent	8.8%(137)	15.6%(64)	14.0%(29)	13.3%(135)	22.7%(44)	38.5%(13)
Straight	9.2%(304)	11.2%(152)	16.0%(58)	11.7%(145)	20.5%(44)	30.0%(10)
Single-Component	6.2%(305)	7.4%(175)	13.0%(84)	11.3%(53)	21.1%(19)	0.0%(2)

Note. — The numbers in parentheses correspond to the number of sources in each sample and sub-sample from which the percentages are calculated.

Table 9
RASS-FSC Matches (within 5'0)

Sample (1)	$N_{1.0}^{-19} < 40$			$N_{1.0}^{-19} \geq 40$		
	All (2)	$z \leq 0.25$ (3)	$z \leq 0.15$ (4)	All (5)	$z \leq 0.25$ (6)	$z \leq 0.15$ (7)
Visual-Bent	6.5%(62)	5.9%(34)	8.0%(12)	20.2%(104)	26.4%(53)	31.3%(16)
Auto-Bent	7.3%(137)	7.8%(64)	0.0%(29)	14.8%(135)	20.5%(44)	30.8%(13)
Straight	9.2%(304)	8.6%(152)	9.0%(58)	12.4%(145)	20.5%(44)	30.0%(10)
Single-Component	5.6%(305)	3.4%(175)	5.0%(84)	13.2%(53)	15.8%(19)	0.0%(2)

Note. — The numbers in parentheses correspond to the number of sources in each sample and sub-sample from which the percentages are calculated.

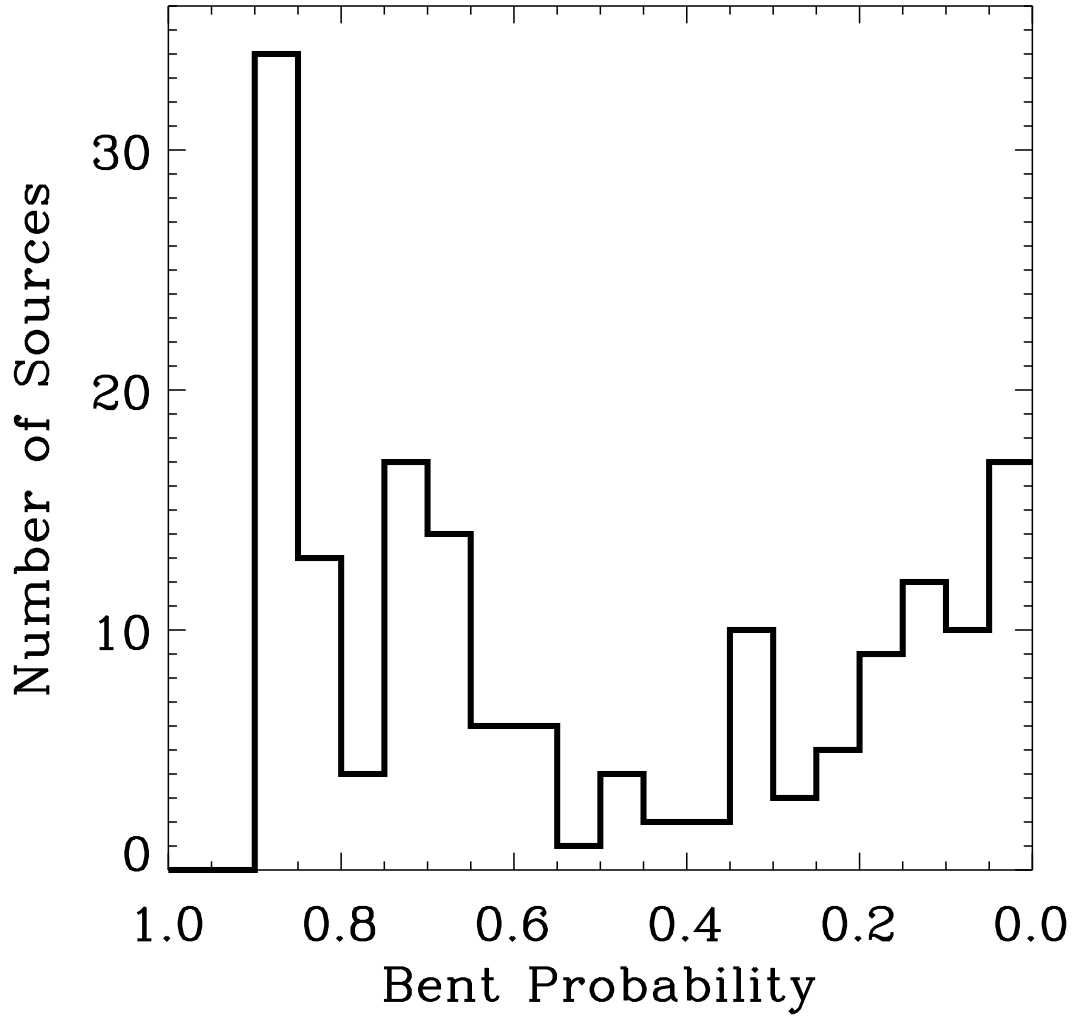


Figure 1. A histogram of the probability scores given to the 167 three-component sources in the visual-bent sample. A score of 1.0 corresponds to a probability of 100% that the source is a bent double-lobed source. The auto-bent sample is composed of sources with scores higher than 0.5. Some of the visual-bent sources have low probabilities as determined by the computer algorithm.

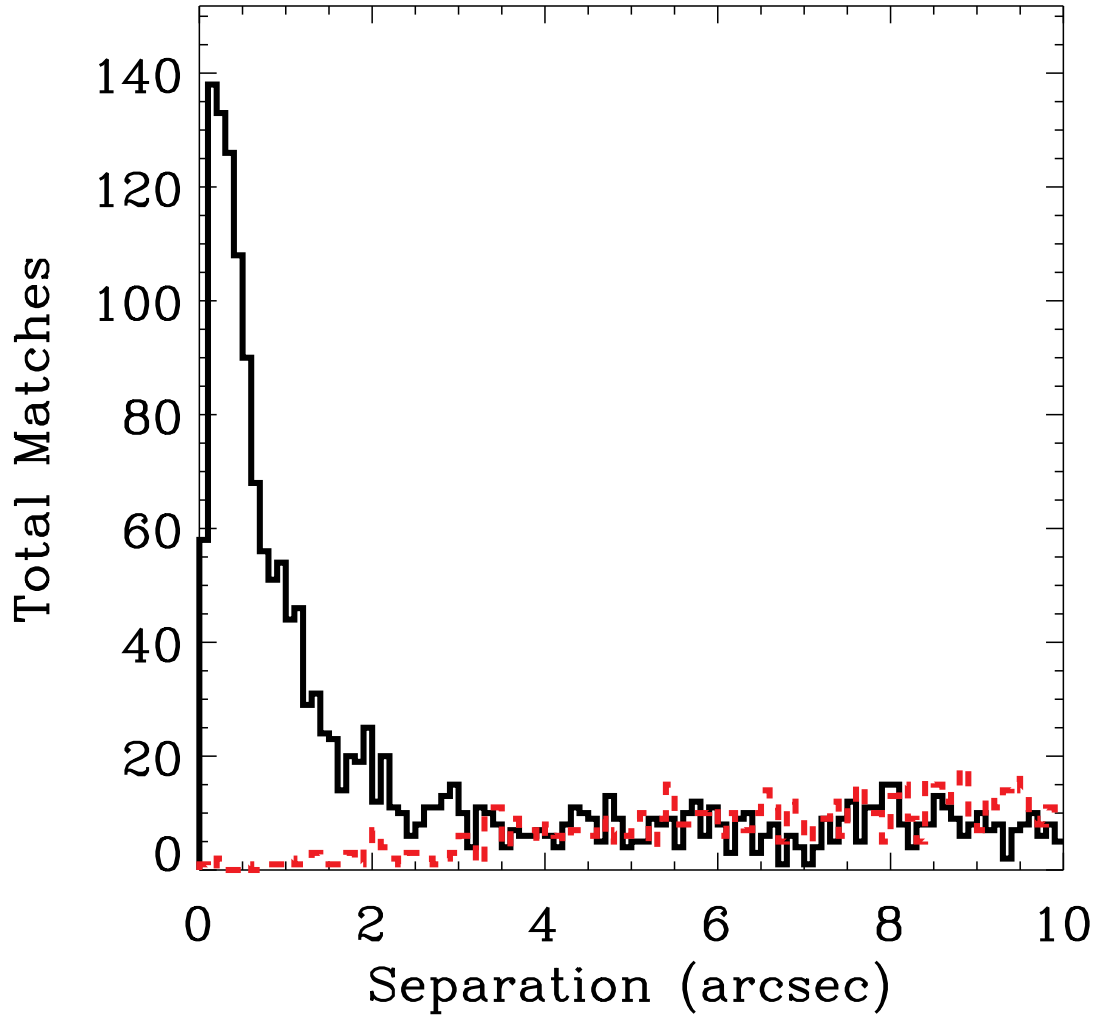


Figure 2. The black solid-line histogram represents the number of optical sources associated with radio sources (in this case from the straight sample) as a function of separation from the radio source center. The peak in the distribution at small separations is a result of real radio/optical counterparts. The red dashed-line histogram plots the distribution of optical matches as a function of separation for the shifted positions of the radio sources, i.e. a random sample of points on the sky. There is no peak at small separations but as the separation increases, the number of matches increases. At large separations the distribution of the real sample matches that of the random sample.

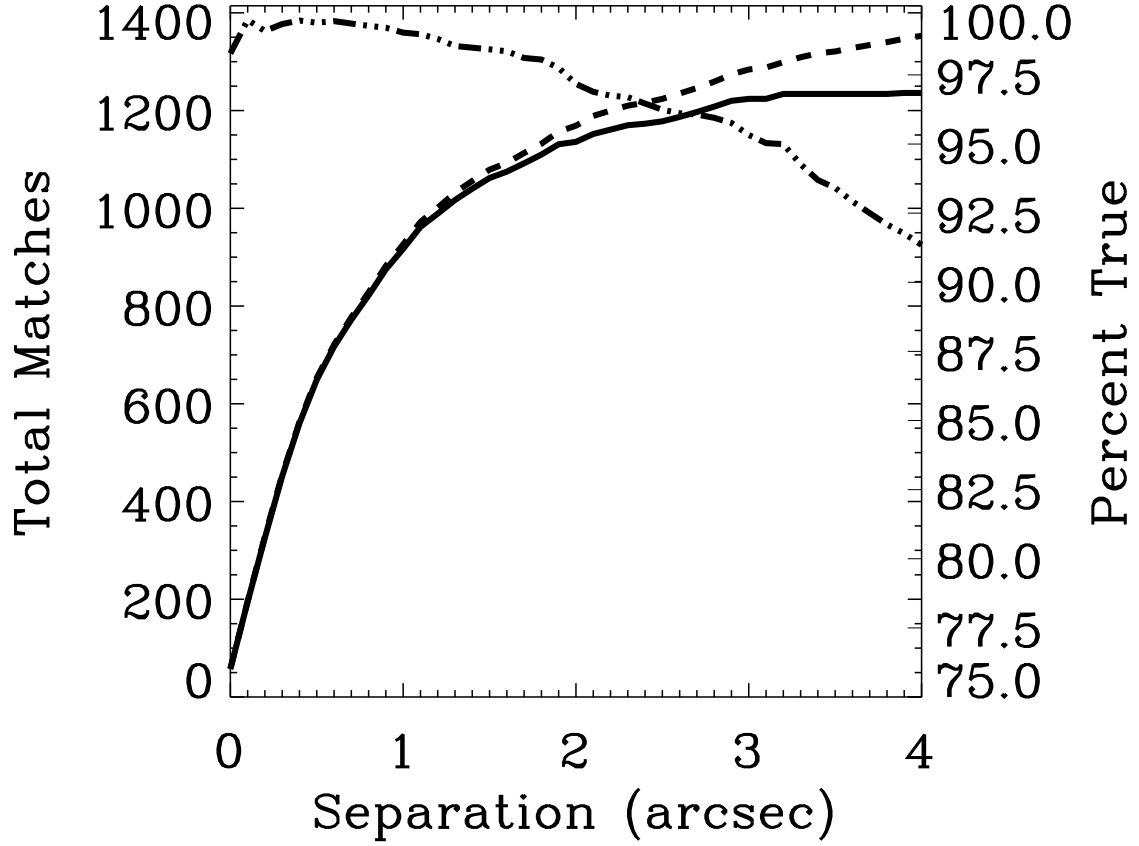


Figure 3. The solid-line represents the cumulative number of good, non-chance-coincidence, matches as the separation between the radio and optical sources is increased. The dashed-line shows the cumulative total number of matches with increasing separation. At a separation of around $3''$ the number of good matches starts to level off and the total number of matches continues to rise. This is illustrated by the dash-dotted-line which shows the percentage of matches that can be expected to be true matches as the separation is increased. We aimed for a 95% reliability cut-off, hence the $3''.2$ separation limit for considering an SDSS source a match with a FIRST source for the straight sample shown here.

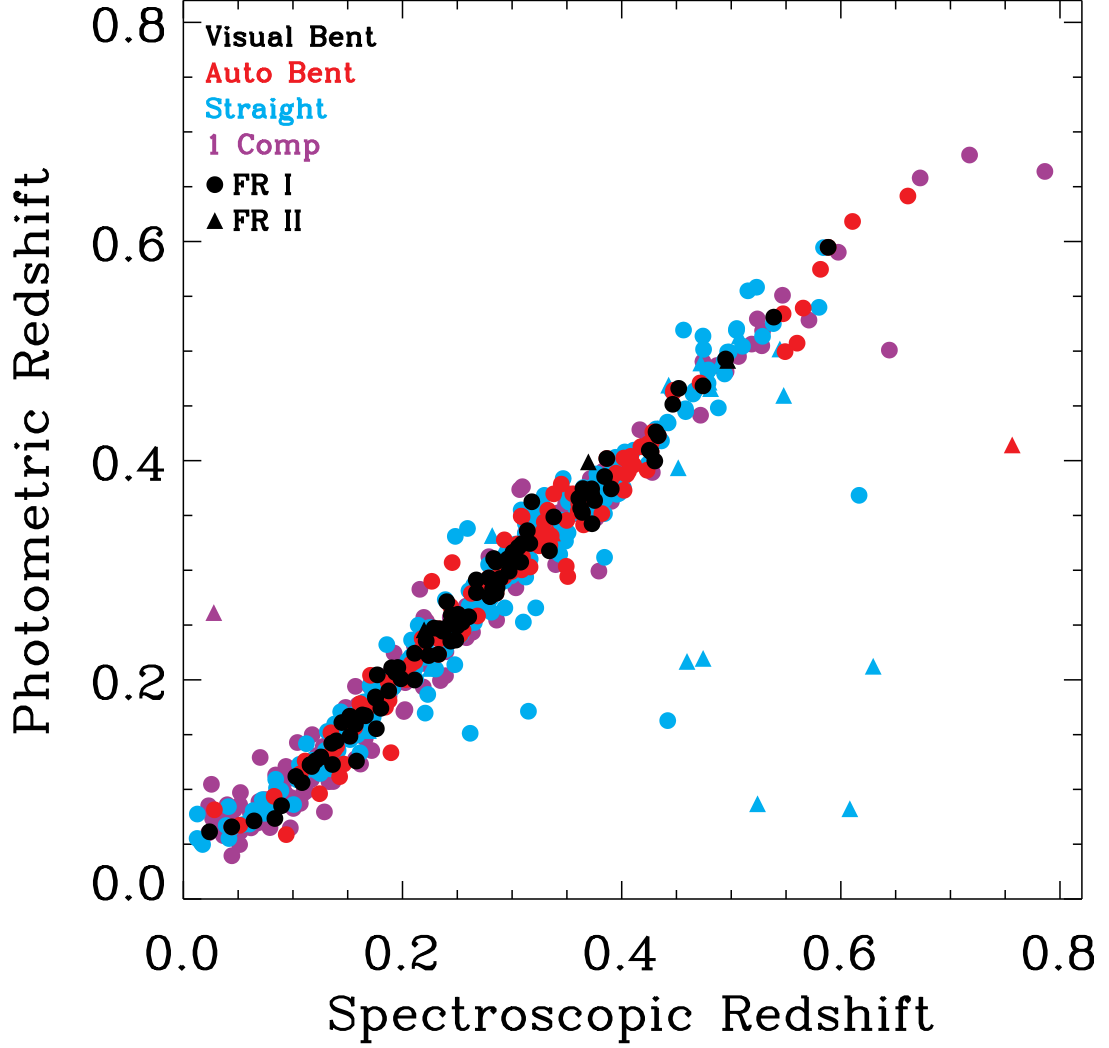


Figure 4. A plot of the spectroscopic redshifts versus the photometric redshifts for the sources in each sample. The photometric redshift here is from the `photoz` table. Not all of the sources with measured spectroscopic redshifts have calculated photometric redshifts. This mostly applies to the sources identified by SDSS as point sources. In general, the spectroscopic and photometric redshifts agree well. Purple filled symbols represent the single-component sample, blue filled symbols represent the straight sample, red filled symbols represent the auto-bent sample, and black filled symbols represent the visual-bent sample. The FR I sources are represented by circles and the FR II sources are represented by triangles.

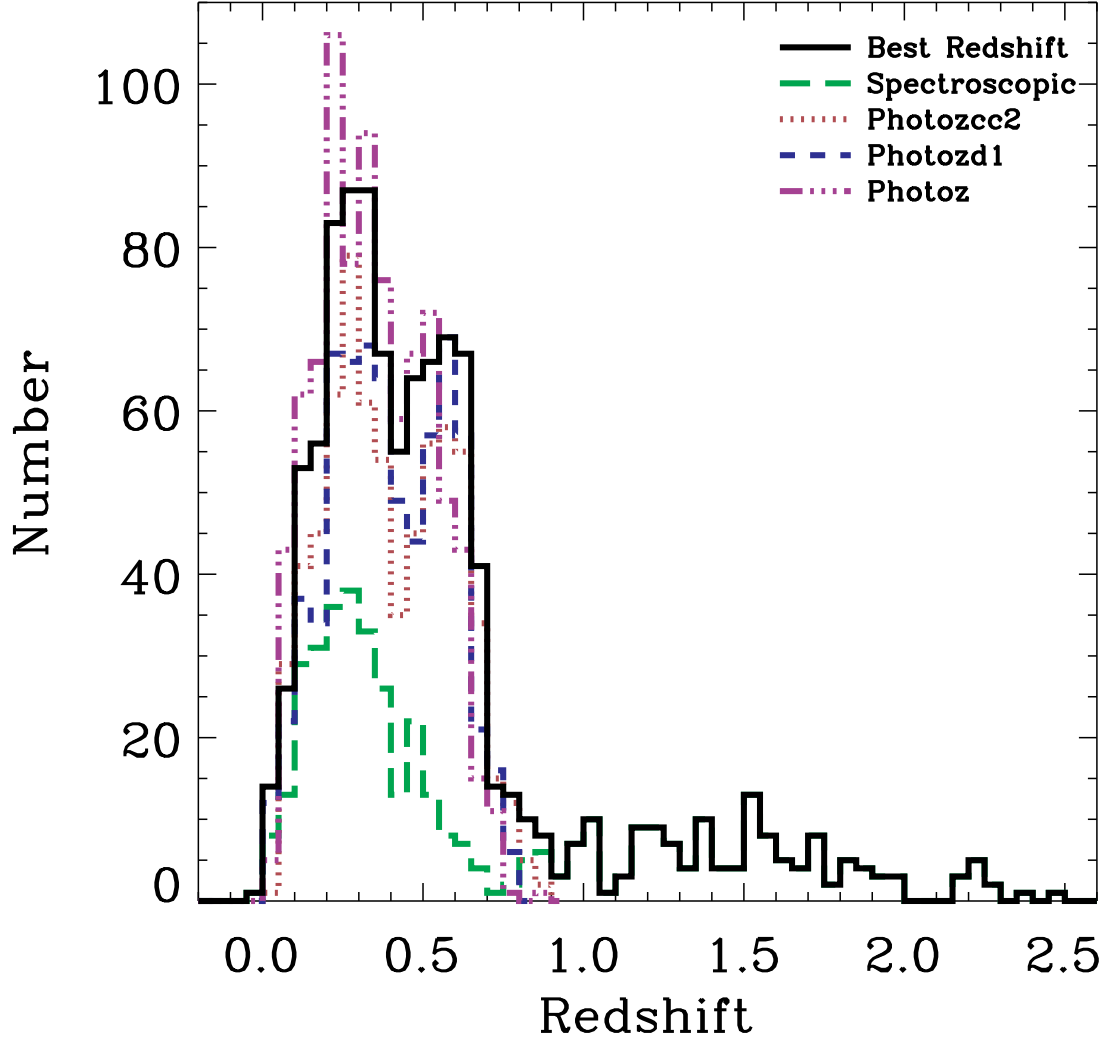


Figure 5. The (black) solid-line is representative of the overall distribution of redshifts, the best redshift for each source as described in §3.2. The green long-dashed-line represents the spectroscopically measured redshifts, and the maroon dotted- and blue short-dashed-lines represent the redshifts given by the adaptive learning decision tree program that calculated the `photoz2` catalog (see §3.2). The purple dash-dotted line represents the redshifts as calculated by the `photoz` catalog. This plot is for the straight sample. The other samples have similar distributions for the various redshift measurement techniques. The distributions of the best redshifts for each sample can be seen in Figure 6.

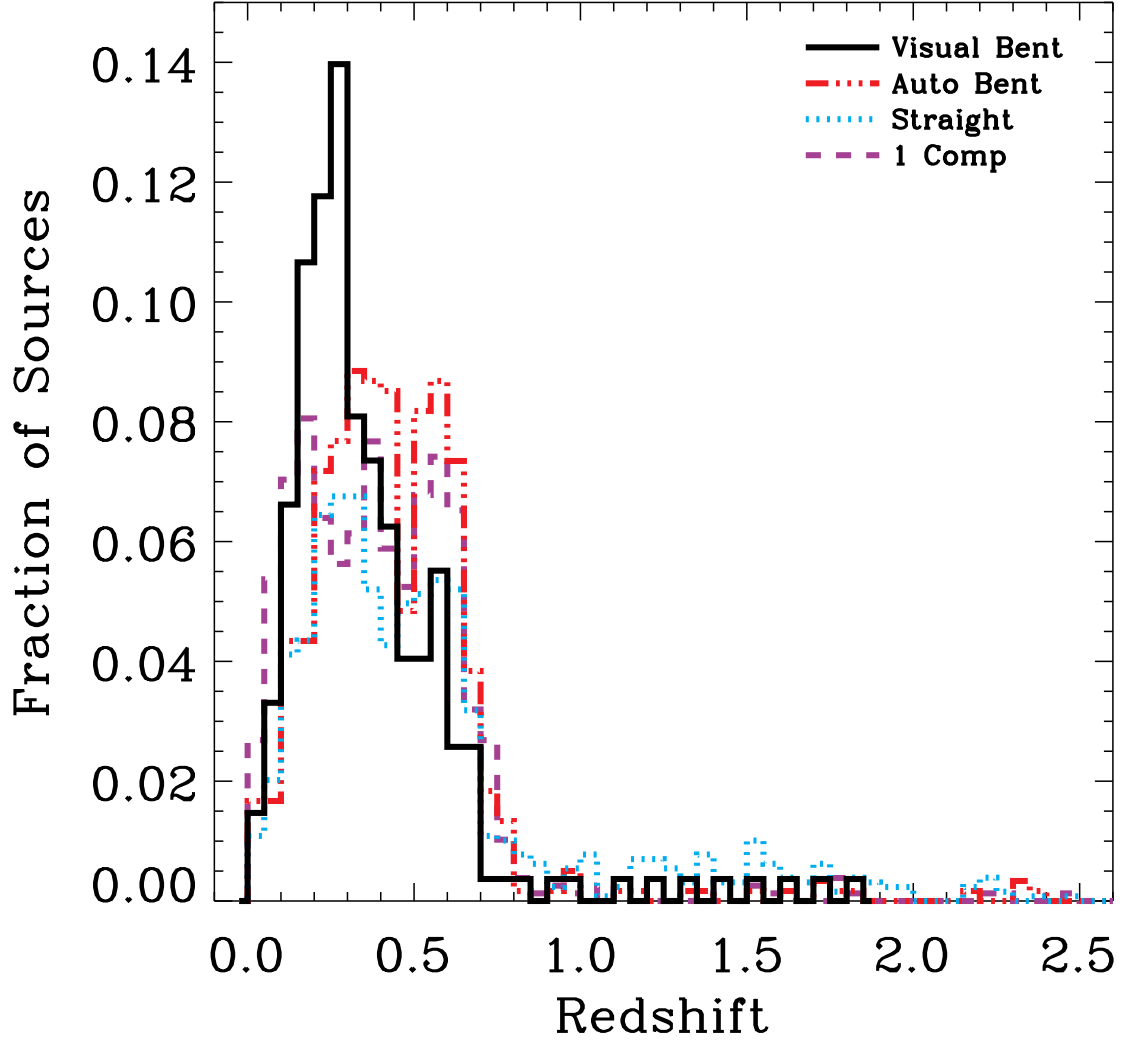


Figure 6. The distribution of redshifts for each sample. The black solid-line represents the visual-bent sample, the red dash-dotted line represents the auto-bent sample, the blue dotted line represents the straight sample, and the purple dashed line represents the single-component sample. These are the best redshifts (see §3.2) for each optically identified radio source. The visual-bent sample peaks at a lower redshift than the other samples. This is most likely due to the nature of the selection. It is easier to classify a source as a bent-double source if it is at lower redshift and angularly larger on the sky.

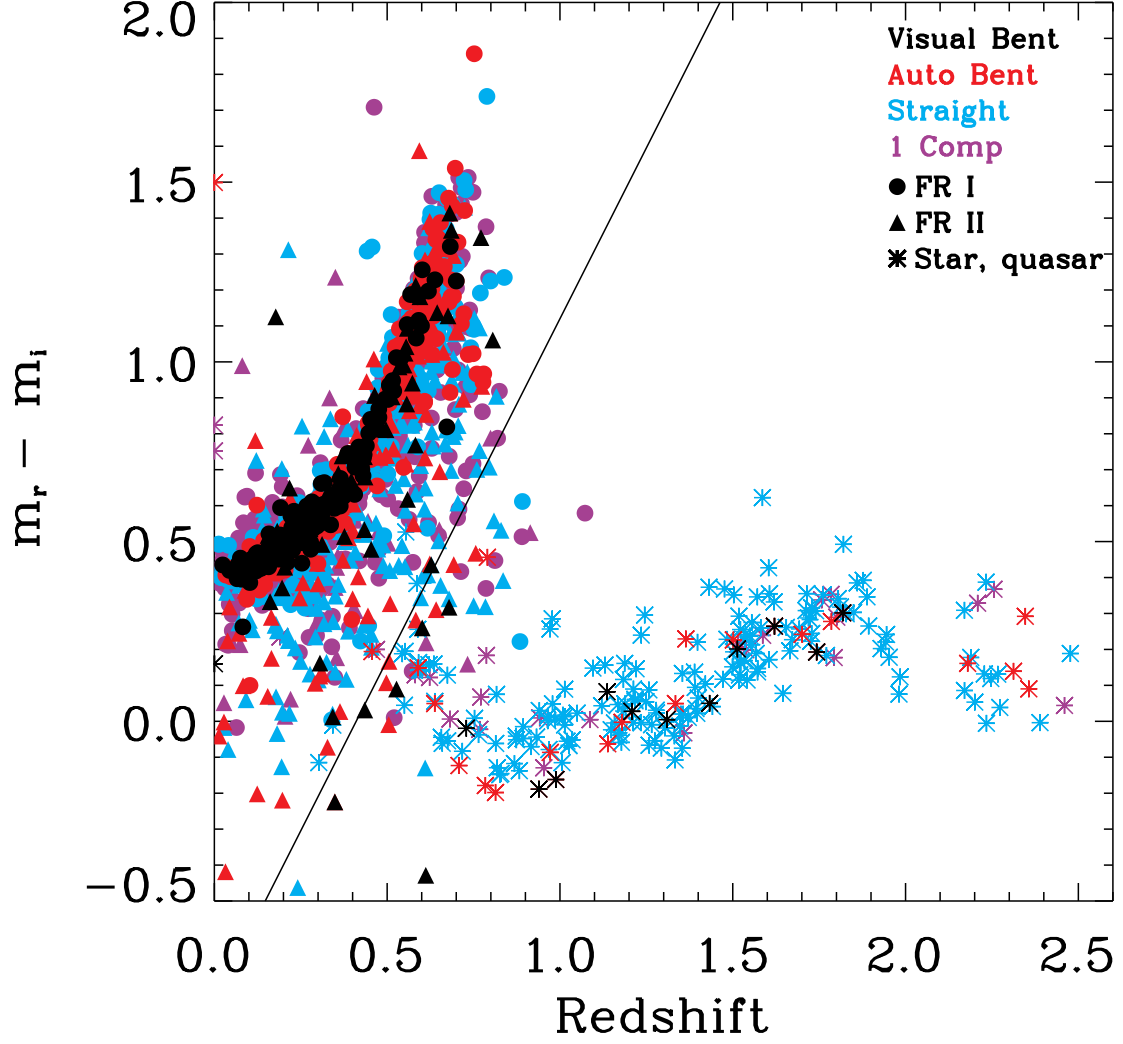


Figure 7. Redshift vs. color for our radio source hosts. The symbols are the same as in Figure 4. The point sources, as identified by SDSS (either misidentified stars or quasars), are represented by asterisks. For the most part, the elliptical galaxies at the centers of galaxies clusters should have similar colors. Thus, as redshift increases, the color of the galaxy should get redder. The solid line represents the cut-off between sources that are likely to be red elliptical galaxies and those that are likely quasars.

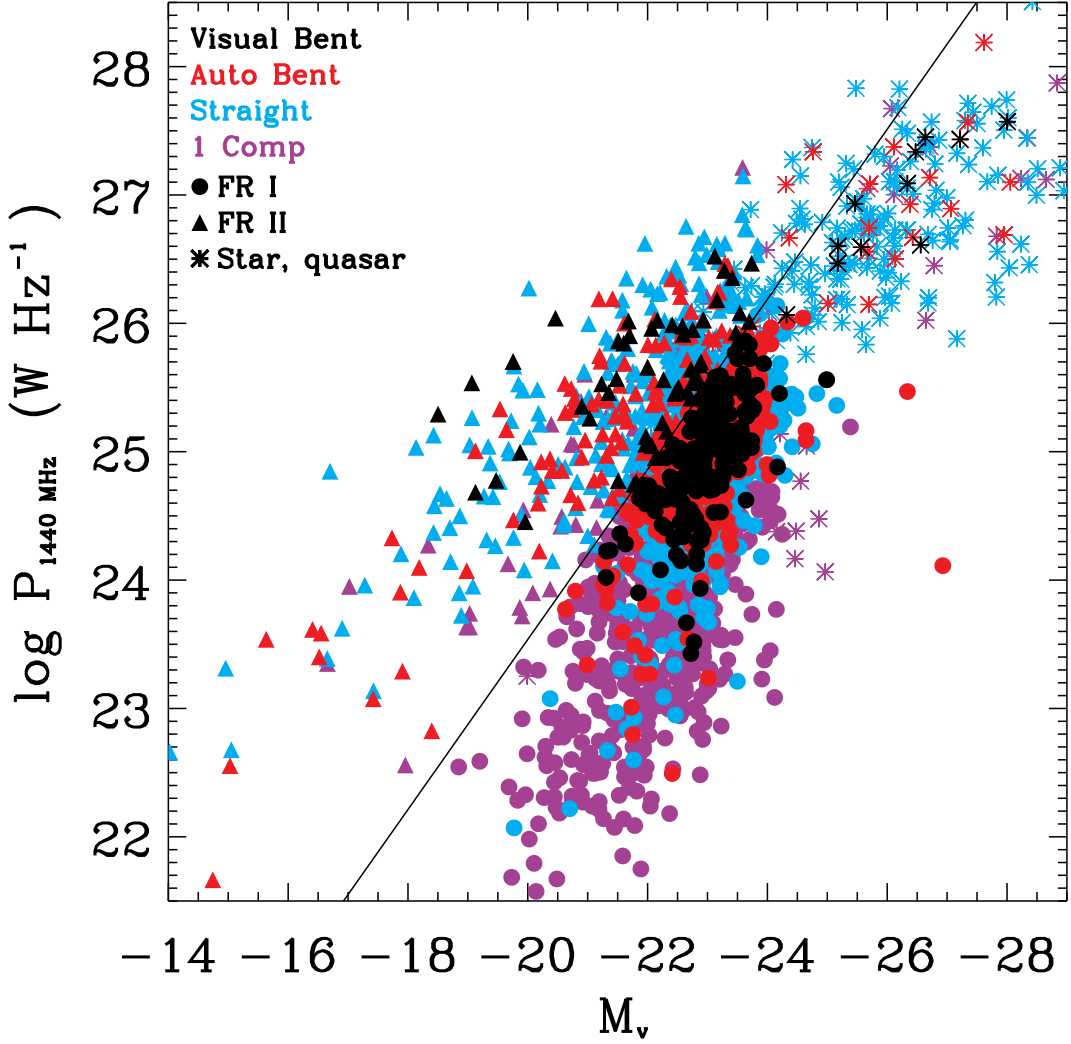


Figure 8. Absolute V-magnitude vs. 1440 MHz radio power for sources in our samples. The symbols are the same as in Figure 7. Ledlow & Owen (1996) showed that based on a comparison of a source's absolute V magnitude and its radio power, a distinction could be made between FR I and FR II sources. The line represents the division that Ledlow & Owen (1996) found between FR I and FR II sources. The FR II's are above and to the left of the line and the FR I's are below and to the right of the line. Using this, we were able to classify sources as either FR I or FR II and use this classification to make comparisons between cluster richness for each type.

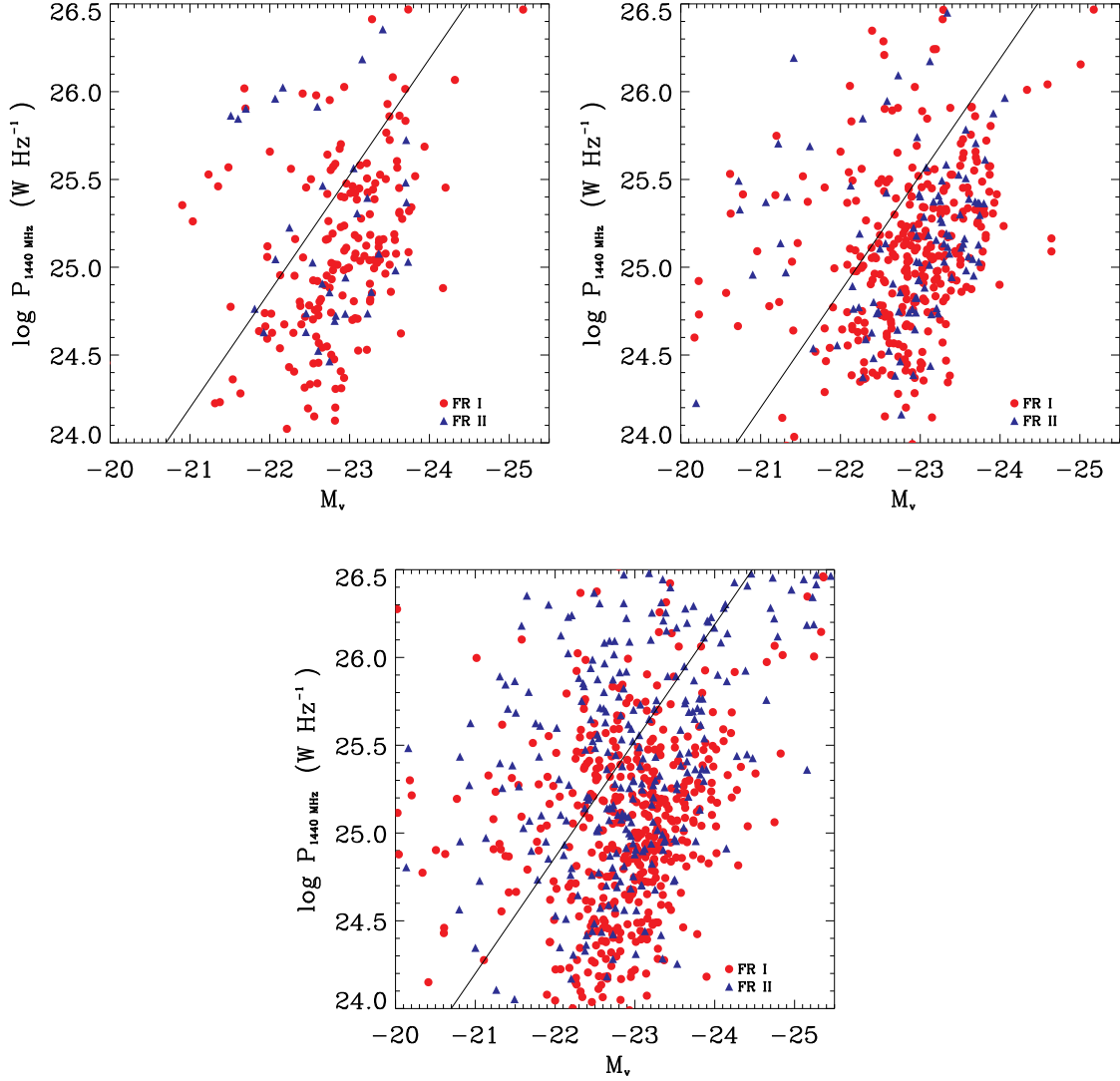


Figure 9. Absolute V-magnitude vs. 1440 MHz radio power for sources in our samples with visual FR classifications. Filled red circles represent sources we have visually classified as FR I and blue filled triangles represent sources we have visually classified as FR II. The top-left panel shows the results of the visual-bent sample, the top-right panel shows the results of the auto-bent sample, and the bottom panel shows the results of the straight sample. We find that while there is a general trend for the FR I type radio sources to be located below the threshold set forth in Ledlow & Owen (1996), it does not hold for all sources, in agreement with Best (2009).

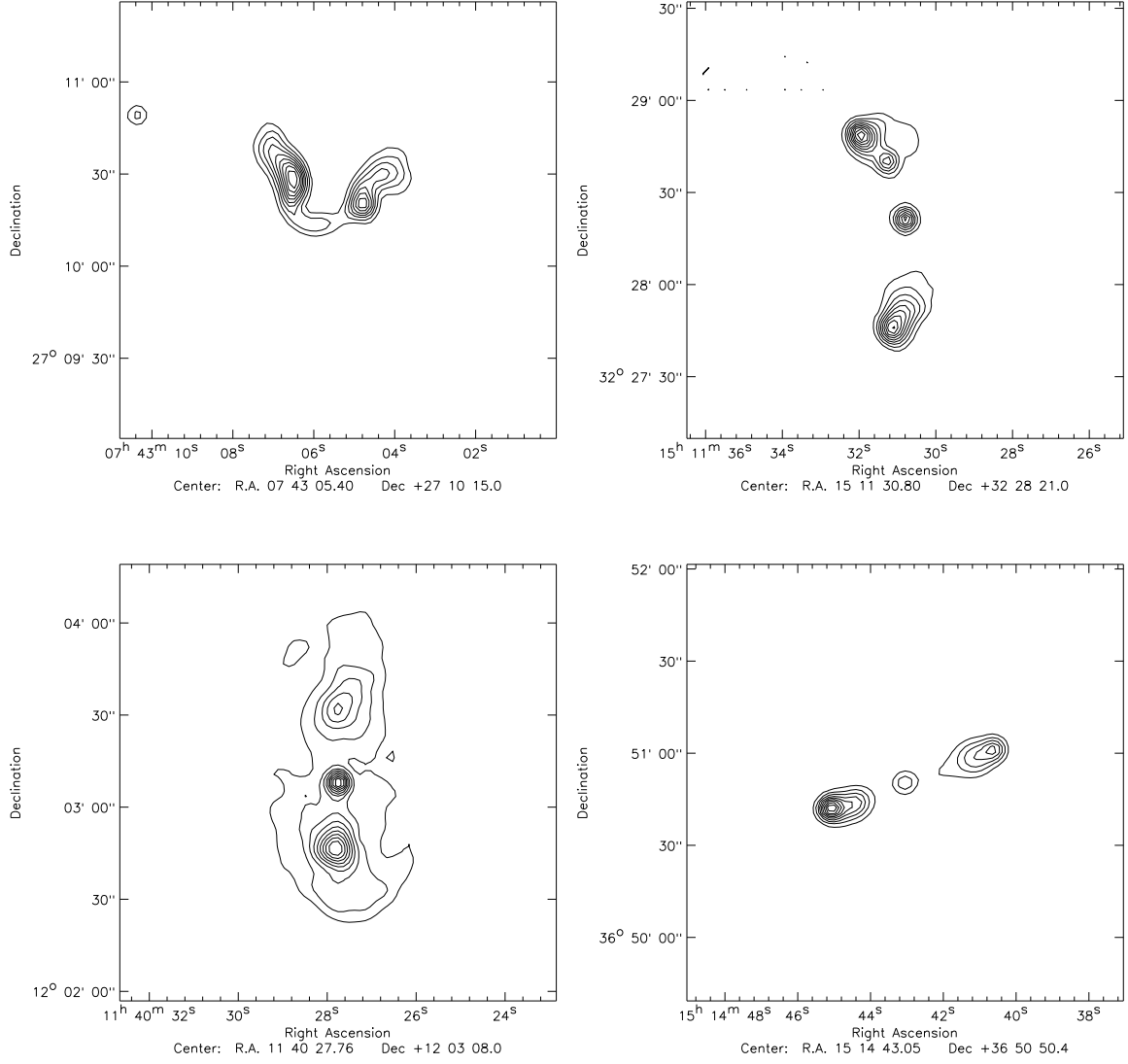


Figure 10. Radio contours of characteristic sources from our samples. The top panels both show bent-lobed sources, the left-hand panel illustrates an example of a bent FR I source, the right-hand panel is an example of a bent FR II source. The bottom panels both show straight-lobed radio sources, the left-hand panel is an example of a straight FR I source, the right-hand panel is an example of a straight FR II source. The contours are linearly scaled with ten contours with minimum contours of 0.76 mJy, 1.2 mJy, 3.1 mJy, and 13 mJy and maximum contours of 9.1 mJy, 16 mJy, 31 mJy, and 160 mJy for the upper-left, upper-right, lower-left, and lower-right panels, respectively.

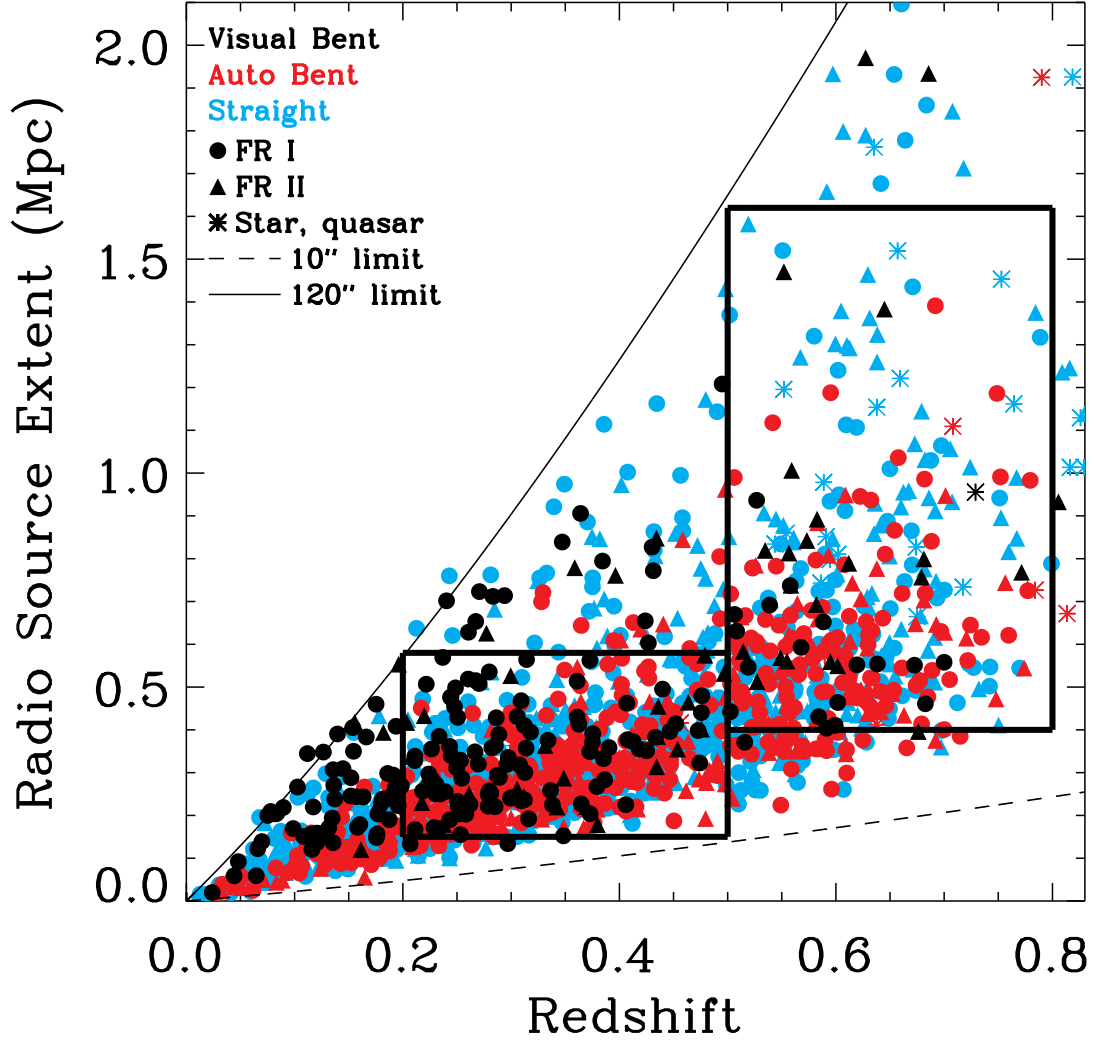


Figure 11. Radio source extent vs. redshift. The symbols are the same as in Figure 7. The dashed line corresponds to the physical extent at a given redshift for a multi-component source that has a total angular size of $10''$. This is the lower limit to the detection and identification of a multi-component source in the FIRST survey. The solid line corresponds to an angular size of $120''$. This is the approximate upper limit for the physical extent of our sources. The few sources above this line are slightly larger owing to the extent of the lobes. The boxes represent samples of sources that are without selection effects for physical size and/or redshift. The two boxes are used to constrain the samples in order to compare similar distributions of sources.

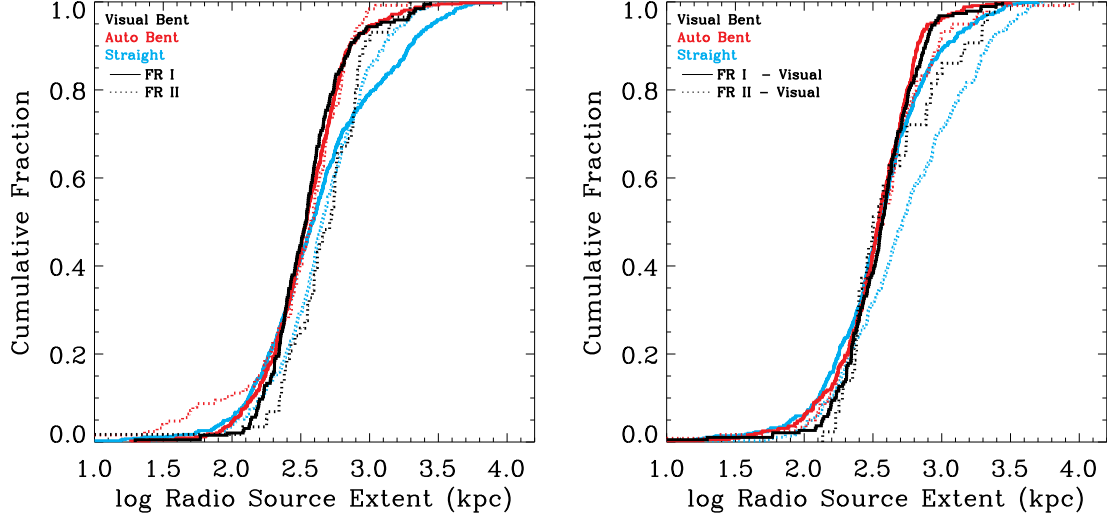


Figure 12. The cumulative distribution of the physical extent of FR I and FR II sources in the different samples. The solid lines represent the distributions of the FR I sources and the dotted lines represent the distributions of the FR II sources. Black solid and dotted lines represent the visual-bent sample, red for the auto-bent sample, and blue for the straight sample. The left panel shows the distribution when using the Ledlow & Owen (1996) criteria for determining FR I/II morphology and the right panel is the distribution when using our visual FR I/II classification. In general, the FR II sources are larger than the FR I sources.

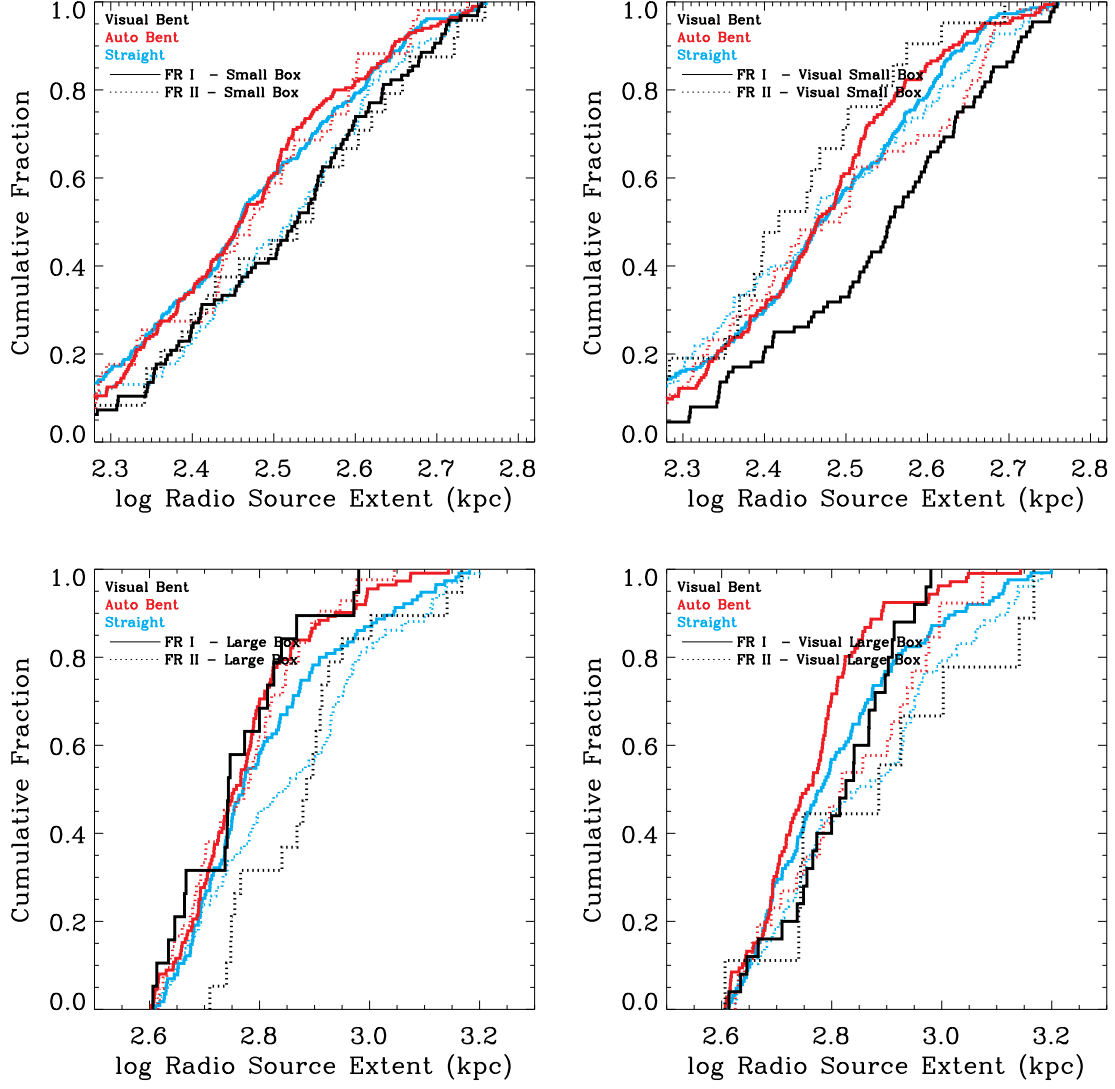


Figure 13. A reproduction of Figure 12, except using only sources contained within the small (top panels) box from Figure 11 and the large box (bottom panels). Specifically, the upper-left panel shows the cumulative distribution of the radio source extent for sources with FR classification derived using the Ledlow & Owen (1996) criteria and located within the small box in Figure 11. The upper-right panel shows the same distribution for sources located within the small box in Figure 11 and classified as FR I or II based on our visual inspection. The lower-left panel shows the distribution of sources contained in the large box and classified as FR I or II based on Ledlow & Owen (1996) and the lower-right panel shows the distribution of sources contained in the large box and classified as FR I or II based on our visual inspection. In general, we see that FR II sources are larger than FR I sources.

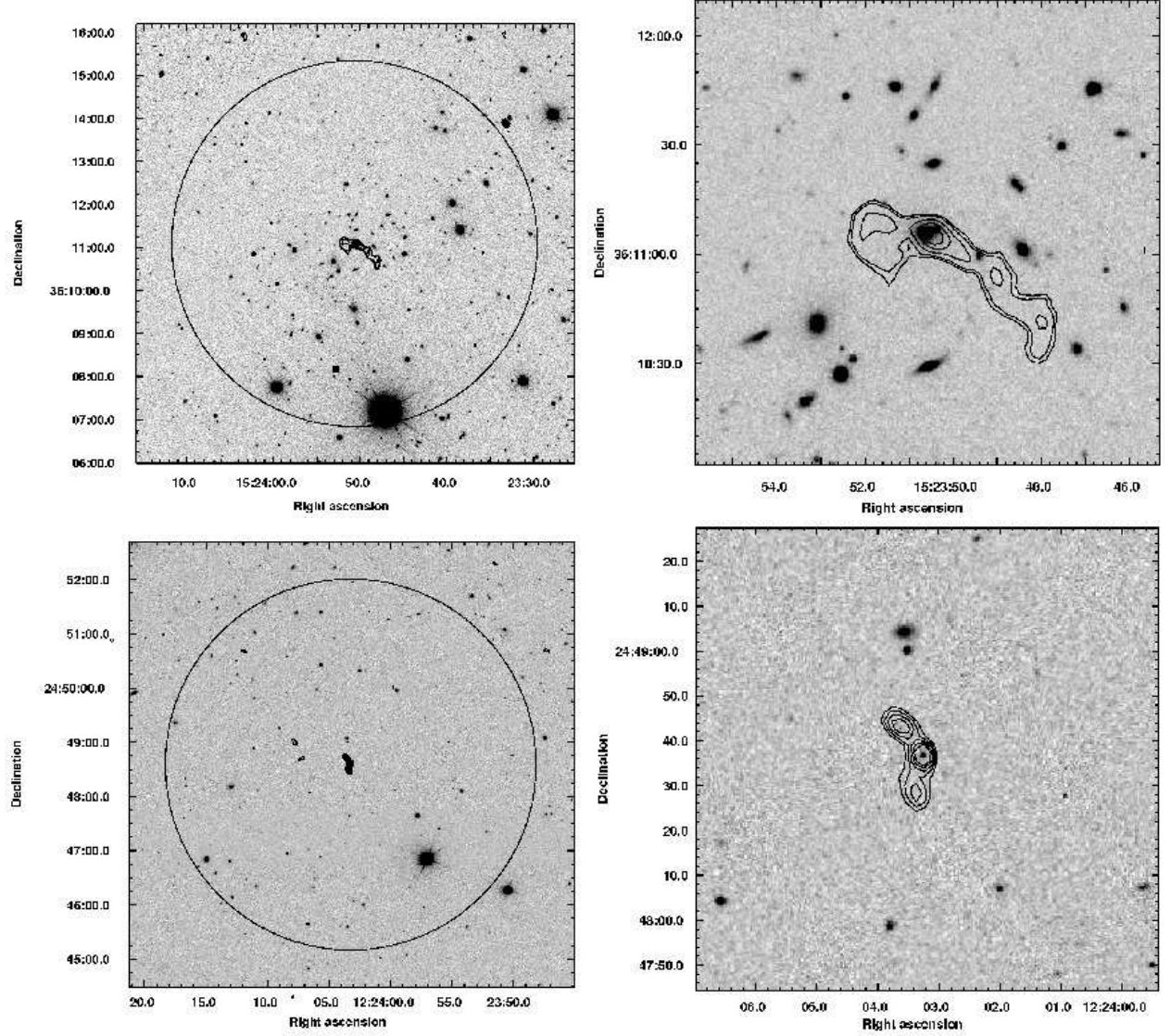


Figure 14. SDSS *r*-band images with FIRST contours overlaid for both rich and poor environments. The left-hand panels show a view of the area in which we looked for cluster members (illustrated by the circle showing an area with a radius of 1.0 Mpc around the radio source), the right-hand panels show a zoomed in (250×250 kpc) view. The top panels show a rich cluster located at a redshift of $z = 0.25$ with $N_{1.0}^{-19} = 102$. The bottom panels show a non-cluster located at a redshift of $z = 0.32$ with $N_{1.0}^{-19} = -9$. Both sources are visually selected bent sources. The contours are square root scaled with five contours with minimum contours of 0.55 mJy and maximum contours of 1.1 mJy and 4 mJy for the upper and lower panels, respectively.

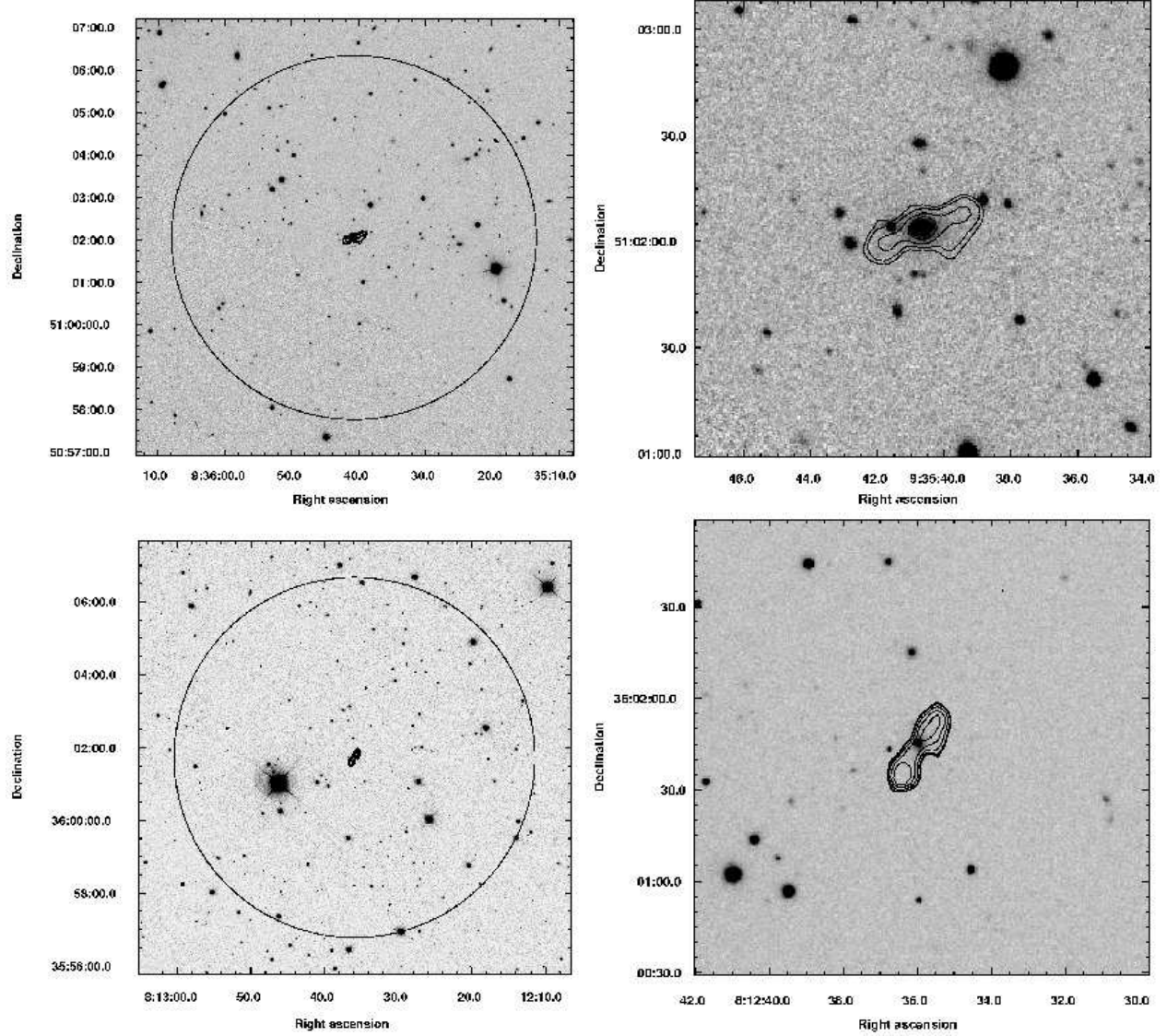


Figure 15. SDSS r -band images with FIRST contours overlaid for both rich and poor galaxy environments around straight sources. The left-hand panels show a view of the area in which we looked for cluster members (illustrated by the circle showing an area with a radius of 1.0 Mpc around the radio source), the right-hand panels show a zoomed in (250×250 kpc) view. The top panels show a rich cluster located at a redshift of $z = 0.25$ with $N_{1.0}^{-19} = 72$. The bottom panels show a poor environment located at a redshift of $z = 0.20$ with $N_{1.0}^{-19} = -25$. Both sources are automatically selected straight sources. The contours are square root scaled with five contours with minimum contours of 0.55 mJy, and maximum contours of 5 mJy and 2 mJy for the upper and lower panels, respectively.

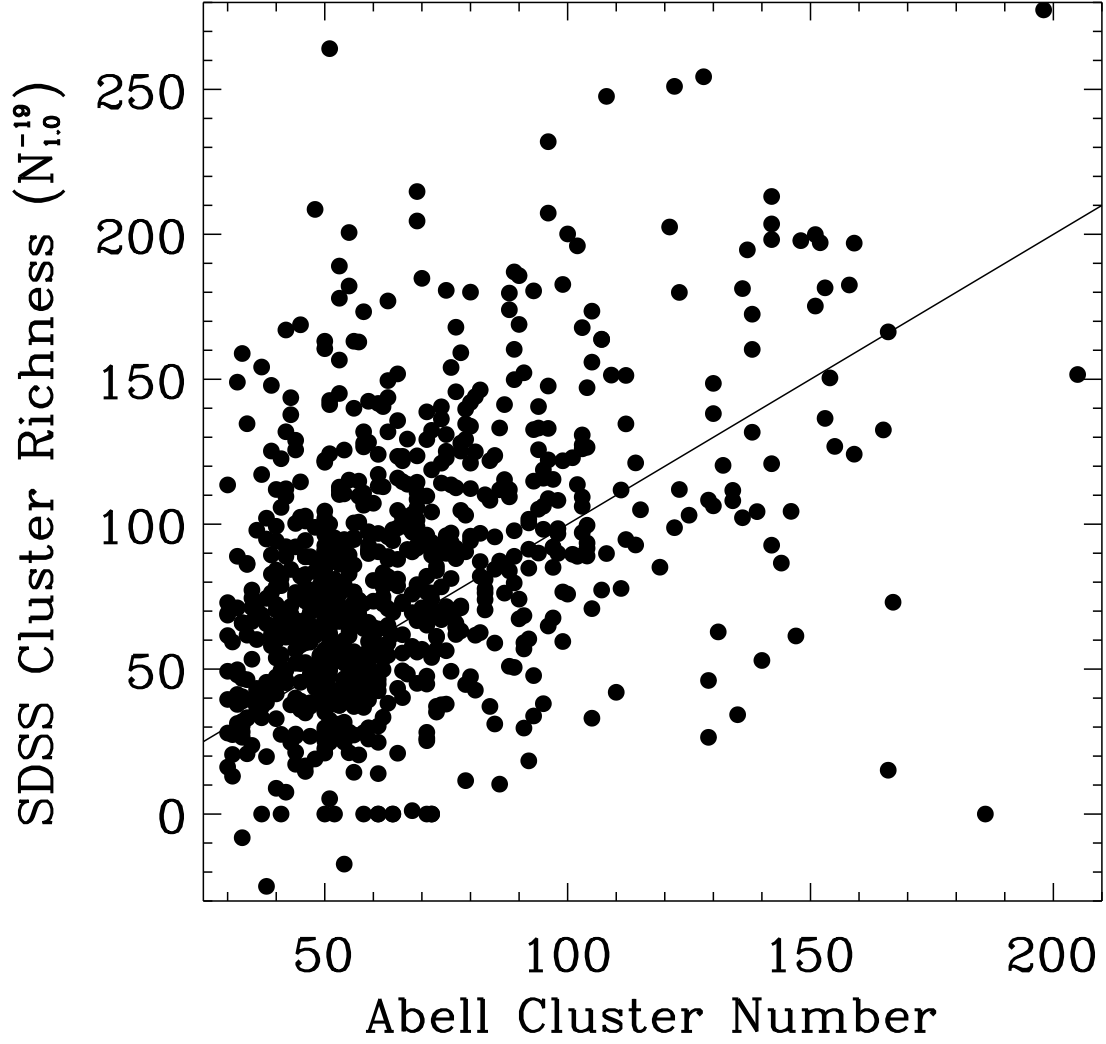


Figure 16. The relationship between the number of cluster members cataloged by Abell (1958) compared to our $N_{1.0}^{-19}$ method. The line represents a one-to-one correlation between cluster galaxy counts. There is a general trend (with a Spearman correlation coefficient of 0.423) for the richer clusters in the Abell (1958) catalog to also have higher $N_{1.0}^{-19}$, but there is considerable scatter.

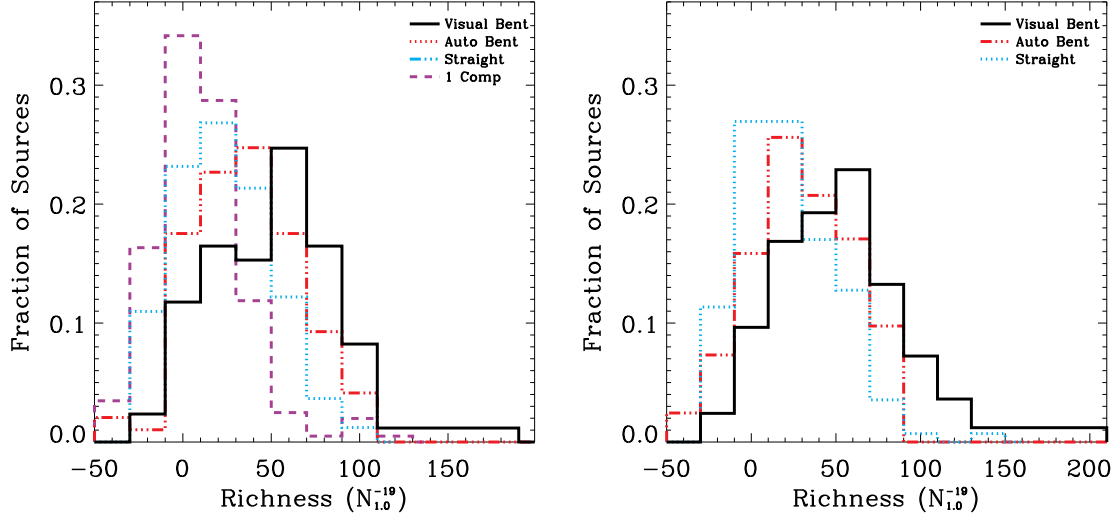


Figure 17. The distribution of cluster richness associated with FR I sources (classified using the Ledlow & Owen (1996) criteria [left panel] and visually [right panel]) for the different samples. The black solid line represents the visual-bent sample, the red dotted line represents the auto-bent sample, the blue dash-dotted line represents the straight sample, and the purple dashed line represents the single-component sample. The single-component sample is not included in the right panel because they were not classified visually. The visual-bent sample is the best sample for selecting rich clusters. In general, bent sources are more often associated with rich cluster environments than non-bent sources and extended sources are more often associated with rich environments than single-component sources.

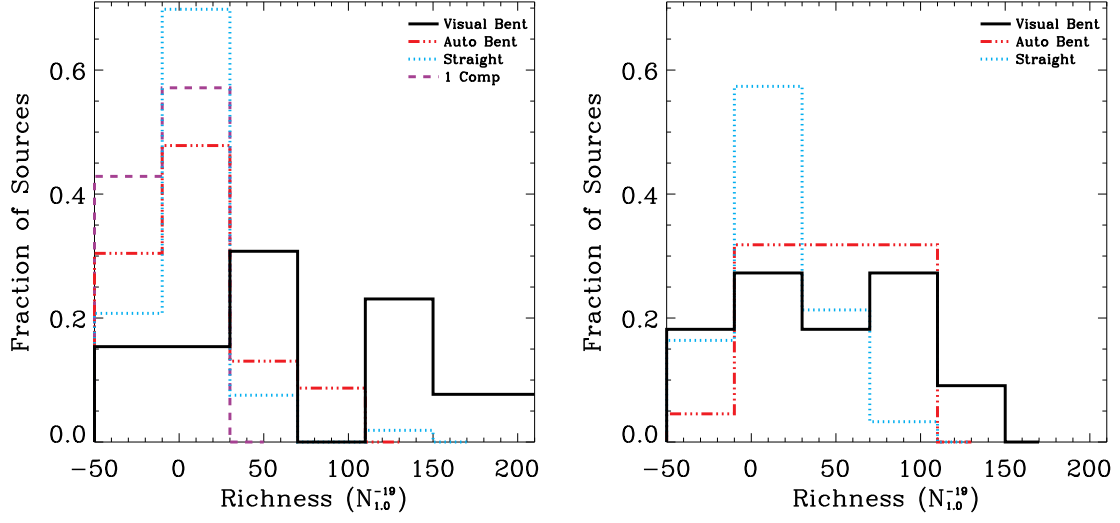


Figure 18. The distribution of cluster richness associated with FR II sources (classified using the Ledlow & Owen (1996) criteria [left panel] and visually [right panel]) for the different samples. The line styles and colors are the same as in Figure 17. The single-component sample is not included in the right panel because they were not classified visually. The visual-bent sample is the best sample for selecting rich clusters. In general, bent sources are more often associated with rich cluster environments than non-bent sources and extended sources are more often associated with rich environments than single-component sources.

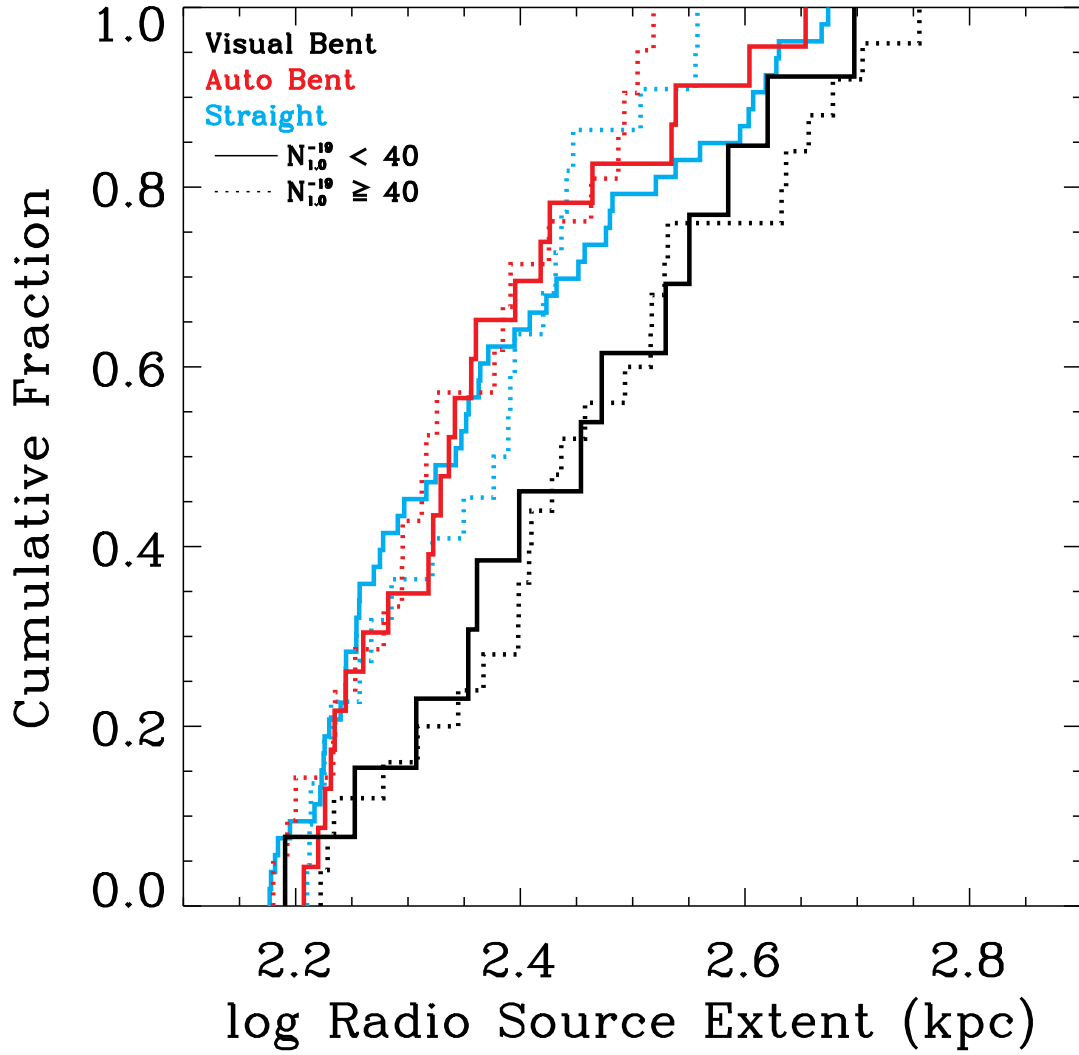


Figure 19. The relationship between radio source physical extent and cluster richness. The line colors and styles are the same as in Figure 12. All of the sources in each sample that are contained within the small box from Figure 11 and have redshifts and magnitudes such that there is no need for a Schechter correction (see §4.3) are included. There appears to be no difference in the size distributions of sources in clusters versus those not in clusters.

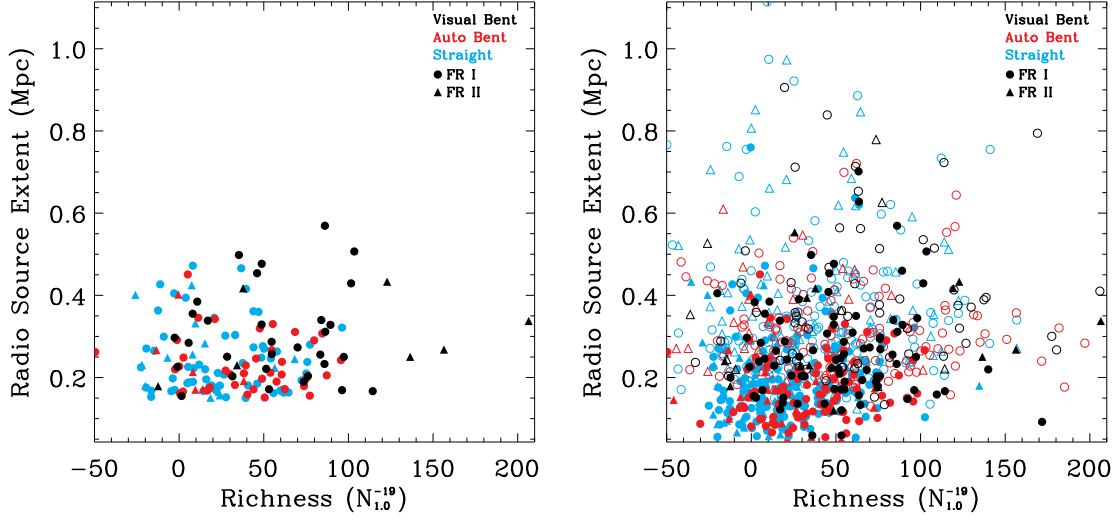


Figure 20. The relationship between the richness of a cluster and the physical size of the radio source associated with that cluster. The left-hand panel plots only those sources in the small box from Figure 11 and need no Schechter correction (see §4.3). The right-hand panel shows all sources, including those with Schechter corrections and located outside of the small box. The symbols are the same as in Figure 7. The sources with Schechter corrections in the range of $1 < f_c \leq 3$ are identified as open symbols. There does not appear to be a relationship between cluster richness and radio source size.

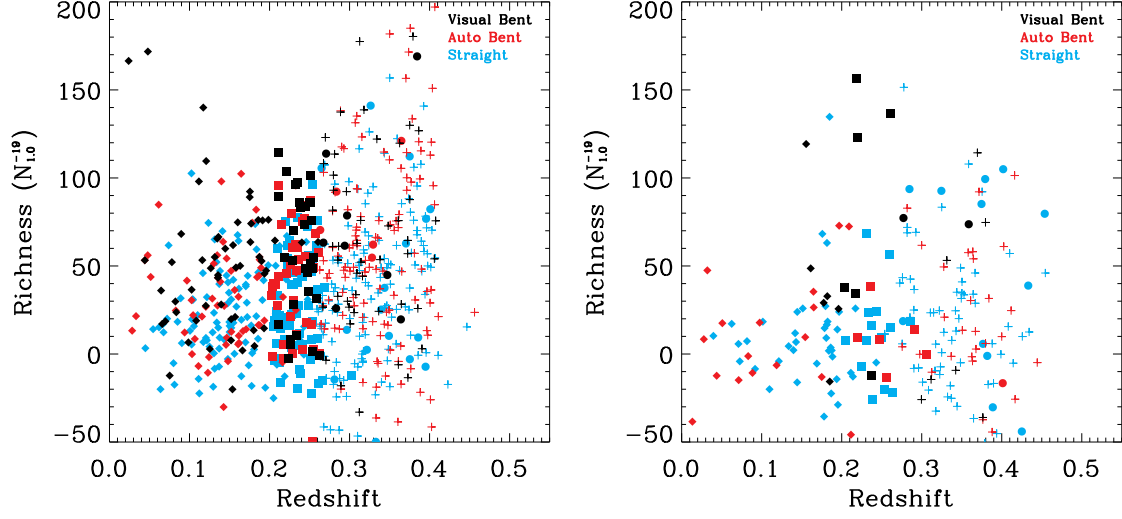


Figure 21. Redshift vs. richness. We have plotted the FR I (left panel) and FR II (right panel) sources separately, using the Ledlow & Owen (1996) criteria to determine morphology. The filled-diamonds represent sources that are not contained within the small box from Figure 11 and have no Schechter correction (see §4.3). The filled-squares represent sources contained within the small box and have no Schechter correction. The pluses are sources that are contained within the small box but have $1 < f_c \leq 3$. Finally, the filled-circles represent sources that are not within the small box and have $1 < f_c \leq 3$. Black symbols represent the visual-bent sample, red symbols represent the auto-bent sample, and blue symbols represent the straight sample. Our results show a possible trend of the richest clusters being associated with sources at higher-redshifts.

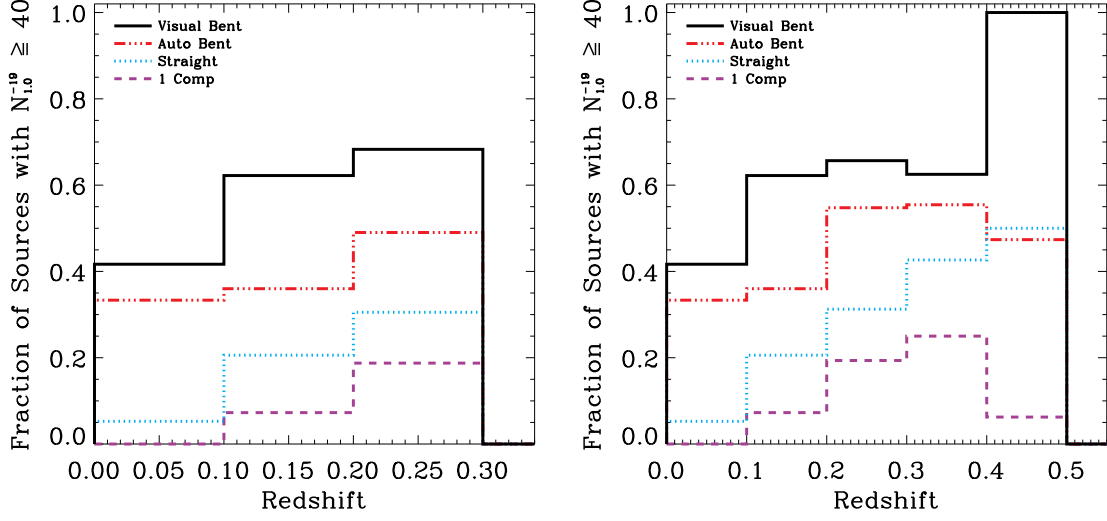


Figure 22. The fraction of sources in each redshift bin that are associated with clusters (those having $N_{1.0}^{-19} \geq 40$) compared to the total number of radio sources with optical counterparts in each redshift bin. The line styles and colors are the same as in Figure 17. The left-hand panel shows the results when only taking into account those sources that have no Schechter correction (see §4.3). The right-hand panel includes all sources with Schechter corrections up to our limit ($f_c \leq 3$) as described earlier.

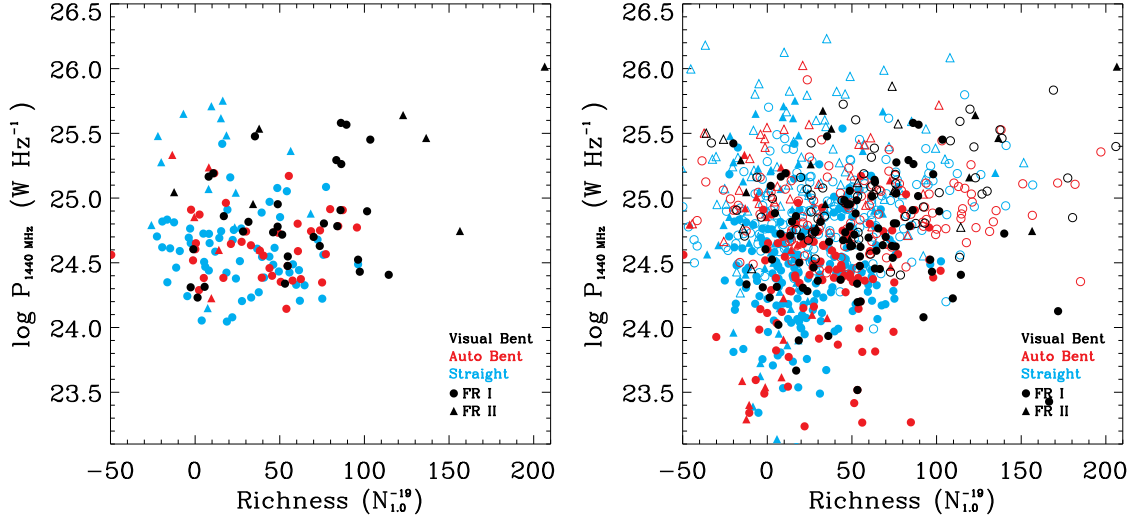


Figure 23. Richness vs. 1440 MHz radio power. The left-hand panel plots only those sources in the small box from Figure 11 and need no Schechter correction (see §4.3). The right-hand panel shows all sources that have Schechter corrections less than $f_c = 3$, including sources outside of the small box. The symbols are the same as in Figure 7. The open symbols represent sources that have Schechter corrections in the range $1 < f_c \leq 3$. It appears that the richest clusters in our samples have a radio power that is consistent with them being located on the FR I/II break. These are likely to be WATs.

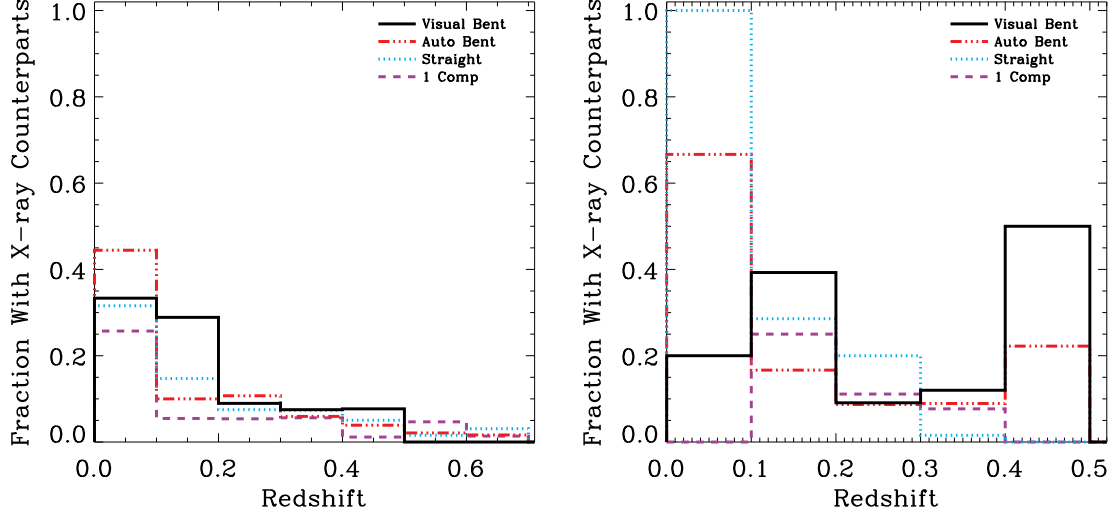


Figure 24. The fraction of sources in each redshift bin that have X-ray counterparts in the RASS-FSC within 1.0 Mpc of the position of the radio source compared to the total number of sources in each redshift bin. The line styles and colors are the same as in Figure 17. The left-hand plot shows the distribution for all of the radio sources with optical counterparts not in clusters and the right-hand plot is for only sources with $N_{1.0}^{-19} \geq 40$. We see that the fraction of sources with X-ray counterparts is much higher for those radio sources associated with clusters. The fraction of all optical sources associated with X-ray sources drops as the redshift increases. This is likely a result of flux limits of the RASS as well as the angular radius corresponding to 1 Mpc decreasing with redshift resulting in fewer chance matches at high z . X-ray sources associated with radio/optical sources at high redshift are unlikely to be detected. We see a similar trend for the sources associated with clusters with the exception of the last redshift bin in which the fraction associated with clusters increases. It is possible that this is due to the small number of sources residing in this redshift bin.